

# Results from the UCLA/FNPL Underdense Plasma Lens Experiment

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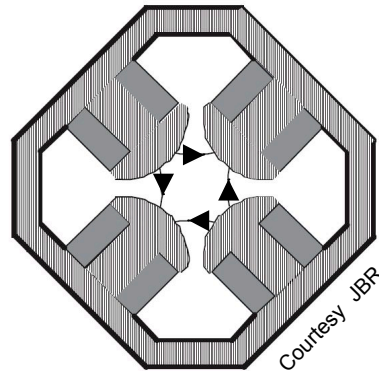
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# Advanced Electron Beam Lens

## Magnetic Quadrupoles

Uses magnetic forces to focus electron beam in one dimension at a time.

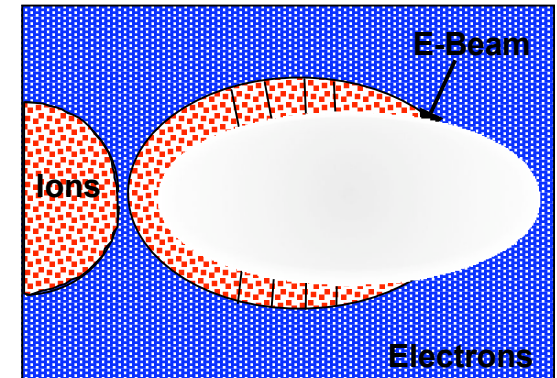


$$\vec{F}_{\perp} = q\vec{v} \times \vec{B}_{quad} = ecB'(y\hat{y} - x\hat{x})$$

$$B' \approx 250 \text{ T/m} \quad \text{State-of-the-Art Superconducting Quad}$$

## Underdense Plasma Lens

Uses electrostatic forces to focus electron beam in both dimensions.

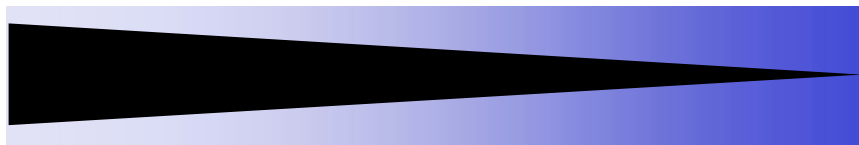


$$\vec{F}_{\perp} = q\vec{E}_{ion} = 2\pi e^2 n_p (-y\hat{y} - x\hat{x})$$

$$B'_{equivalent} = 3 \times 10^{-11} n_p \text{ T/m}$$

### Adiabatic Focusing: Adiabatic increase in $B'$

- Circumvents limits on focusing due to synchrotron radiation induced chromatic aberrations.
- Plasma lens are ideally suited for adiabatic focusing.



Even “weak” plasma lens are immensely strong:

**150 T/m at  $5 \times 10^{12} \text{ cm}^{-3}$**

**1500 T/m at  $5 \times 10^{13} \text{ cm}^{-3}$**

With appropriate parameters 70% - 80% of the beam is focused.

# Plasma Lens Development

## Overdense

$$n_b \ll n_p$$

Plasma cancels beam's space charge and remaining beam magnetic forces focus the beam

$$F_r \approx 2\pi n_b e^2 r$$

Since  $n_b$  is not generally uniform, overdense lens have significant aberrations.

## Underdense

$$n_b \gtrsim \frac{n_p}{2}$$

Plasma electron ejected from beam entirely, uniform ion column focuses beam.

$$F_r = 2\pi n_p e^2 r$$

$n_p$  can easily be both uniform and adjustable.

For a underdense gaussian plasma lens:

$$f = \frac{1}{KL} \quad KL = \int \frac{2\pi r_e n_p(l)}{\gamma} dl$$

### Overdense Channeling:

Rosenzweig et al. @ ANL (1989)  
 $n_p \sim 10^{13} \text{ cm}^{-3}$      $n_b \sim 10^{12} \text{ cm}^{-3}$   
 Plasma Length = 33 cm

### Overdense Lens:

Nakanishi et al. @ U. Tokyo (1991)  
 $n_p \sim 10^{11} \text{ cm}^{-3}$      $n_b \sim 10^{10} \text{ cm}^{-3}$   
 Plasma Length = 15 cm  
 Focal Length ~ 1 m

Hairapetian et al. @ UCLA (1994)  
 $n_p \sim 10^{12} \text{ cm}^{-3}$      $n_b \sim 10^{10} \text{ cm}^{-3}$   
 Plasma Length = 7.5 cm  
 Focal Length ~ 30 cm

Govil et al. @ LBNL (1999)  
 $n_p \sim 10^{14} \text{ cm}^{-3}$      $n_b \sim 10^{12} \text{ cm}^{-3}$   
 Plasma Length = 2 cm  
 Focal Length ~ 15 cm

Bolton et al. @ SLAC (2001)  
 $n_p \sim 10^{17} \text{ cm}^{-3}$      $n_b \sim 10^{16} \text{ cm}^{-3}$   
 Plasma Length = 3 mm  
 Focal Length ~ 15 mm

