

Constraints on Structure Based Optical Accelerators

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Outline

- *Optical structures – short overview*
- *Efficiency & Luminosity*
- *Non-linear phase-shift*
- *Heat dissipation*
- *Stress considerations*

Constraints & Assumptions

- ◆ **Gradient**: order of 1 [GV/m] or higher.
- ◆ **Efficiency**: limited by radiation source and acceleration scheme
 - # Lasers anticipated efficiency of wall-plug to light 10% → 30%?!
 - # Efficiency of acceleration scheme – major **difficulty**
- ◆ **Breakdown**: at optical wavelengths **dielectrics** sustain higher fields comparing to metals → **non-linear effects**
- ◆ **Manufacturing** constraints favor planar structures – consistent with luminosity constraints.
- ◆ **Single Mode**: width of vacuum tunnel $0.3\lambda - 0.8\lambda$ → **position**
- ◆ **Machining tolerance**: $1\mu\text{m}$ at 3 cm wavelength. Four orders of magnitude difference are difficult to preserve at $\lambda=1\mu\text{m}$.

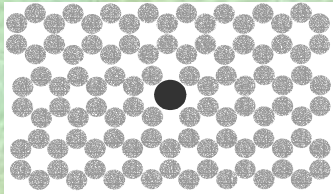
S. Banna, D. Schieber and L. Schächter; App. Phys. Lett., Vol.84(5) 723-5 (2004).

S. Banna, D. Schieber and L. Schächter; J. of Appl. Phys. 95(8) 4415-4426 (2004).

Structure parameters

$$Z_{\text{int}} \equiv (E_0 \lambda)^2 / 2P$$

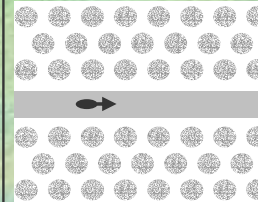
Transverse PBG



$$\underbrace{\frac{R_{\text{int}}}{\lambda} \approx 0.68}_{\varepsilon=2.1, \lambda \approx 1[\mu\text{m}]} \Rightarrow \begin{cases} Z_{\text{int}} \approx 19.5[\Omega] \\ \beta_{\text{gr}} \approx 0.58 \\ \frac{E_{\text{acc}}}{E_{\text{max}}} \approx 0.5 \end{cases}$$

E. Lin, PR STAB, 2000

Longitudinal PBG

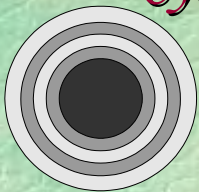


$$\underbrace{\frac{D_{\text{int}}}{\lambda} = 0.55 \div 1.25}_{\varepsilon=2.1, \lambda \approx 1.5[\mu\text{m}]} \Rightarrow \begin{cases} Z_{\text{int}} \frac{\Delta_y}{\lambda} \approx 250 \div 20[\Omega] \\ \beta_{\text{gr}} \approx 0.2 \div 0.6 \\ \frac{E_{\text{acc}}}{E_{\text{max}}} \approx 0.35 \div 0.15 \end{cases}$$

B. Cowan, PR STAB, 2003

LEAP

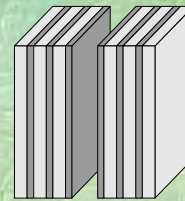
Cylindrical Bragg Structure



$$\underbrace{\frac{R_{\text{int}}}{\lambda} \approx 0.3 \div 0.8}_{\varepsilon_1=2.1, \varepsilon_2=4, \lambda=1[\mu\text{m}]} \Rightarrow \begin{cases} Z_{\text{int}} \approx 268 \div 37[\Omega] \\ \beta_{\text{gr}} \approx 0.41 \div 0.48 \\ \frac{E_{\text{acc}}}{E_{\text{max}}} \approx 0.73 \div 0.37 \end{cases}$$

A. Mizrahi & L. Schachter, Phys. Rev. E, 2004

Planar Bragg Structure



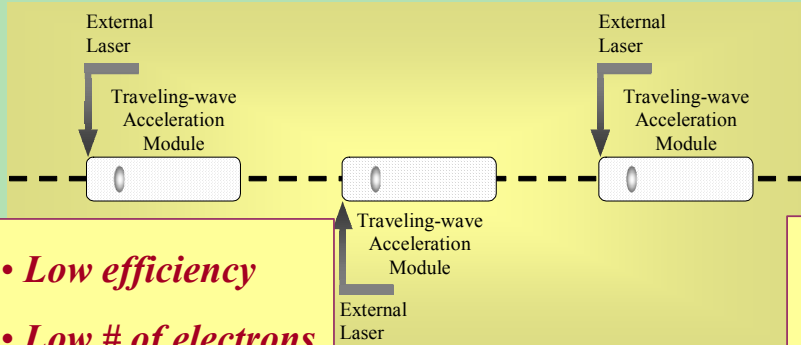
$$\underbrace{\frac{D_{\text{int}}}{\lambda} = 0.3 \div 0.8}_{\varepsilon_1=2.1, \varepsilon_2=4, \lambda=1[\mu\text{m}]} \Rightarrow \begin{cases} Z_{\text{int}} \frac{\Delta_y}{\lambda} \approx 147 \div 25.7[\Omega] \\ \beta_{\text{gr}} \approx 0.42 \div 0.53 \\ \frac{E_{\text{acc}}}{E_{\text{max}}} \approx 0.47 \div 0.20 \end{cases}$$

Outline

- *Optical structures*
- *Efficiency & Luminosity*
- *Non-linear phase-shift*
- *Heat dissipation*
- *Stress considerations*

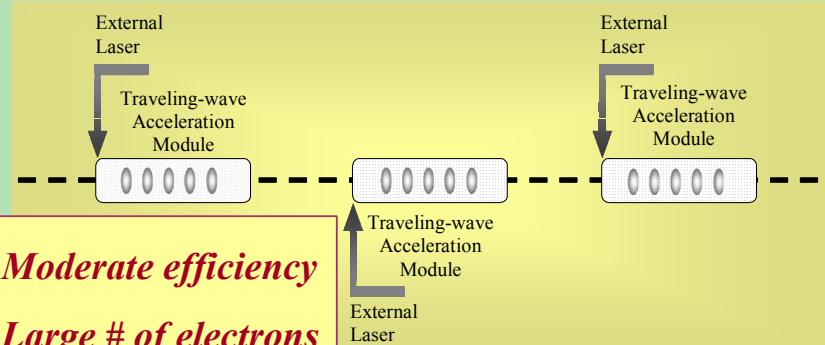
Configurations

Single bunch & no feedback



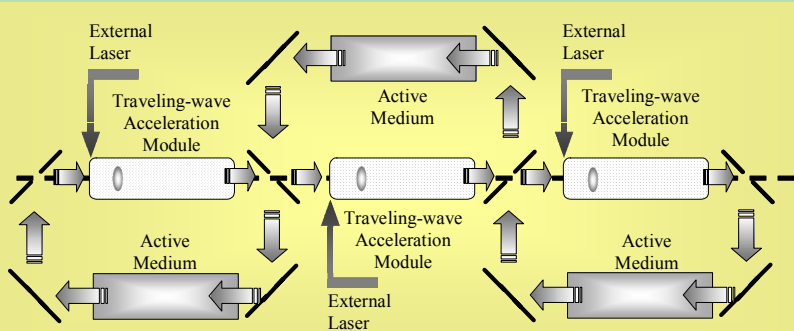
- Low efficiency
- Low # of electrons

Train of micro-bunches & no feedback



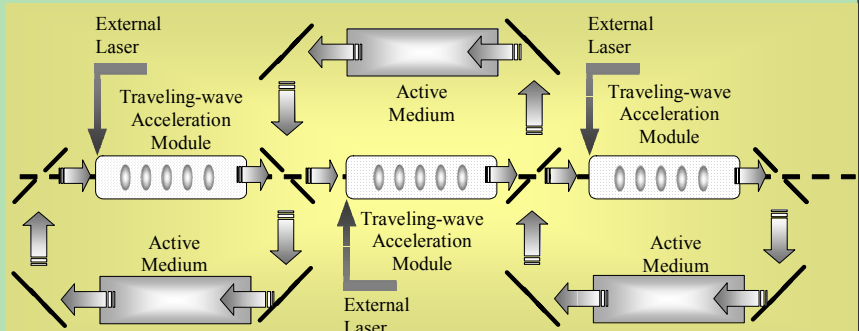
- Moderate efficiency
- Large # of electrons

Single bunch & feedback



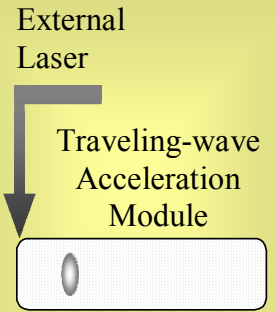
- High efficiency
- Low # of electrons

Train of micro-bunches & feedback



- High efficiency
- Large # of electrons

Single bunch & no feedback



•Wake parameter:

Decelerating field for a given charge $E_{\text{dec}} \equiv \kappa q$

$$\kappa = 2 / 4\pi\epsilon_0 R^2$$

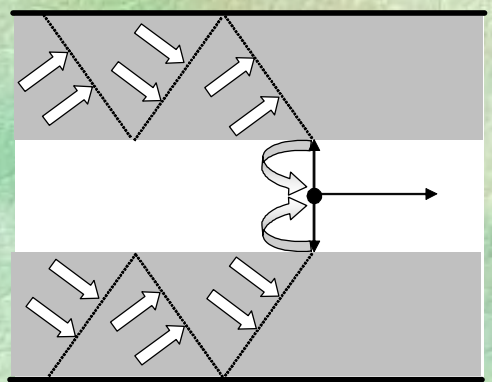
•Beam-loading parameter:

Beam-loading of the accelerating mode $E_{\text{dec}}^{(F)} \equiv \kappa_1 q$

$$\kappa_1 \equiv \kappa W_1$$

$$E_z(r=0, \tau = t - z/c) \approx q\kappa \sum_{n=1}^{\infty} W_n \cos(\omega_n \tau) 2h(\tau)$$

$$\sum_{n=1}^{\infty} W_n = 1$$

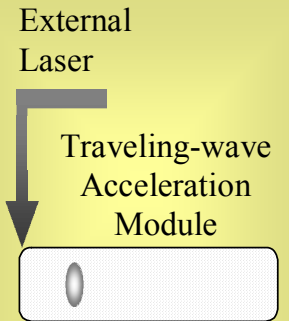


$$\kappa_1 = \frac{\beta_{\text{gr}}}{1 - \beta_{\text{gr}}} \frac{Z_{\text{int}}}{\sqrt{\mu_0 / \epsilon_0}} \frac{\pi}{4\pi\epsilon_0 \lambda^2}$$

Contribution of the fundamental to the total deceleration

Stupakov & Bane, PR STAB, 2003

Single bunch & no feedback



- Loaded gradient: $E_{\text{eff}} \equiv E_{\text{acc}} - E_{\text{dec}} = E_{\text{acc}} - \kappa q$

- Kinetic energy: $\Delta U_{\text{KIN}} \equiv q E_{\text{eff}} d$

- EM energy: $U_{\text{EM}} \equiv P_{\text{Laser}} \frac{d}{V_{\text{gr}}} (1 - V_{\text{gr}} / c)$

Zero force charge

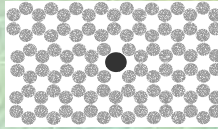
$$\eta \equiv \frac{\Delta U_{\text{KIN}}}{U_{\text{EM}}} = \eta_{\text{max}} \frac{4q(q_0 - q)}{q_0^2} \Rightarrow q_{\text{opt}} = \frac{1}{2} q_0 \equiv \frac{1}{2} \frac{E_{\text{acc}}}{\kappa}$$

$$\eta_{\text{max}} = \frac{\kappa_1}{\kappa}$$

Maximum efficiency is set by the projection of the total deceleration on the fundamental !!

Single bunch & no feedback

Transverse PBG

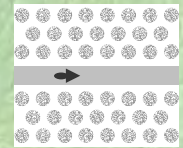


$$\left. \begin{aligned} R_{\text{int}} &\approx 0.68\lambda \\ \varepsilon &= 2.1, \lambda \approx 1.0[\mu\text{m}] \\ Z_{\text{int}} &\approx 19.5[\Omega] \\ \beta_{\text{gr}} &\approx 0.58 \\ E_{\text{max}} &\approx 2[\text{GV/m}] \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} P_{\text{Laser}} &\approx 50[\text{kW}] \\ \eta &\approx 6\% \\ q_{\text{opt}} &\approx 7 \times 10^4 e \\ E_{\text{acc}} &\approx 1[\text{GV/m}] \end{aligned} \right\}$$

E. Lin, PR STAB, 2000

Longitudinal PBG

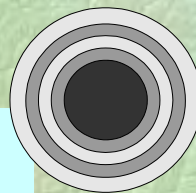


$$\left. \begin{aligned} D_{\text{int}} &\approx 0.55\lambda \\ \varepsilon &= 2.1 \\ \lambda &\approx 1.5[\mu\text{m}] \\ Z_{\text{int}}\Delta_y / \lambda &\approx 250[\Omega] \\ \beta_{\text{gr}} &\approx 0.2 \\ E_{\text{max}} &\approx 2[\text{GV/m}] \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} \bar{P}_{\text{Laser}} &\approx 2.3[\text{kW}/\mu\text{m}] \\ \eta &\approx 36\% \\ \bar{q}_{\text{opt}} &\approx 5 \times 10^4 [e/\mu\text{m}] \\ E_{\text{acc}} &\approx 0.6[\text{GV/m}] \end{aligned} \right\}$$

B. Cowan, PR STAB, 2003

Cylindrical Bragg Structure

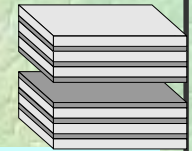


$$\left. \begin{aligned} R_{\text{int}} &\approx 0.68\lambda \\ \varepsilon_1 = 2.1, \varepsilon_2 = 4 \\ \lambda &\approx 1[\mu\text{m}] \\ Z_{\text{int}} &\approx 56.4[\Omega] \\ \beta_{\text{gr}} &\approx 0.58 \\ E_{\text{max}} &\approx 2[\text{GV/m}] \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} P_{\text{Laser}} &\approx 18[\text{kW}] \\ \eta &\approx 9\% \\ q_{\text{opt}} &\approx 7 \times 10^4 e \\ E_{\text{acc}} &\approx 1[\text{GV/m}] \end{aligned} \right\}$$

A. Mizrahi & L. Schachter, Phys. Rev. E, 2004

Planar Bragg Structure

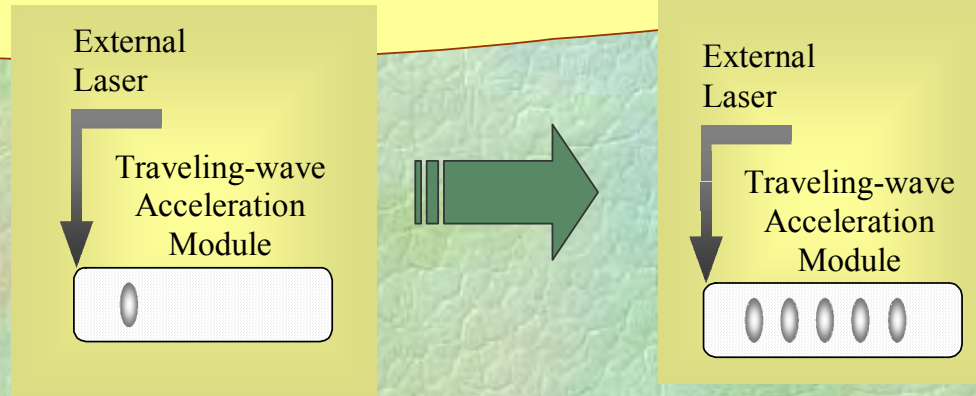


$$\left. \begin{aligned} D_{\text{int}} &\approx 0.55\lambda \\ \varepsilon_1 = 2.1, \varepsilon_2 = 4 \\ \lambda &\approx 1[\mu\text{m}] \\ Z_{\text{int}}\Delta_y / \lambda &\approx 57[\Omega] \\ \beta_{\text{gr}} &\approx 0.48 \\ E_{\text{max}} &\approx 2[\text{GV/m}] \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} P_{\text{Laser}} &\approx 5.3[\text{kW}/\mu\text{m}] \\ \eta &\approx 8\% \\ q_{\text{opt}} &\approx 3.3 \times 10^4 [e/\mu\text{m}] \\ E_{\text{acc}} &\approx 0.56[\text{GV/m}] \end{aligned} \right\}$$

Single bunch & no feedback

By *splitting the bunch* into a train of micro-bunches, the projection of the wake on the fundamental remains the same, but *higher frequencies are suppressed*



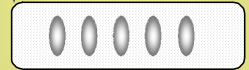
$$\eta_{\max} = \frac{\kappa_1}{\bar{\kappa}(M)} = \frac{\kappa_1}{\kappa_1 + \kappa_2(M) + \dots}$$

$$P(M) = q^2 c \kappa \underbrace{\sum_{n=1}^{\infty} W_n}_{\bar{\kappa}(M)} \left[\frac{\text{sinc}\left(\pi M \frac{\omega_n}{\omega_1}\right)}{\text{sinc}\left(\pi \frac{\omega_n}{\omega_1}\right)} \right]^2$$

