

***CHANNELING projects at LNF:
From Crystal Undulators to Capillary Waveguides***

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Channeling: Orientational Effects of Transmission & Radiation

• 1962-63:

Robinson &

Oen:

Piercy &

Lutz:

• 1965:

Lindhard:

.....

Andersen

Uggerhoj

Kagan

Kononez

Firsov

Tsyganov

Gibson

Kumakhov

Beloshitsky

Gemmel

Appleton

.....

Prediction of anomalous penetration

Experimental discovery

Theoretical description

Classical theory

Quantum theory

Prediction of channeling radiation (ChR)

Experimental confirmation: positron channeling in diamond crystal

USSR-USA collaboration, SLAC 1978

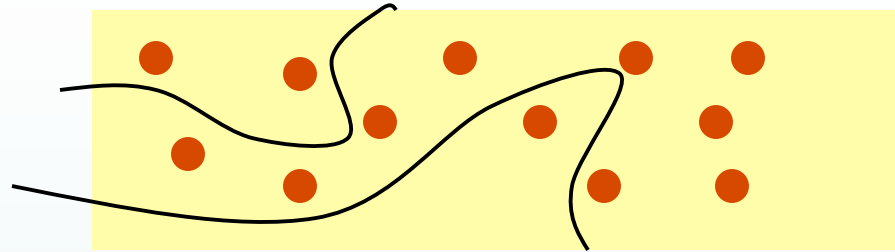
JETP Lett. 1979 (Miroshnichenko, Avakyan, Figut, et al.)

Rev. Mod. Phys. 1974: 1 MeV e⁻ @ Cu crystal

more than 1000 articles + a number of monographs

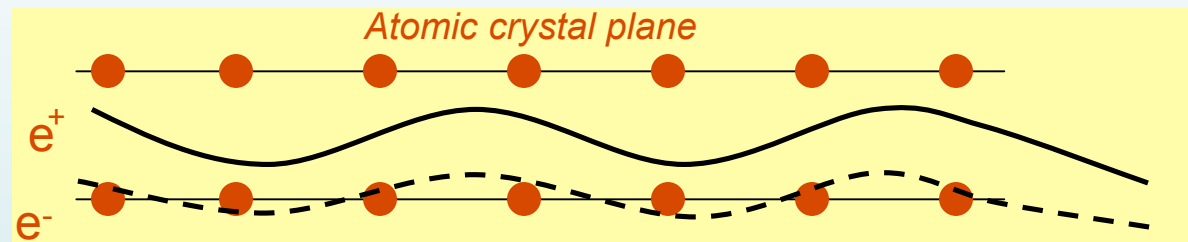
Channeling of Charged Particles

@ Amorphous:

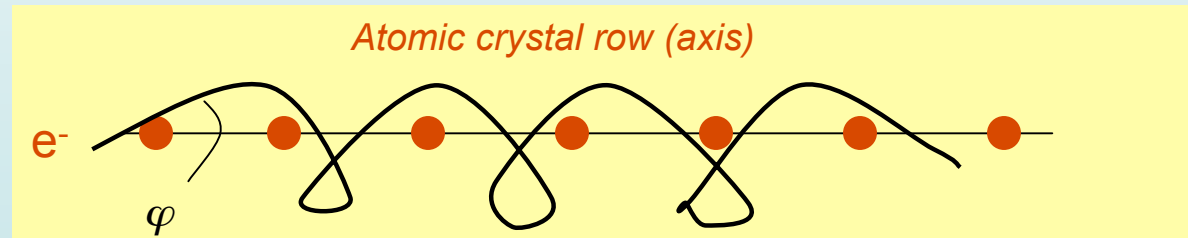


@ Channeling:

planar channeling



axial channeling



$\varphi \ll 1$ ($\varphi < \varphi_L \sim \sqrt{U/E}$) - the Lindhard angle is the critical angle for channeling

Channeling: Continuum model

$$V(r) = \frac{Z_1 Z_2 e^2}{r} \varphi(r/a)$$

screening function of Thomas-Fermi type

$$a = .8853 a_0 (Z_1^{1/2} + Z_2^{1/2})^{2/3}$$

screening length



$$\varphi(r/a): \sum_{i=1}^3 \alpha_i \exp(-\beta_i r/a) \quad \text{Molier's potential}$$

$$1 - \left[1 + \frac{Ca}{r^2} \right]^{-1/2} \quad C^2 \approx 3 \quad \text{Lindhard potential}$$