### Underdense Channeling:

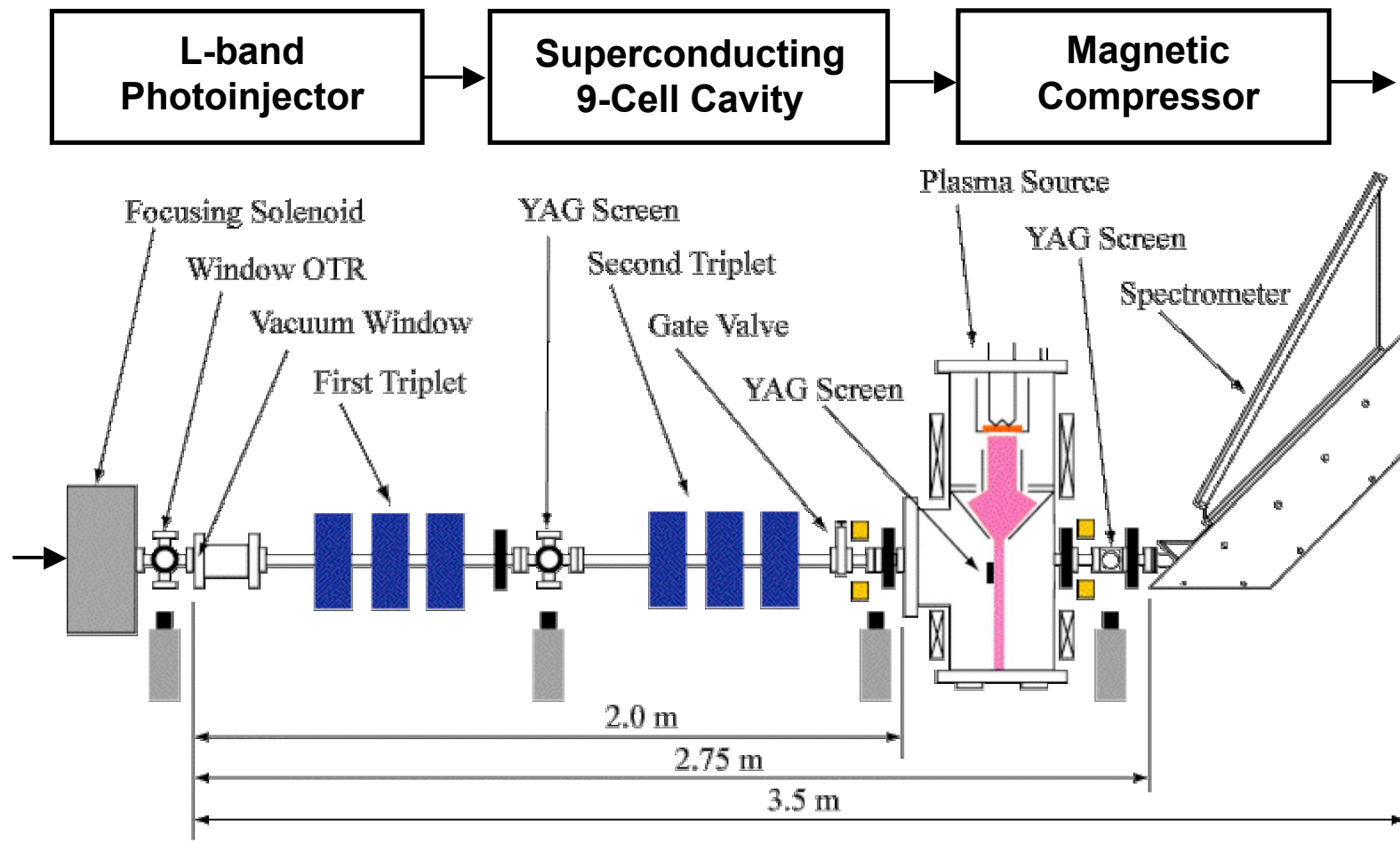
Barov et al. @ ANL (1998)  
 $n_p \sim 1 \times 10^{13} \text{ cm}^{-3}$      $n_b \sim 2 \times 10^{13} \text{ cm}^{-3}$   
 Plasma Length = 12 cm

Clayton et al. @ SLAC (2002)  
 $n_p \sim 10^{14} \text{ cm}^{-3}$      $n_b \sim 10^{15} \text{ cm}^{-3}$   
 Plasma Length = 1.4 m

# The Experimental Beam Line

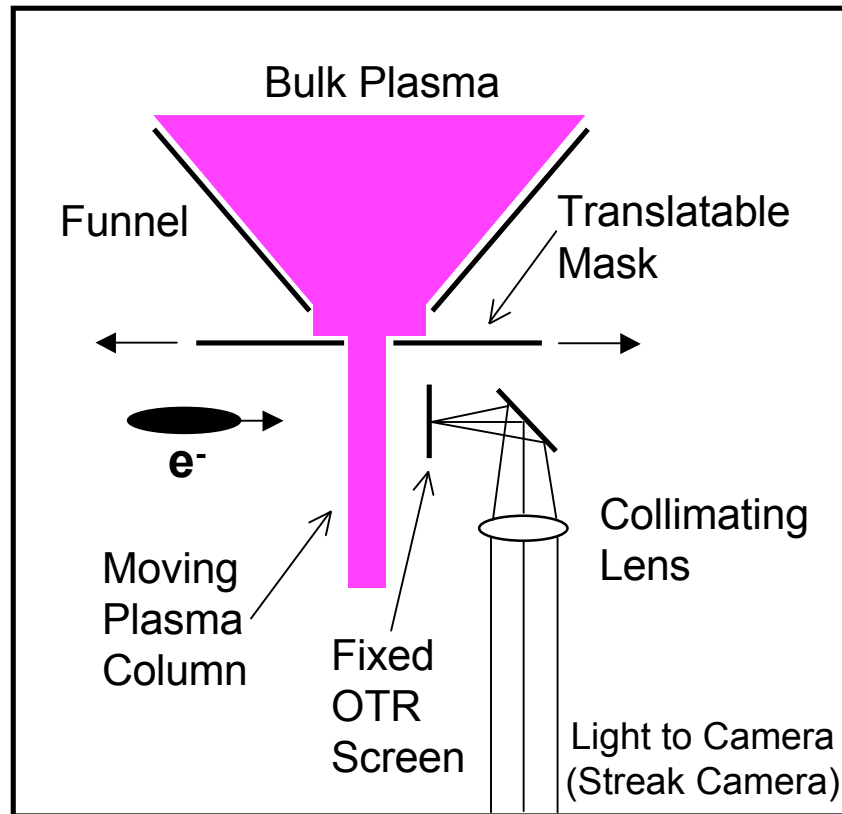
The experiment took place at the Fermilab NICADD Photoinjector Laboratory (FNPL) in the spring and early summer of 2005.