Train of bunches & no feedback

External
Laser

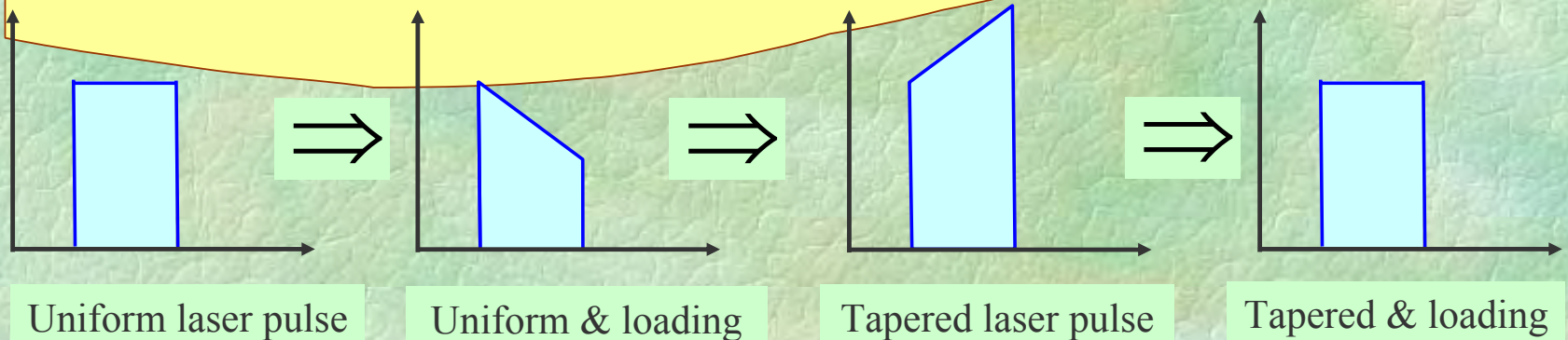
Traveling-wave
Acceleration
Module



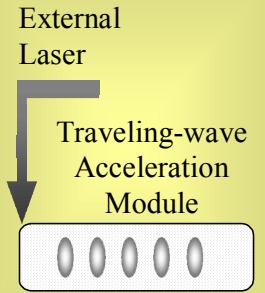
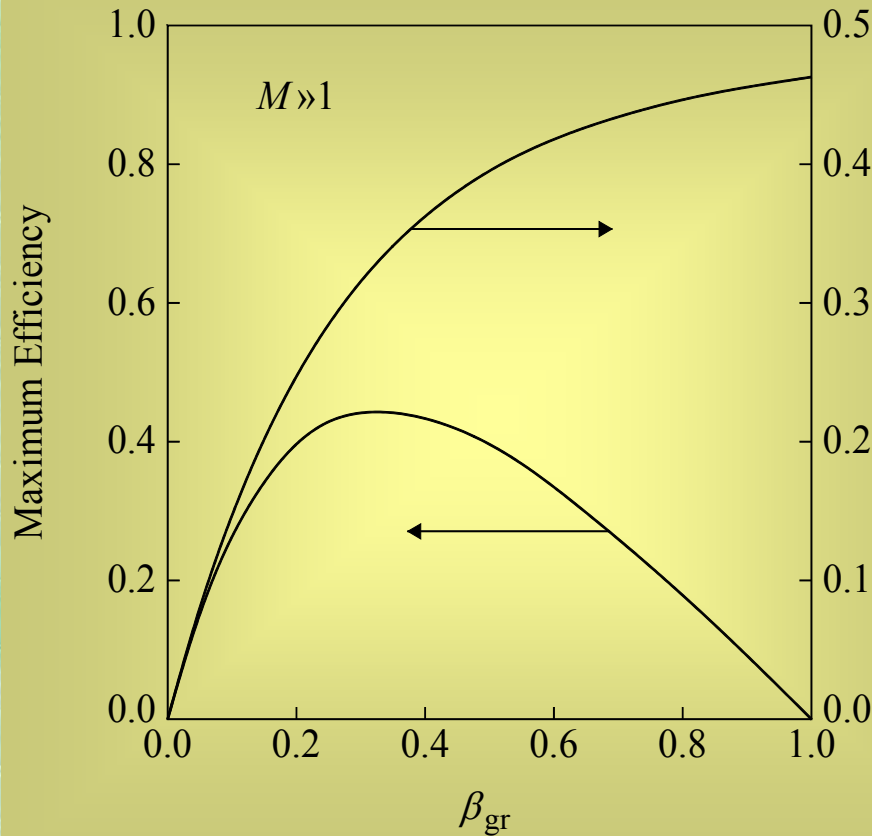
What is the efficiency in case of a train of micro-bunches?

For an answer, one needs to make two observations:

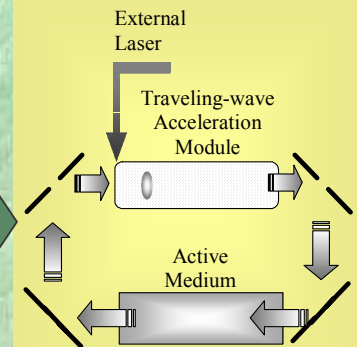
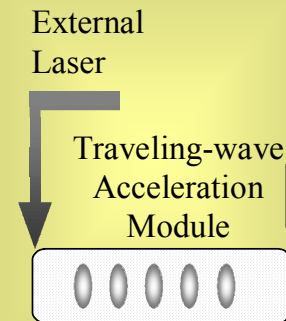
- a) The laser pulse duration ought to be **longer** in order to account for the macro-bunch length.*
- b) The envelope of the laser pulse must be **tapered**, in order to compensate for beam loading.*



Train of bunches & no feedback



In spite of splitting the macro-bunch, there still is 50% waste of the laser energy \rightarrow feedback loop.



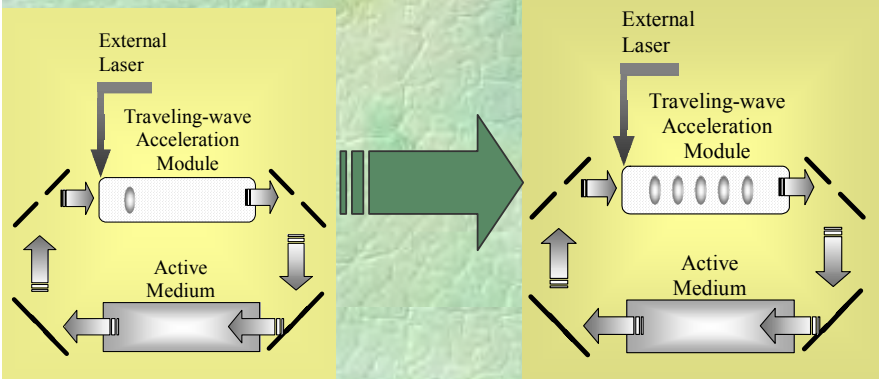
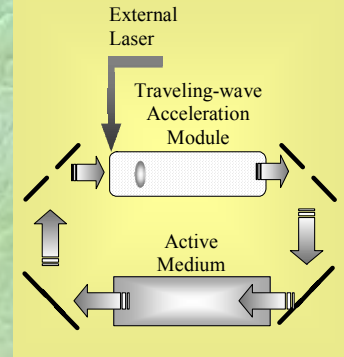
Single bunch & feedback

$$\eta = \frac{\Delta U_{KIN}}{U_{LASER} + U_{ACTIVE}} = \frac{\Delta U_{KIN}}{\Delta U_{KIN} + U_{LOSS}} = \frac{1}{1 + \frac{1}{Q} \frac{U_{OUT}}{\Delta U_{KIN}}}$$

$$q_{opt} = \frac{1}{2} q_0$$

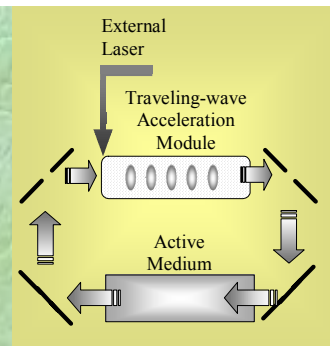
$$\eta_{max} \approx \frac{1}{1 + \frac{1}{Q} \frac{\kappa_1}{\kappa}} \approx \begin{cases} 1 & Q \gg 1 \\ \frac{\kappa_1}{\kappa} & Q \rightarrow 1 \end{cases}$$

High efficiency but,
small number of electrons \rightarrow
train of bunches and feedback loop



Ensure that **output & feedback** are
consistent with the necessary **input** !!

Train of bunches & feedback



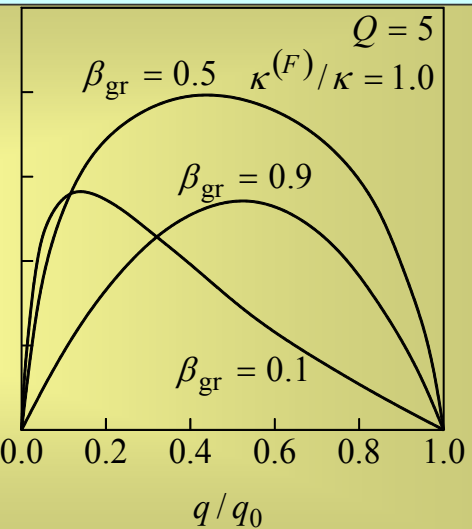
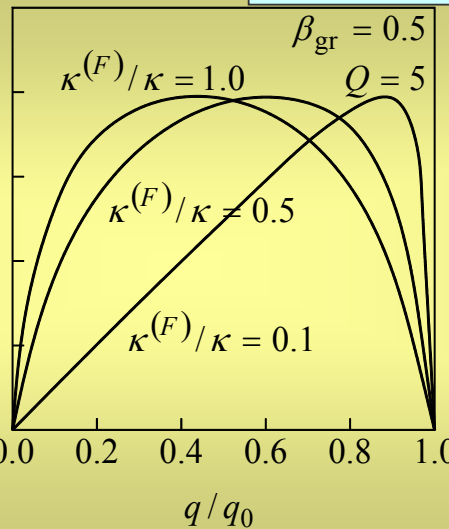
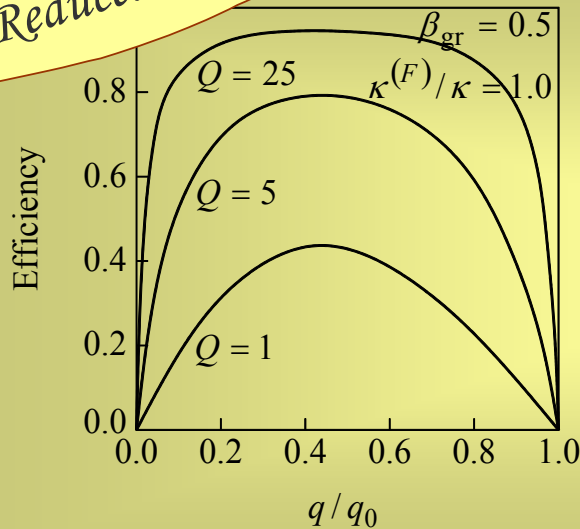
Conditions for self-consistent field:

- (I) Amplifier compensates for all **radiation loss**
- (II) External laser compensates for **beam-loading**

Active enhancement of the quality factor

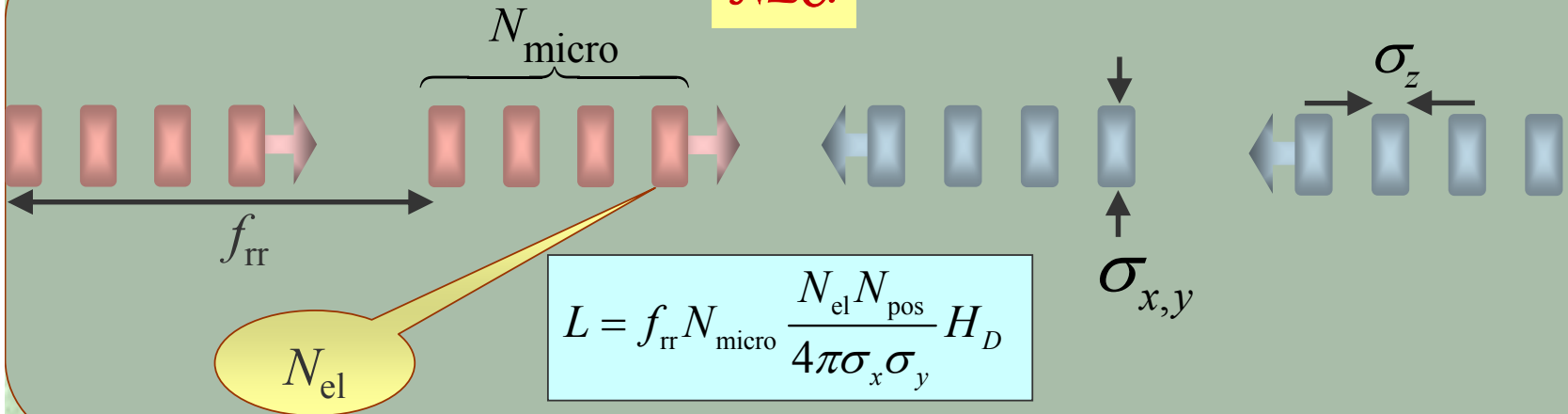
High efficiency
Reduced sensitivity

$$\eta = \frac{\Delta U_{KIN}}{U_{LASER} + U_{ACTIVE}} = \frac{1}{1 + \frac{1}{Q} \frac{U_{OUT}}{\Delta U_{KIN}}}$$



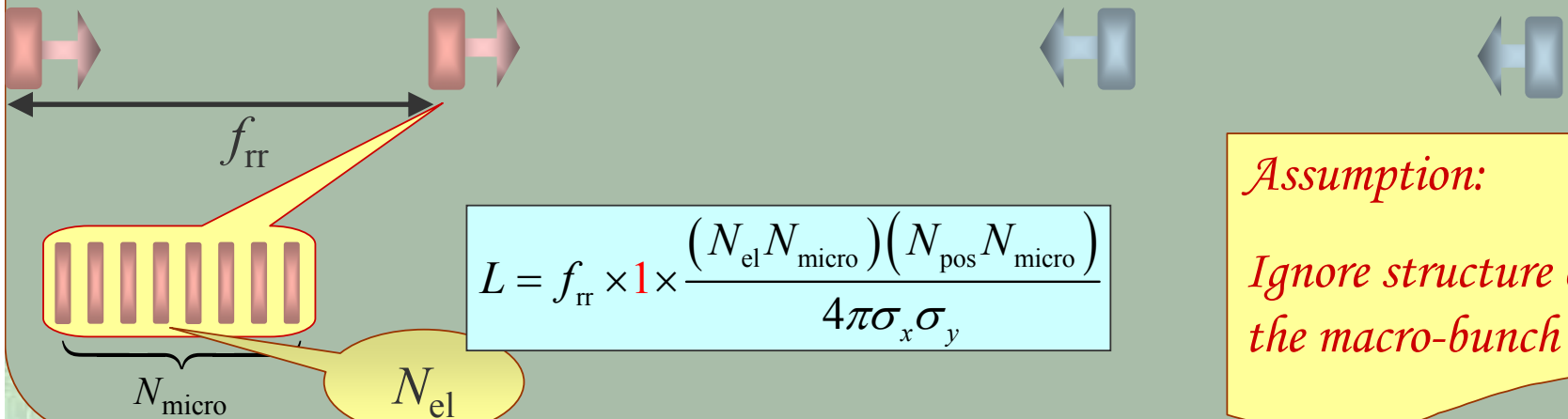
Luminosity

NLC:



$$L = f_{rr} N_{micro} \frac{N_{el} N_{pos}}{4\pi\sigma_x\sigma_y} H_D$$

Optical Acc.:



$$L = f_{rr} \times 1 \times \frac{(N_{el} N_{micro})(N_{pos} N_{micro})}{4\pi\sigma_x\sigma_y}$$

Assumption:

Ignore structure of the macro-bunch

Luminosity

	NLC	Single no FB	Single no FB	Train & FB	Train & FB
f_{rr} [Hz]	120	1(6)	1(9)	1(6)	1(6)
N_{micro}	190	1	1	1(3)	1(3)
N_{el}	0.75(10)	5(4)	5(4)	1(6)	1(6)
σ_z [nm]	0.11(6)	4	4	4	4
σ_x [nm]	245	245	24.5	245	24.5
σ_y [nm]	2.7	2.7	0.27	2.7	0.27
$n^{-1/3}$ [Å]	2.1	3.8	0.8	1.4	0.3
H_D	1.4	1.0	1.0	1.0	1.0
L [cm ⁻² sec ⁻¹]	2(34)	3(25)	3(30)	1.2(34)	1.2(36)
Beam power [MW]	13.7	4(-3)	4	80	80

Fluence

Density !