FNPL Beamline:

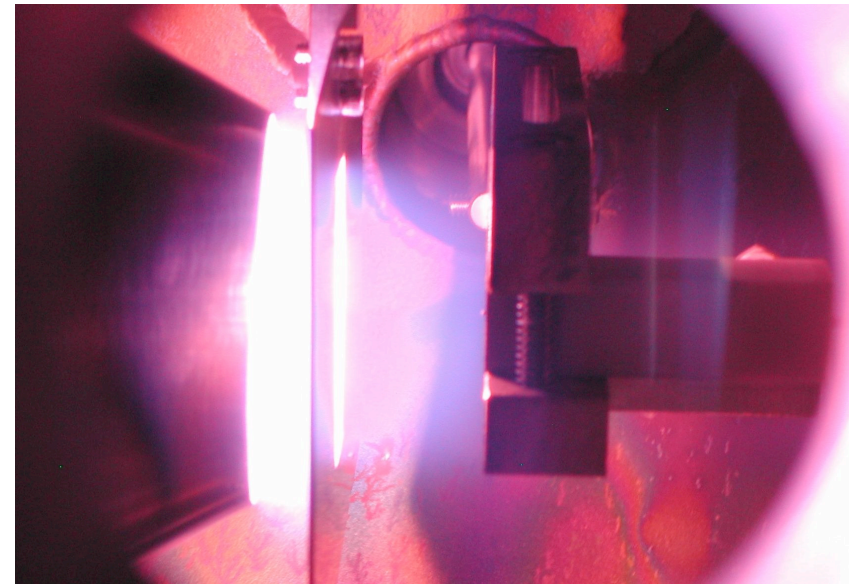
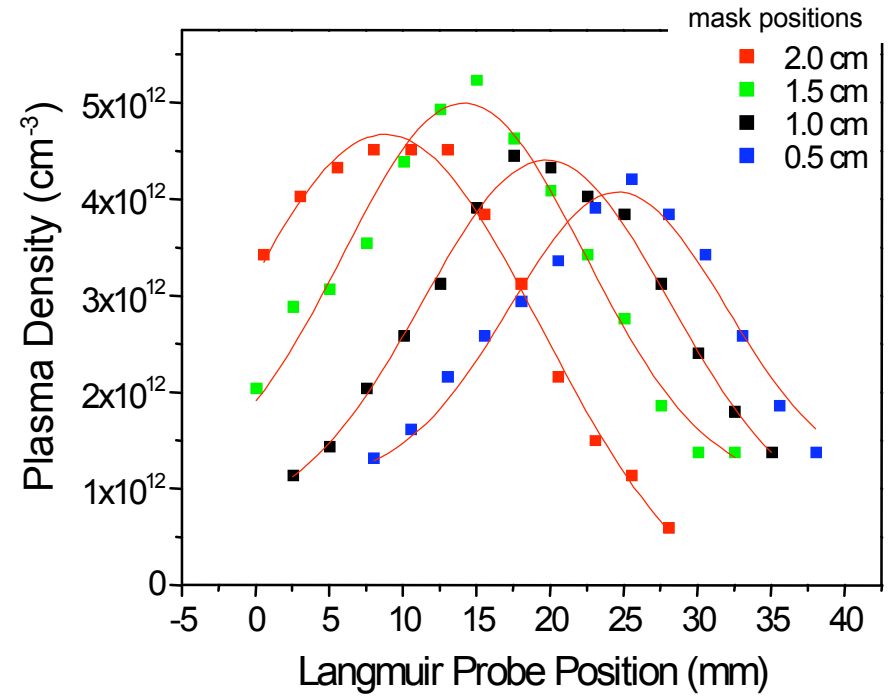


# Plasma Lens Apparatus

A 1.25 cm wide moving window is placed in front of the fixed 5 cm plasma column. The resulting translatable plasma column is used to focus the beam onto a fixed OTR screen.



Schematic of the Experiment



Photograph of Measurement in Progress

# Gaussian Underdense Plasma Lens

This is the first experiment to examine underdense plasma focusing in a well diagnosed true lens configuration with:

- High Demagnification
- Beam Focus Outside Plasma
- Variable Lens Position

## Achieved Experimental Parameters

<b>Peak Plasma Density</b>	4.7 x 10 <sup>12</sup> cm <sup>-3</sup>
<b>Plasma Skin Depth (c/ω<sub>p</sub>)</b>	3.6 mm
<b>Plasma Thickness (L<sub>p</sub>)</b>	9.9 mm
<b>Beam Energy</b>	15 MeV
<b>Beam Charge</b>	16 nC (10 <sup>10</sup> e <sup>-</sup> )
<b>Beam Duration (σ<sub>t</sub>)</b>	22 ps
<b>Initial Beam Radius (σ<sub>r</sub>)</b>	950 μm
<b>Beam Emittance (L<sub>n</sub>)</b>	90 mm-mrad
<b>Peak Beam Density</b>	2.2 x 10 <sup>12</sup> cm <sup>-3</sup>