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- *Heat dissipation*
- *Stress considerations*

Polarization non-linearity

- ◆ *Breakdown & Nonlinearity*: In dielectrics at optical wavelengths breakdown threshold is *higher* than that required to excite nonlinear effects.
- ◆ *Main Nonlinear Effect*: laser affects dielectric coefficient
→ phase shift.

$$\vec{P} = \epsilon_0 \left[\chi^{(1)} \vec{E} + \chi^{(2)} \vec{E}\vec{E} + \chi^{(3)} \vec{E}\vec{E}\vec{E} + \dots \right]$$

- *Third harmonic generation*
- *Four wave mixing*
- *Nonlinear refraction*

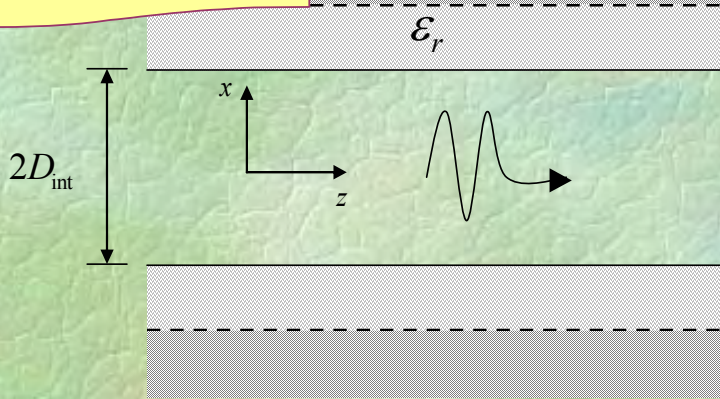
- *Second harmonic generation*
- *Sum-frequency generation*

Nonlinear Phase-shift

$$n = n_0 + n_2 I$$

$$\Delta\phi_{NL} = 2\pi n_2 I \frac{L}{\lambda}$$

Planar Structure

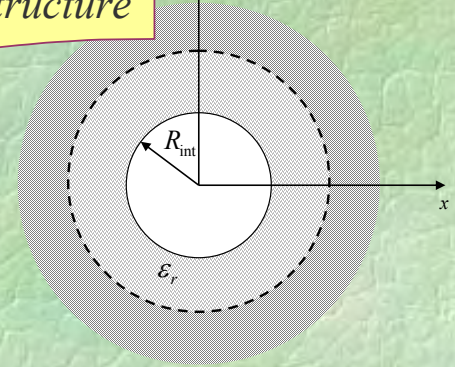


$$E_z = E_0 \exp\left(-j\frac{\omega}{c}z\right), \quad E_x = \left(j\frac{\omega}{c}x\right)E_0 \exp\left(-j\frac{\omega}{c}z\right)$$

$$E_{\max}^{\text{incident}} = E_{\text{acc}} \frac{2\pi D_{\text{int}}}{\lambda}$$

$$\Delta\phi_{NL}^{\max} = \frac{\pi L}{\eta_0 \lambda} n_0 n_2 E_{\text{acc}}^2 \left(\frac{2\pi D_{\text{int}}}{\lambda}\right)^2$$

Cylindrical Structure



$$E_z = E_0 \exp\left(-j\frac{\omega}{c}z\right), \quad E_r = j\frac{\omega r}{c} E_0 \exp\left(-j\frac{\omega}{c}z\right)$$

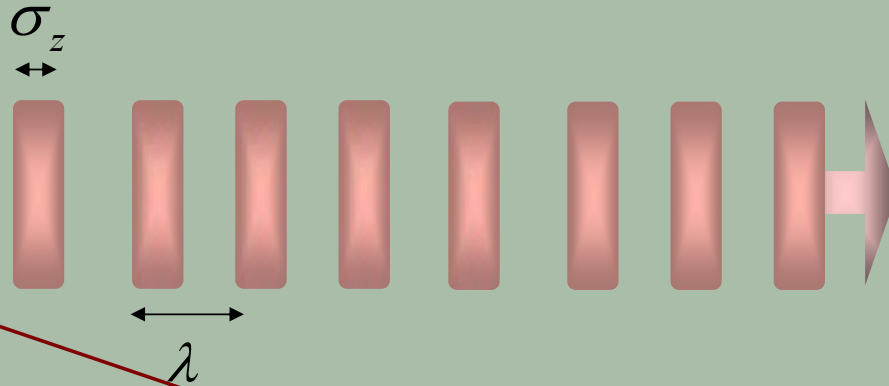
$$E_{\max}^{\text{incident}} = E_{\text{acc}} \frac{1}{2} \frac{2\pi R_{\text{int}}}{\lambda}$$

$$\Delta\phi_{NL}^{\max} = \frac{\pi L}{\eta_0 \lambda} n_0 n_2 E_{\text{acc}}^2 \left(\frac{1}{2} \frac{2\pi R_{\text{int}}}{\lambda}\right)^2$$

Non-linear Phase-shift criterion

$$\sigma_z = \frac{\alpha}{2\pi} \lambda$$

$$0 < \alpha < \frac{2\pi}{12}$$



Efficient acceleration

Synchronization

Condition

Phase-shift less than 10%

$$\Delta\phi_{NL} < \frac{2\pi}{120}$$

Non-linear Phase-shift

Ti:Sapphire laser

Fused Silica

$$n_0 = 1.45$$

$$n_2 = 2.55 \times 10^{-20} \frac{\text{m}^2}{\text{W}}$$

$$R_{\text{int}} = \lambda = 800\text{nm}; L = 1\text{mm}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 0.72 @ E_{\text{acc}} = 0.1 \frac{\text{GV}}{\text{m}}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 72.60 @ E_{\text{acc}} = 1.0 \frac{\text{GV}}{\text{m}}$$

$$R_{\text{int}} = 0.5\lambda = 400\text{nm}; L = 1\text{mm}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 0.18 @ E_{\text{acc}} = 0.1 \frac{\text{GV}}{\text{m}}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 18.15 @ E_{\text{acc}} = 1.0 \frac{\text{GV}}{\text{m}}$$

Zirconia

$$n_0 = 2$$

$$n_2 = 5.23 \times 10^{-20} \frac{\text{m}^2}{\text{W}}$$

$$R_{\text{int}} = \lambda = 800\text{nm}; L = 1\text{mm}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 2.05 @ E_0 = 0.1 \frac{\text{GV}}{\text{m}}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 85.32 @ E_0 = 1.0 \frac{\text{GV}}{\text{m}}$$

$$R_{\text{int}} = 0.5\lambda = 400\text{nm}; L = 1\text{mm}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 0.51 @ E_0 = 0.1 \frac{\text{GV}}{\text{m}}$$

$$\Delta\phi_{\text{NL}}^{\text{max}} = \frac{2\pi}{120} \times 51.34 @ E_0 = 1.0 \frac{\text{GV}}{\text{m}}$$

Solution: Redesigning the structure to (initially) have a phase velocity larger than c .

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Heat flow – single pulse operation

$$\Delta T(r = D_{\text{ext}}) = \frac{1}{h} \left[\frac{\partial}{\partial x} \Delta T \right]_{x=D_{\text{ext}}}$$

$$\left[\frac{\partial}{\partial t} - \frac{1}{D} \nabla^2 \right] \Delta T = \frac{1}{D \sigma_T} p_{\text{loss}}(r, z, t)$$

Diffusion
Coefficient

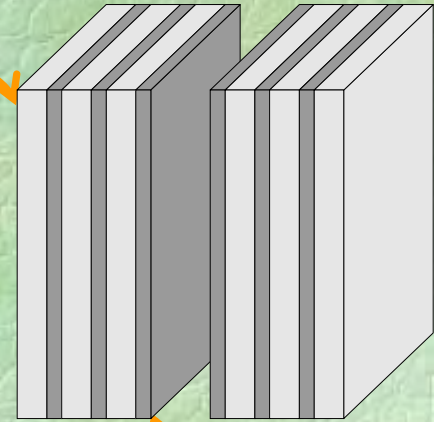
$D[\text{sec}/\text{m}^2]$

Heat
Conductivity

$\sigma_T [\text{J}/\text{sec m}^\circ\text{K}]$

Dissipated EM
Power Density

$$p_{\text{loss}}(r, z, t) \simeq \varepsilon \tan \delta \frac{\omega_0}{c} \langle S_z(r, z, t) \rangle$$



$$\left[\frac{\partial}{\partial x} \Delta T \right]_{x=D_{\text{int}}} = 0$$

Heat Flow – Train of Pulses

$$T_{rr} > 10[\text{nsec}]$$

$$T_p \sim 1[\text{psec}]$$

$$\Delta T(x, z; t) = \frac{P_0}{\sigma_T} \frac{T_p}{T_{rr}} \sum_{v=-\infty}^{\infty} \text{sinc} \left(\pi v \frac{T_p}{T_{rr}} \right) \exp \left(j 2 \pi v \frac{t - z/V_{gr}}{T_{rr}} \right)$$

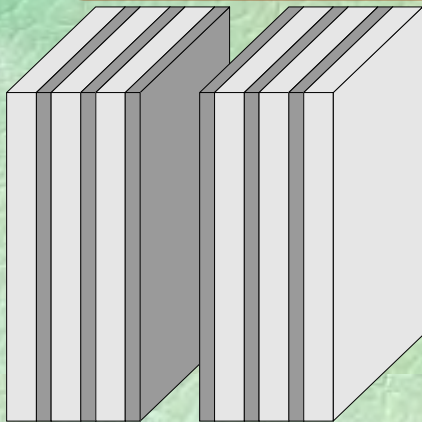
$$\times \sum_{m=0}^{\infty} \cos \left[\frac{\pi(m+1/2)}{D_{\text{ext}} - D_{\text{int}}} (x - D_{\text{int}}) \right]$$

Power profile

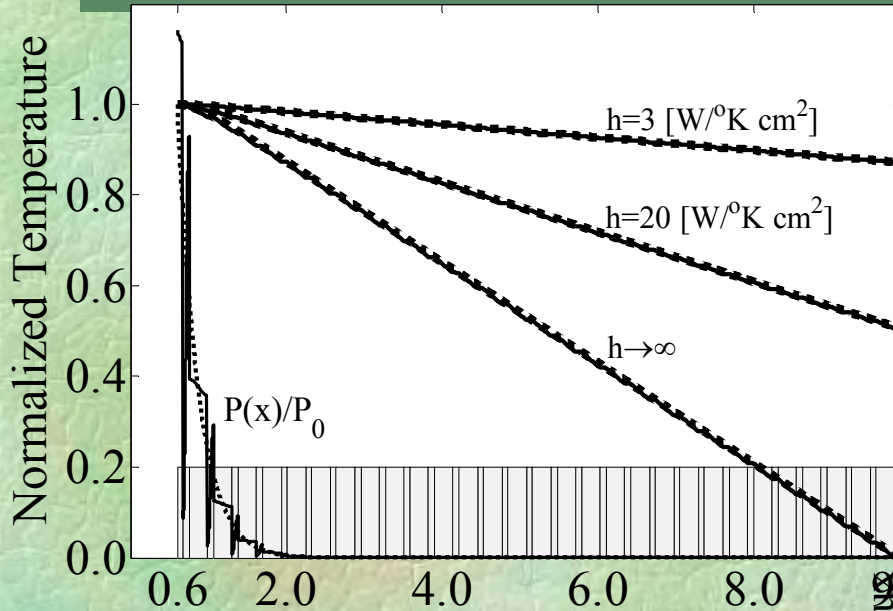
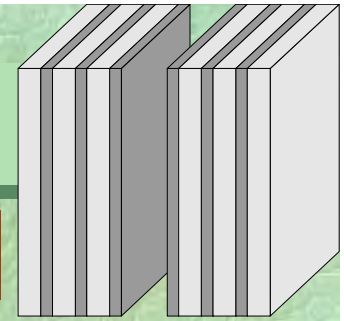
For the parameters of interest,
the deviation from average

ΔT is negligible !!

$$\times \frac{2}{D_{\text{ext}} - D_{\text{int}}} \frac{\int_{D_{\text{int}}}^{D_{\text{ext}}} dx' X_0(x') \cos \left[\frac{\pi(m+1/2)}{D_{\text{ext}} - D_{\text{int}}} (x' - D_{\text{int}}) \right]}{\left[j \frac{2\pi v}{T_{rr}} D + \left(\frac{2\pi v}{T_{rr}} \frac{1}{V_{gr}} \right)^2 + \frac{\pi^2 (m+1/2)^2}{(D_{\text{ext}} - D_{\text{int}})^2} \right]}$$



Heat Flow – Average Quantities



Silica - Silicon

$$\Delta T_{AV} \sim \left[\frac{P_0}{\sigma_T} \frac{x_c}{2} (D_{\text{ext}} - D_{\text{int}}) \right] \frac{T_p}{T_{rr}}$$

$$Q_{AV} \sim \left(P_0 \frac{x_c}{2} \right) \frac{T_p}{T_{rr}}$$

$$T_{\text{max}}(h=3) = 66.4 \times 10^7 \tan \delta_1$$

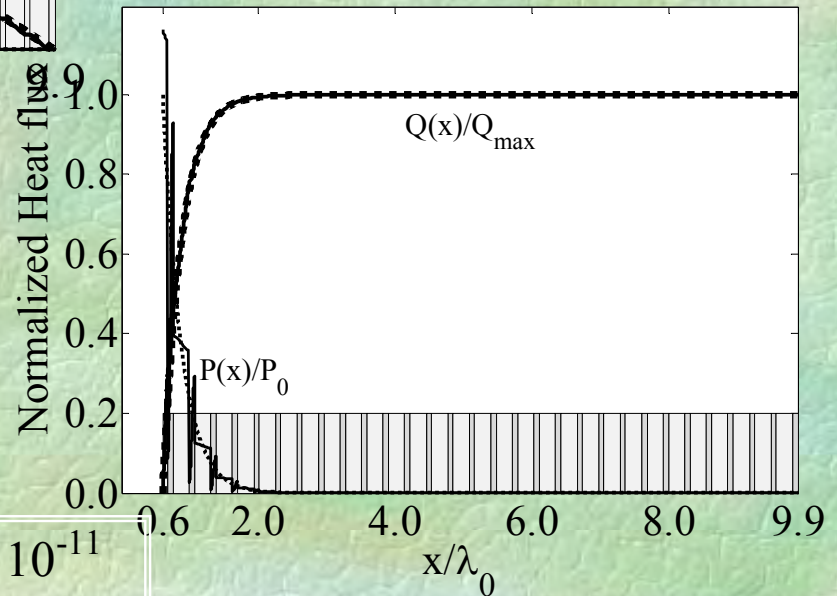
$$T_{\text{max}}(h=20) = 17.2 \times 10^7 \tan \delta_1$$

$$T_{\text{max}}(h \rightarrow \infty) = 8.49 \times 10^7 \tan \delta_1$$

$$Q_{\text{max}} = 1.74 \times 10^9 \tan \delta_1 \text{ [W/cm}^2\text{]}$$

Limit: 1500 [W/cm²]

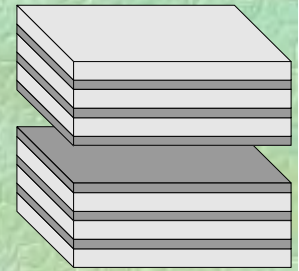
Optical Fibers: $\tan \delta (\alpha = 1 \text{ [dB/km]}) = 5 \times 10^{-11}$



Outline

- *Optical structures*
- *Efficiency & Luminosity*
- *Non-linear phase-shift*
- *Heat dissipation*
- *Stress considerations*

EM Stress on a Planar Accelerator



Total repelling Laser Pressure – Time-averaged Maxwell stress-tensor component



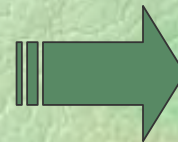
$$\begin{aligned}\langle T_{xx} \rangle &= \frac{1}{4} \epsilon_0 |E_x|^2 - \frac{1}{4} \epsilon_0 |E_z|^2 - \frac{1}{4} \mu_0 |H_y|^2 \\ &= -\frac{1}{4} \epsilon_0 |E_0|^2\end{aligned}$$

Time-averaged Lorentz force density inside the v 'th layer is due to the polarization current



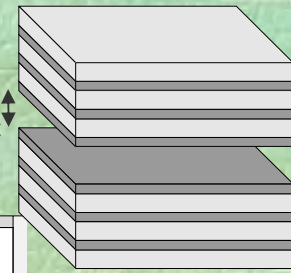
$$\begin{aligned}E_0 = 1 \left[\frac{\text{GV}}{\text{m}} \right] &\Rightarrow \langle T_{xx} \rangle \cong 2.1 \left[\frac{\mu\text{N}}{\mu\text{m}^2} \right] \\ &\cong 2 [\text{MP}] \\ &\ll 1 [\text{GP}]\end{aligned}$$

Total time-averaged boundary stress between the v 'th and the $v+1$ 'th layer is due to polarization surface charge

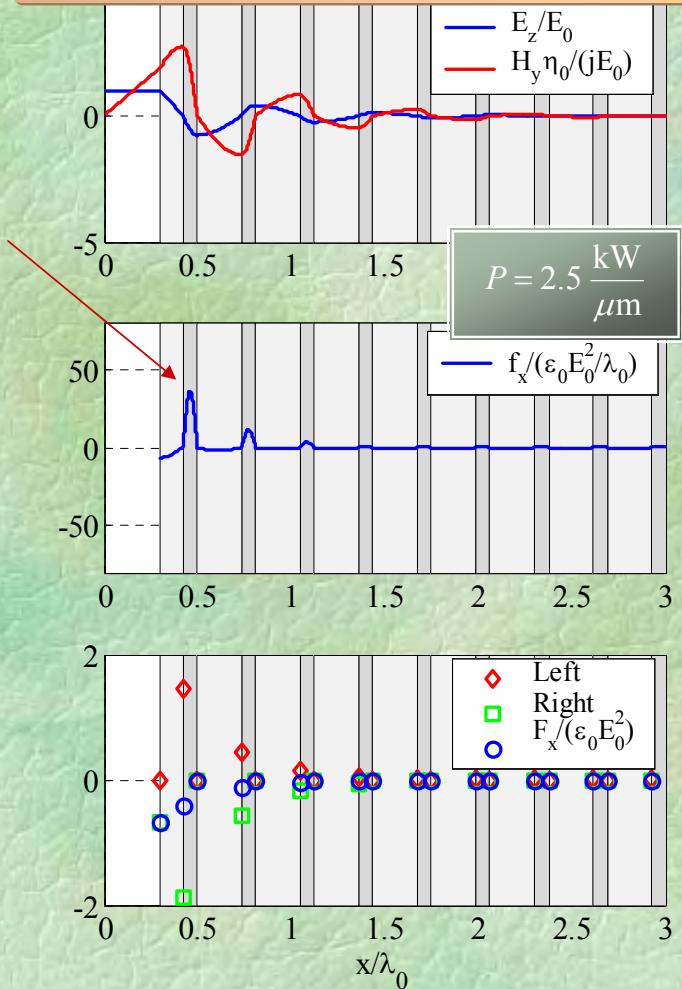


$$F_x = \frac{1}{4} \epsilon_0 |E_{x,v}|^2 \left[\frac{\epsilon_v^2}{\epsilon_{v+1}^2} - 1 \right]$$