$$f = \frac{1}{KL} = \sqrt{\frac{2}{\pi}} \frac{\gamma c^2}{\sigma_p \omega_p^2 \Big|_{peak}}$$

$$f_{predicted} = 1.5 \text{ cm}$$

$$f_{observed} \cong 1.9 \text{ cm}$$

**Threshold Operation:**

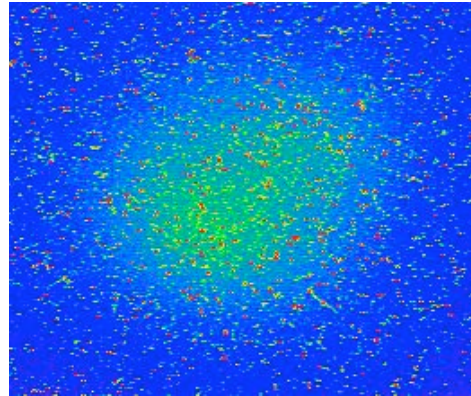
$$n_{beam} \approx \frac{n_p}{2}$$

# Analysis of Round Beam Focusing Results

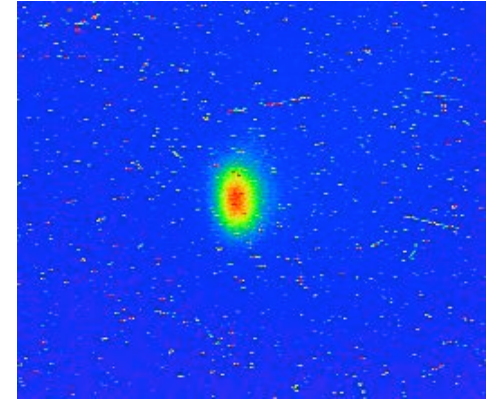
Beam Spot Before:  
x FWHM = 1630  $\mu\text{m}$   
y FWHM = 1540  $\mu\text{m}$   
 $n_b = 2.2 \times 10^{12} \text{ cm}^{-3}$

Beam Spot After (Ave.):  
x FWHM = 260  $\mu\text{m}$   
y FWHM = 420  $\mu\text{m}$   
 $n_b = 5 \times 10^{13} \text{ cm}^{-3}$

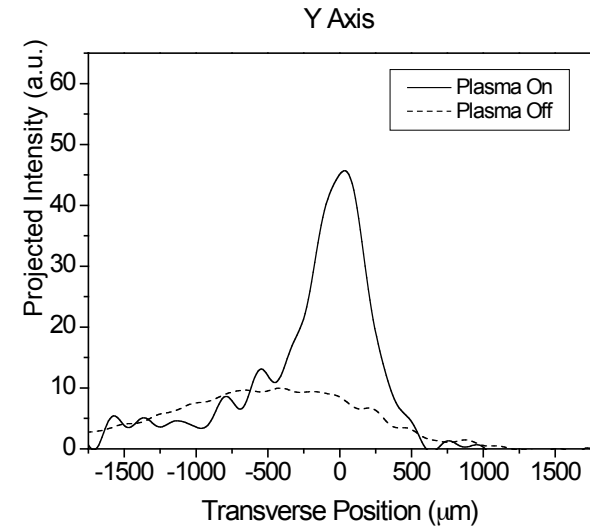
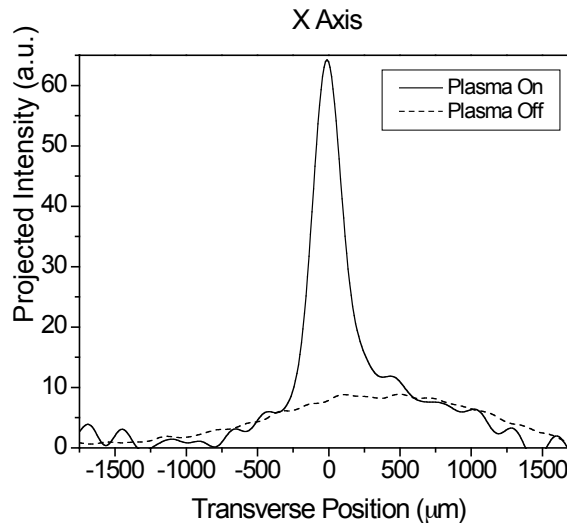
The average transverse area of the beam is reduced by a factor of 23.



Unfocused – 5 electron pulses



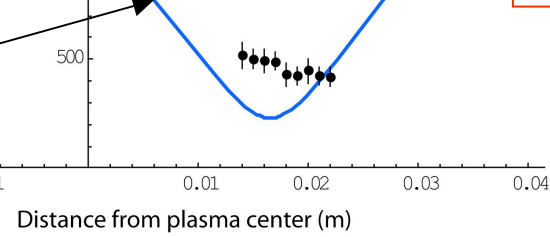
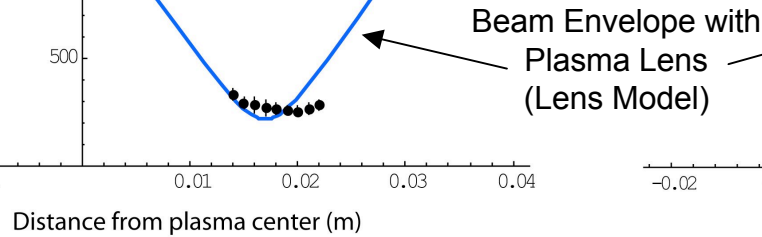
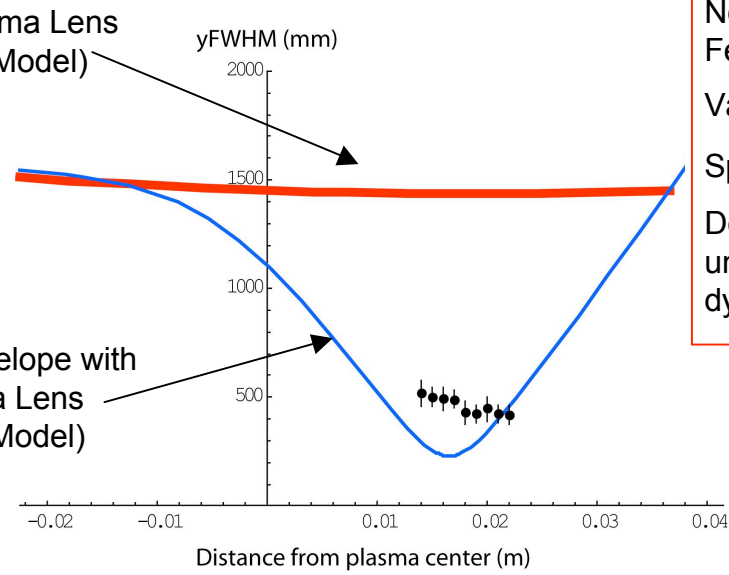
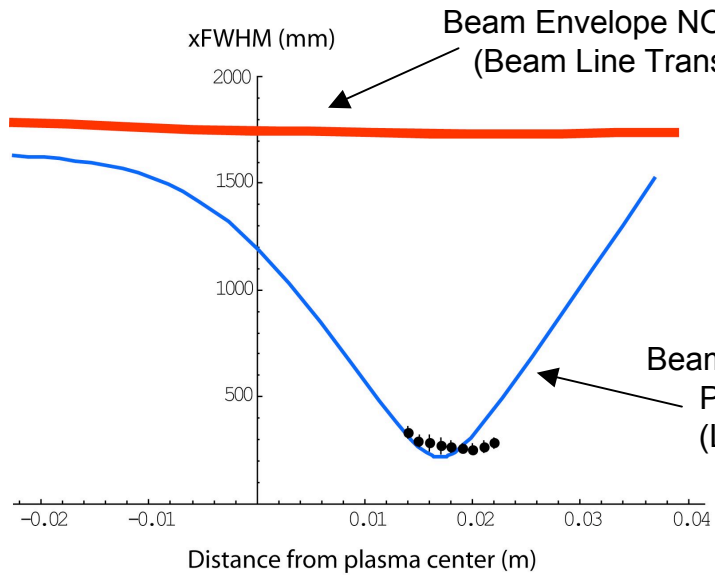
Focused – 1 electron pulse



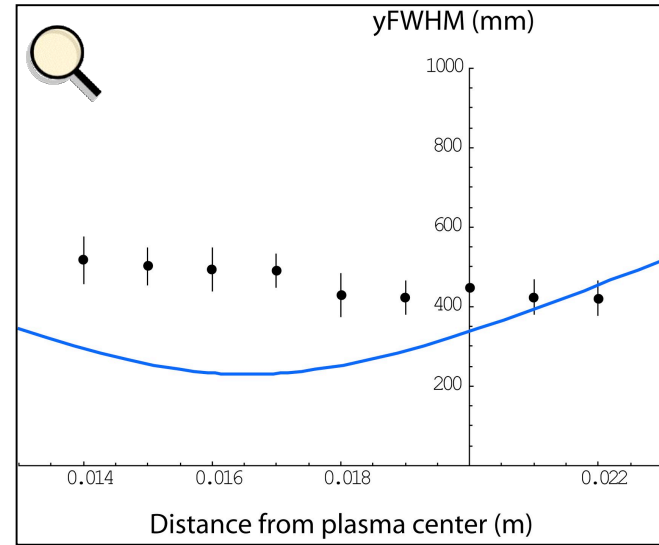
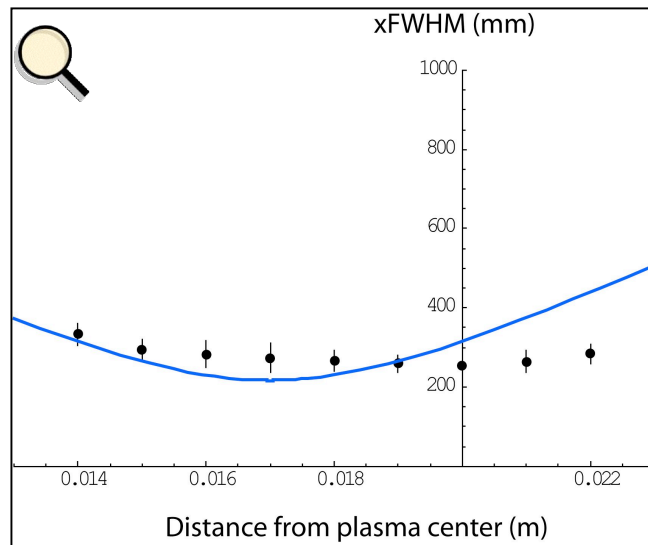
Plots of the image intensity of the above photographs (normalized to 1 electron pulse).

# Evolution of the Beam Envelope

**Model Ignores:**  
 Non-Gaussian Beam Features,  
 Variation in  $n_p$  and  $\sigma_p$   
 Space charge  
 Deviation from perfect underdense lens dynamics



Region Near Focal Point with Data:  
 Line is the evolution of the beam core.