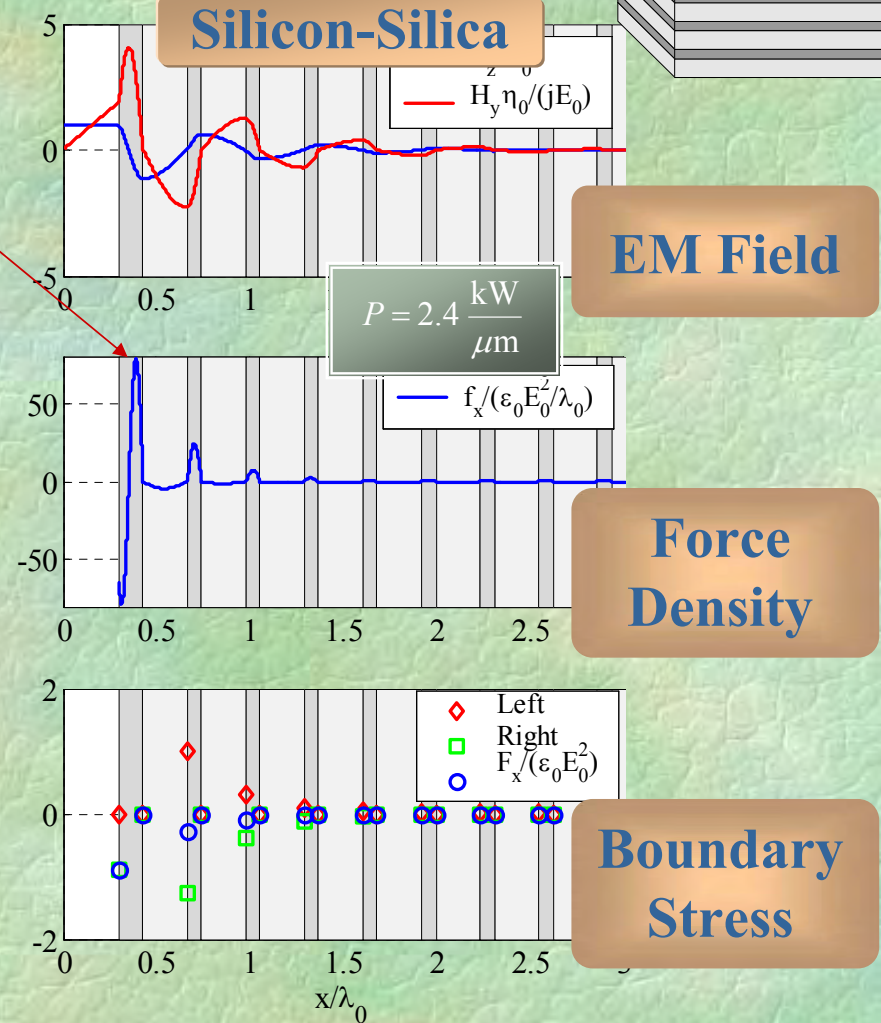
EM Stress – $D_{\text{int}} = 0.3\lambda_0$



Silica($\epsilon=2.1$)-Silicon($\epsilon=11.9$)



Silicon-Silica



EM Field

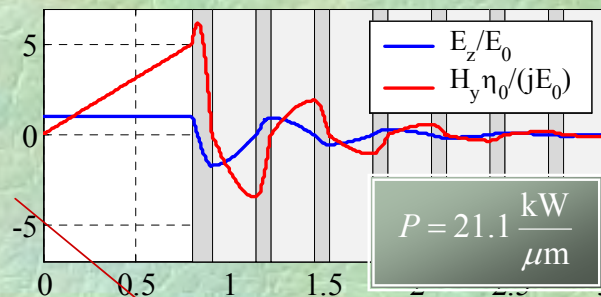
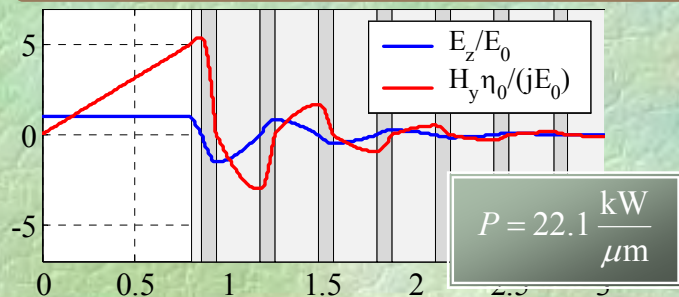
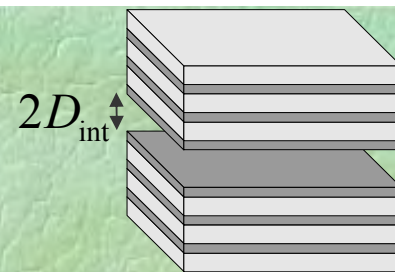
Force Density

Boundary Stress

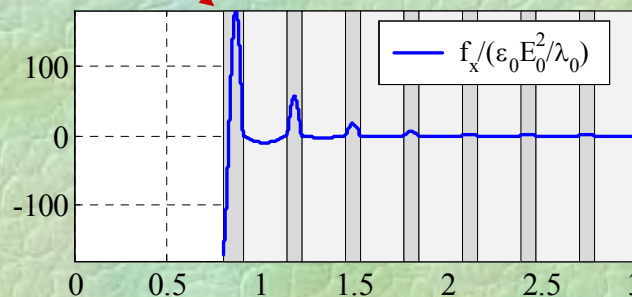
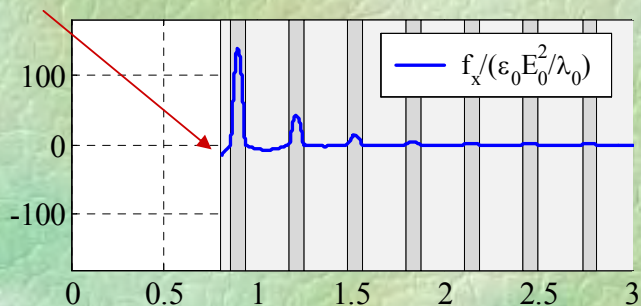
EM Stress – $D_{\text{int}} = 0.8\lambda_0$

Silica($\epsilon=2.1$)-Silicon($\epsilon=11.9$)

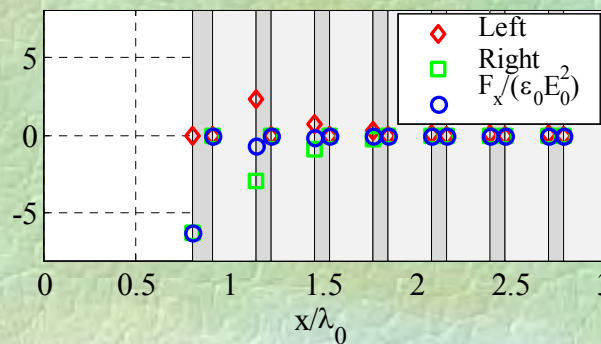
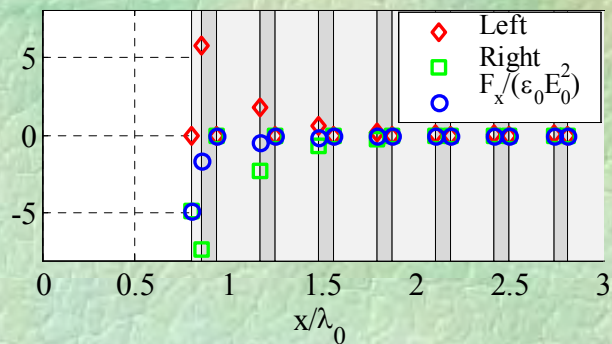
Silicon-Silica