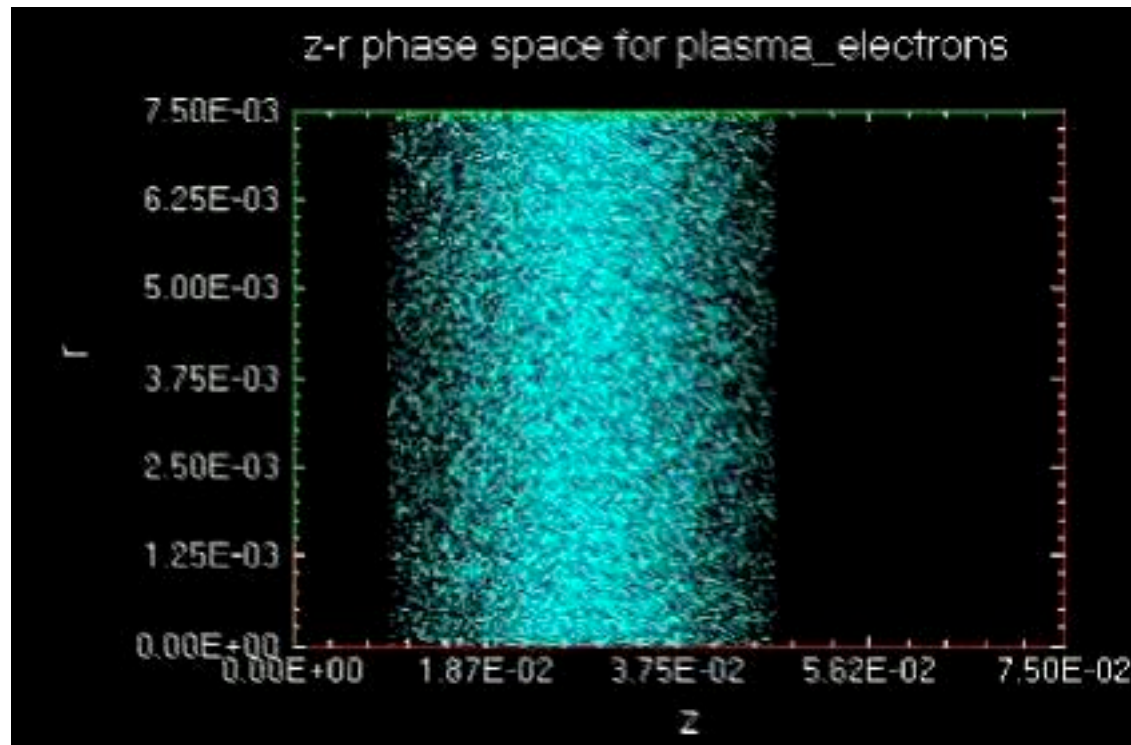




# Simulations: Plasma response

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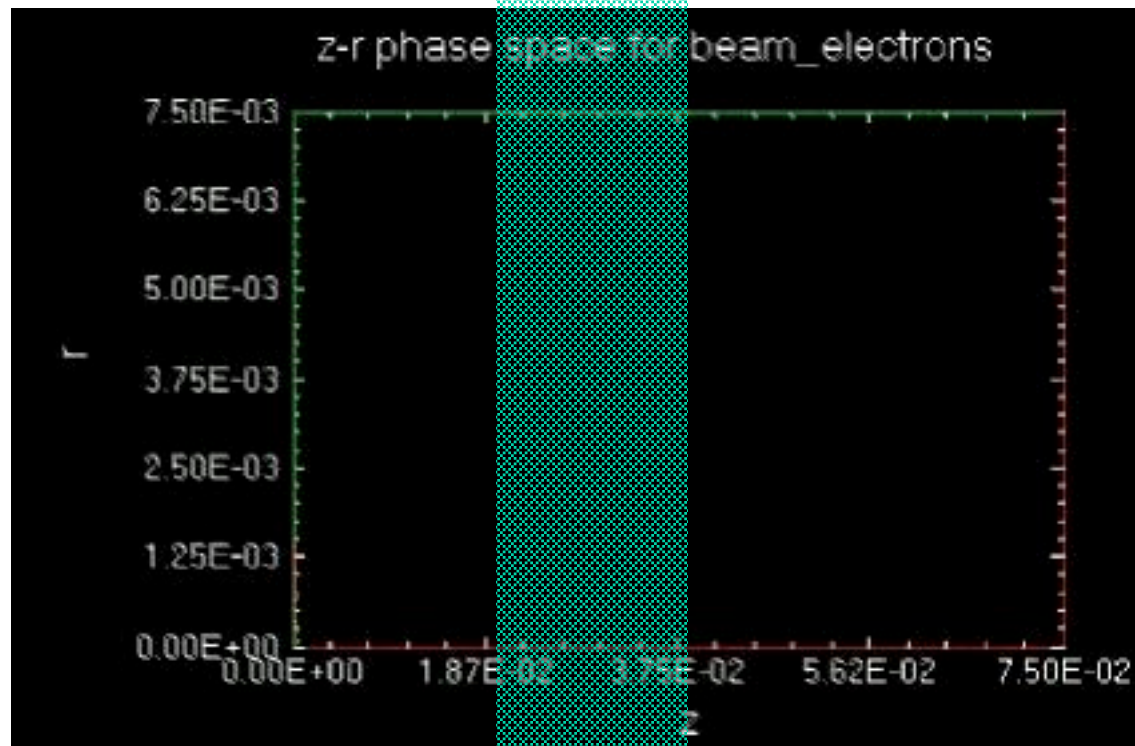
OOPIC simulation of plasma electrons as the electron bunch traverses from left ( $z=0$ ) to right.



→  
Beam Direction

# Simulations: Beam response

OOPIC simulation of beam from left ( $z=0$ ) to right.

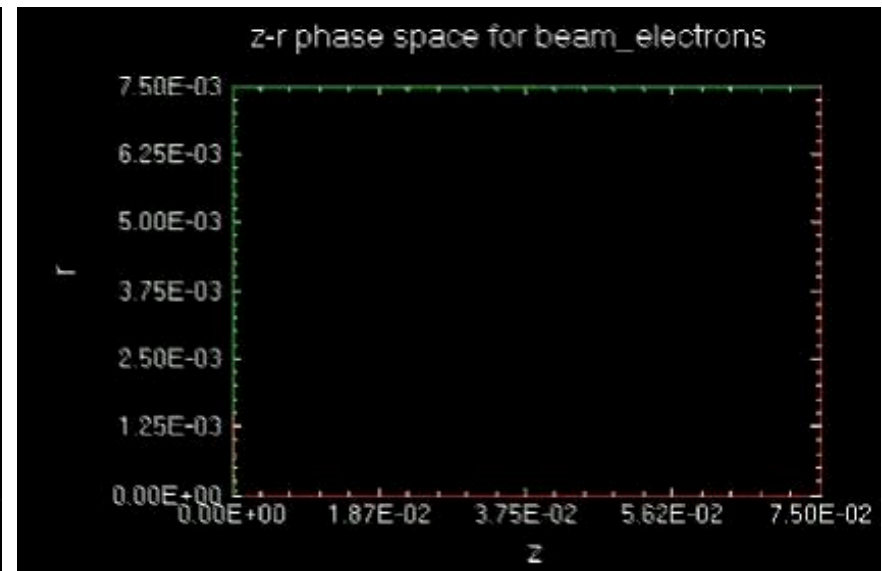
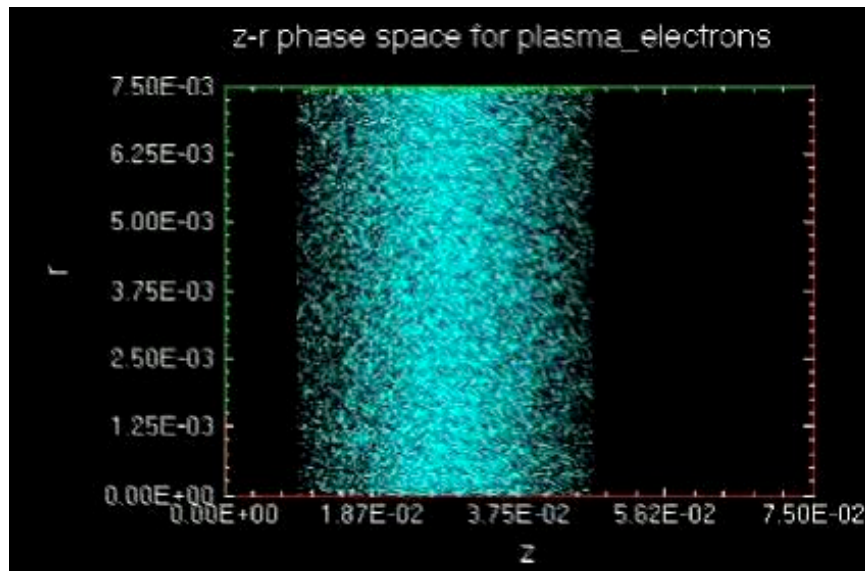


Plasma Column

OTR Screen

# Simulations: Beam and Plasma

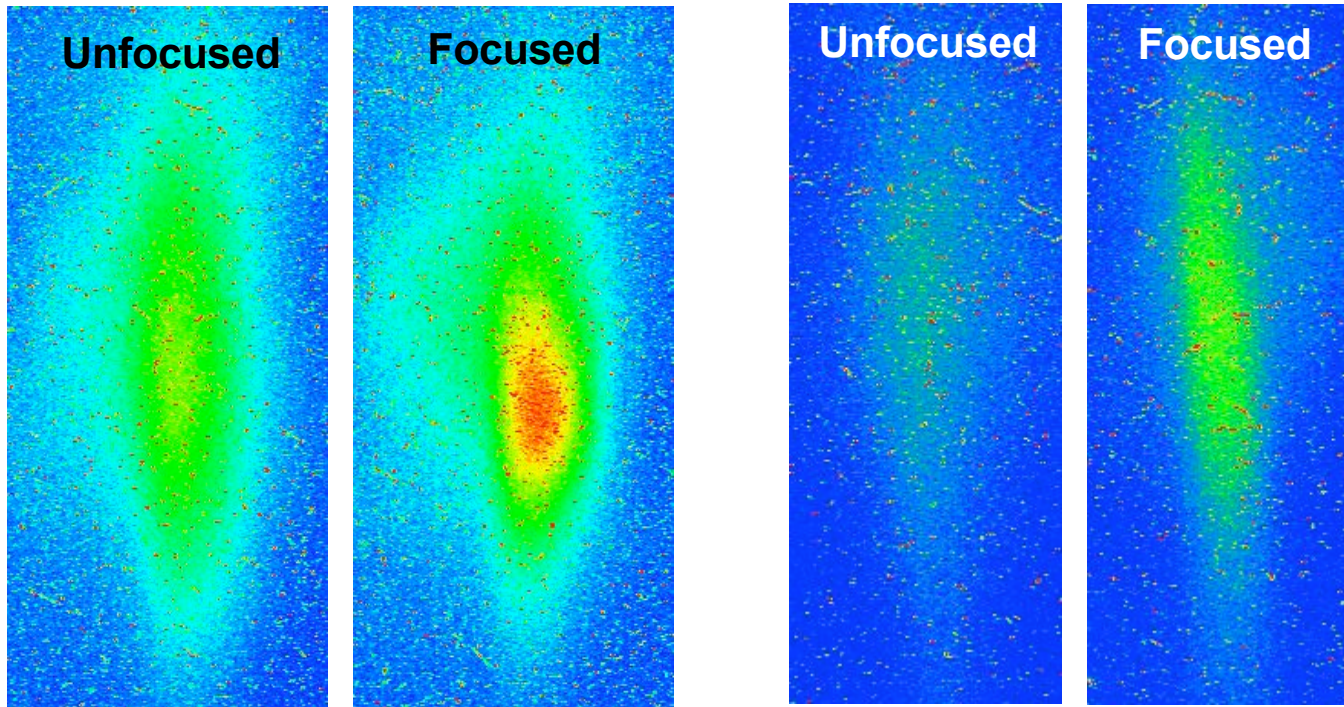
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# Plasma Focusing of High Aspect Ratio Beams