EM Field



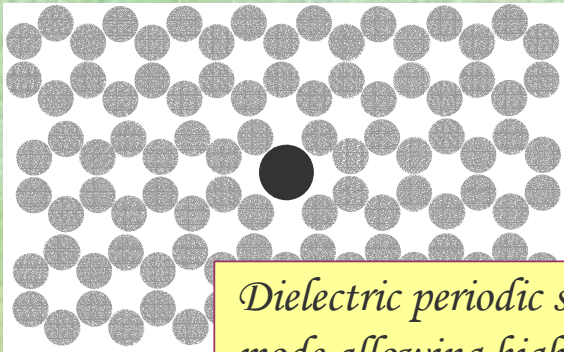
Force Density



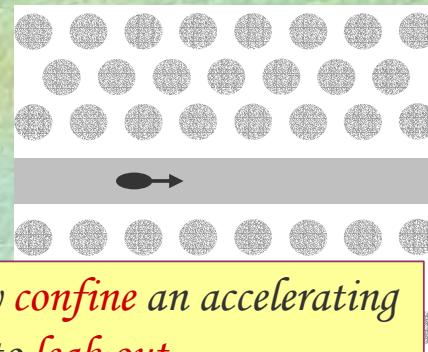
Boundary Stress

Summary: Dielectric Structures

Transverse PBG

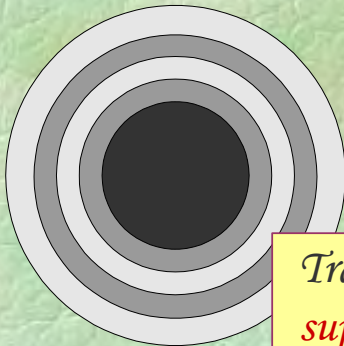


Longitudinal PBG

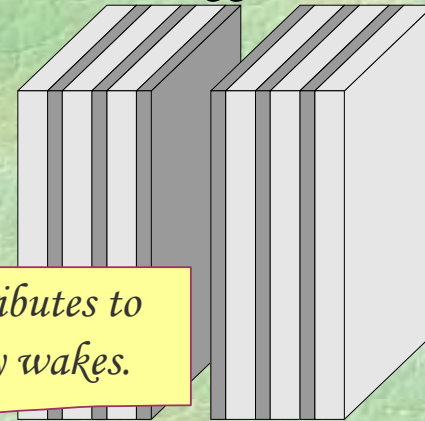


Dielectric periodic structures may *confine* an accelerating mode allowing high order modes to *leak out*.

Cylindrical Bragg Structure



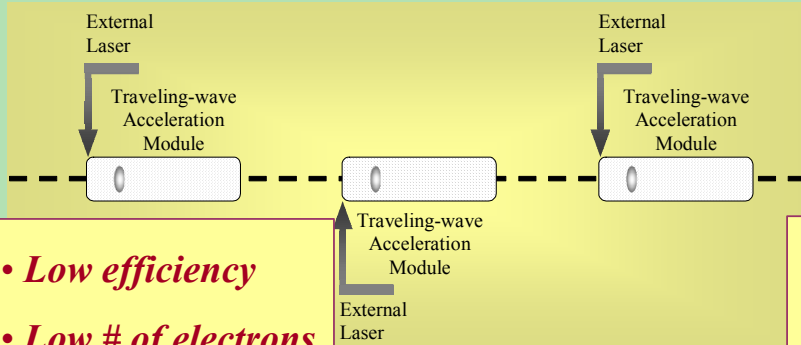
Planar Bragg Structure



Train of micro-bunches contributes to *suppression* of high frequency wakes.

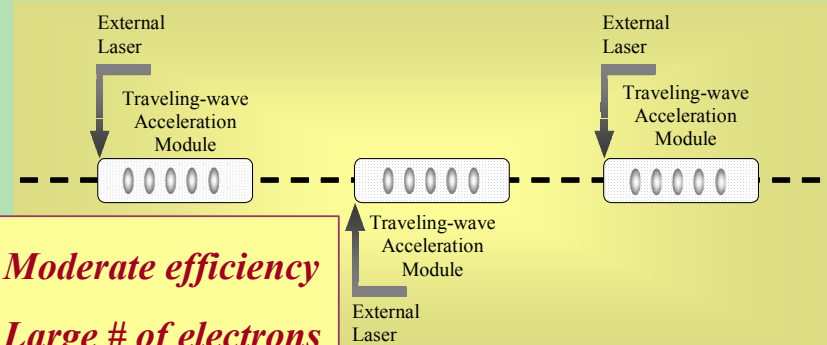
Summary: Configurations

Single bunch & no feedback



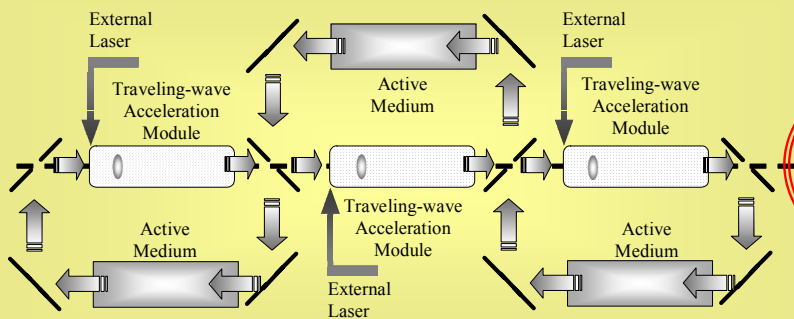
- Low efficiency
- Low # of electrons

Train of micro-bunches & no feedback



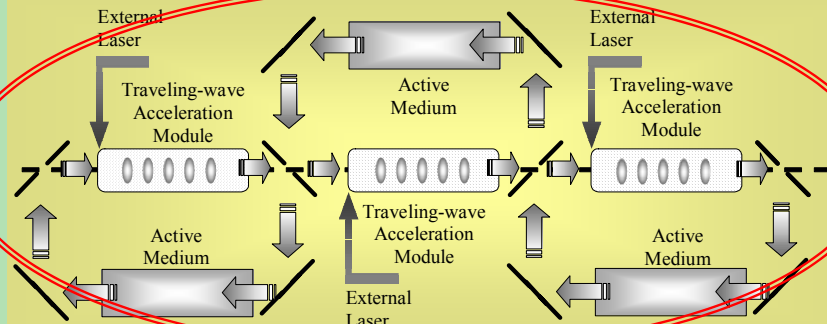
- Moderate efficiency
- Large # of electrons

Single bunch & feedback



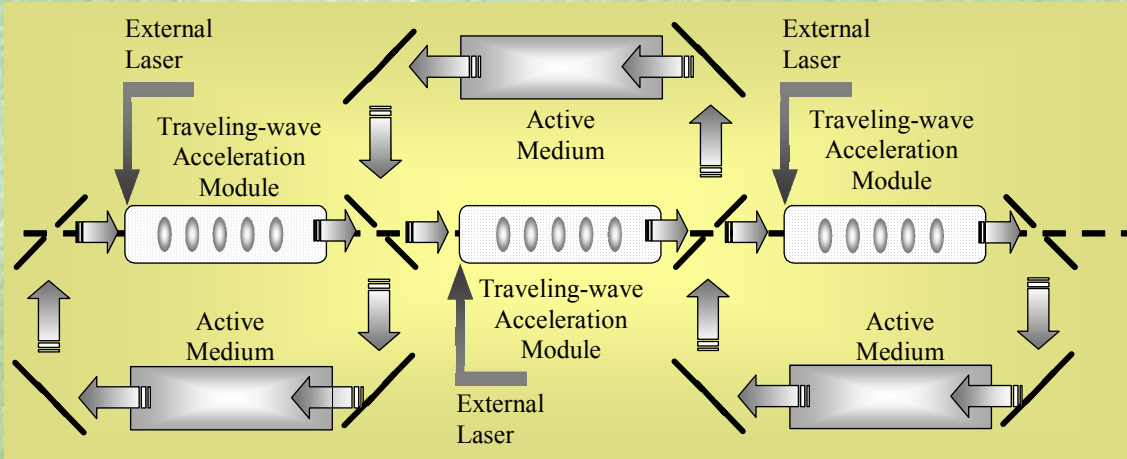
- High efficiency
- Low # of electrons

Train of micro-bunches & feedback



- High efficiency
- Large # of electrons

Summary: Efficiency & Luminosity



- (I) Amplifier compensates for all **radiation loss** (active enhancement of the Q -factor) facilitated by the wake being “quasi-coherent”
- (II) External laser compensates for **beam-loading** (tapered pulse)
- (III) Luminosity

Summary

- (I) *With commonly used materials **Kerr effect** may become a problem. By accounting for the local increase in the dielectric coefficient, it is possible to compensate for the phase velocity reduction.*
- (II) *Preliminary estimates indicate that **heat dissipation** needs close attention because the high repetition rate dictated by the luminosity constraint. Employing optical fiber technology may eliminate the problem although the latter works well in homogeneous medium, implications on multi-layered structure are unclear as yet.*
- (III) *The typical **stress** is evaluated to be of the order of 1[MPascal] which is three orders of magnitude below typical critical values at μm scale.*