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- The International Liner Collider will use a 100:1 aspect ratio beam in order to mitigate detrimental beam/beam affects.
- We measured plasma focusing of beams with transverse aspect ratios up to about 1:5. Note that the emittance remained equal in x and y.



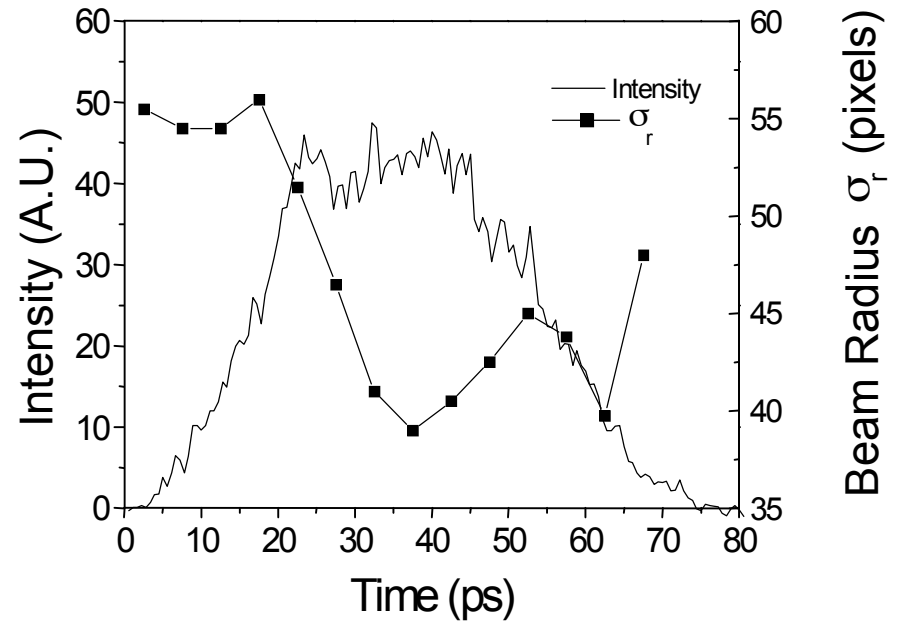
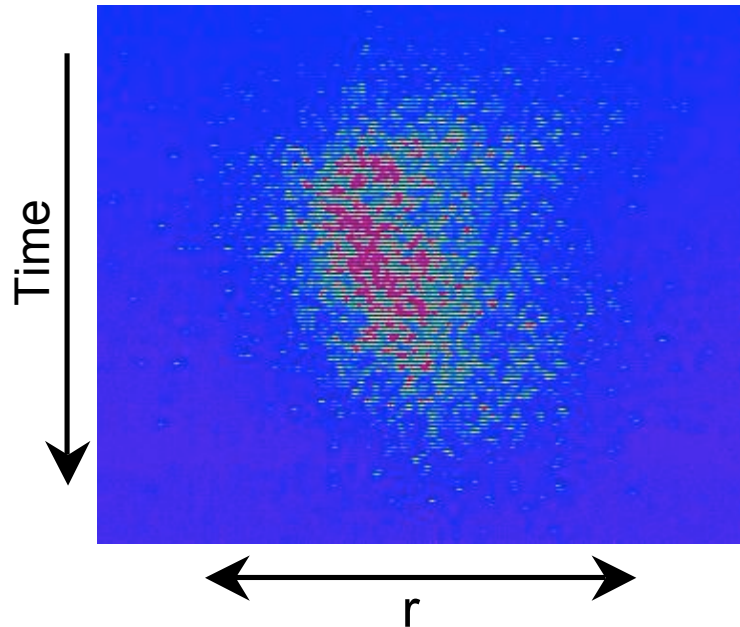
1:3.4 Beam Aspect Ratio  
Equal Number of Beam Pulses

1:4.5 Beam Aspect Ratio  
Equal Number of Beam Pulses

# Time Resolved Measurements

A series of time resolved measurements of the plasma focusing were made by imaging the beam OTR light onto the slit of a streak camera.

As expected, the intensity profile ( $\sim$ charge) of the focused beam in the time domain remains roughly gaussian while the beam is radially larger at the head than in the middle or tail.



# Conclusions

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- We have demonstrated a compact, high demagnification plasma lens for relativistic electron beam operating at the threshold of the underdense regime.
- Time integrated measurements of the plasma focusing of both round and elliptical beams were made.
- Time resolved measurements of the round beam focusing were also obtained.
- Our analysis of this data is ongoing.

## *Future Directions*

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- Recent work pointing out the problem of ion collapse in the ILC afterburner scenario also has implications for final focus plasma lens, especially those of the adiabatic variety. More work is need to explore ion collapse in this context.