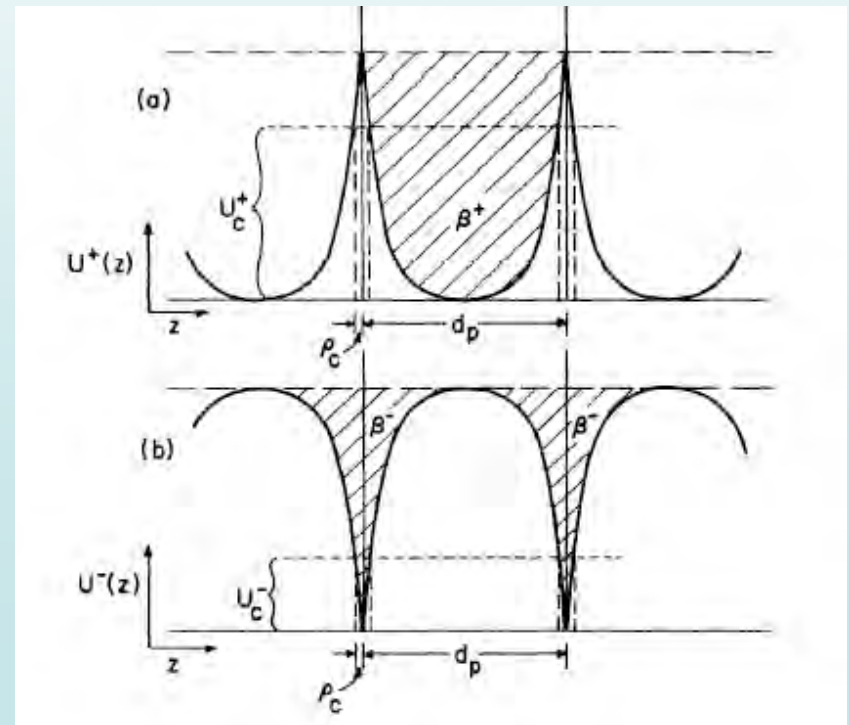
..... Firsov, Doyle-Turner, etc.

Lindhard:

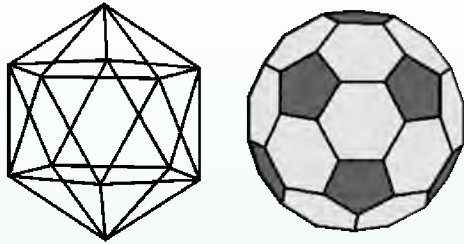
Continuum model –

continuum atomic plane/axis potential

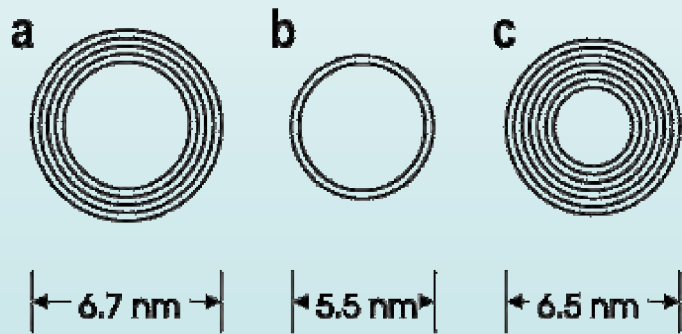
$$V_{RS}(\rho) = \frac{1}{d} \int_{-\infty}^{+\infty} V(\sqrt{\rho^2 + x^2}) dx$$



Nanotubes: continuum potential example

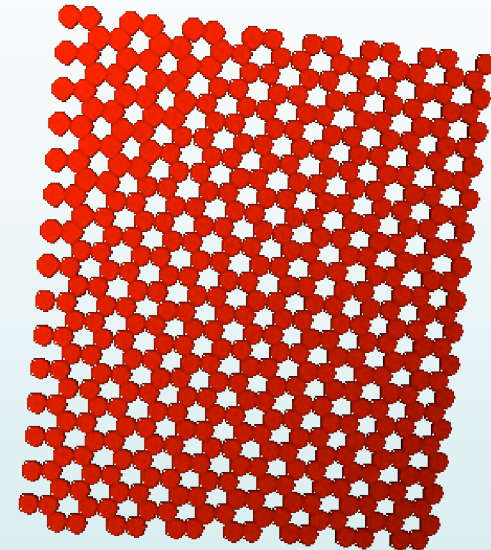


Base: fullerene molecule C_{60}
sphere of $d \sim 0.7 \text{ nm}$



*Roled graphite sheets:
nested nanotubes*

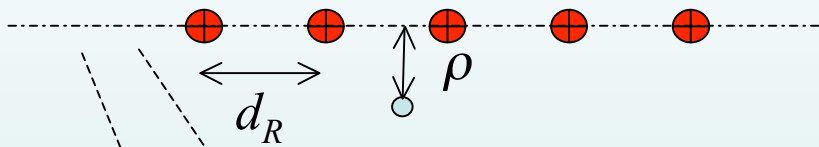
Nanosheet CC



Potentials: Doyle-Turner approximation

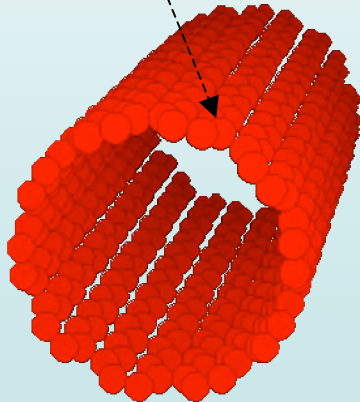


$$f(\mathbf{k}) = 4\pi Ze \sum_{j=1}^N a_j \exp(-k^2/4b_j^2) - \text{form-factor for the separate fullerene}$$



$$V_R(\rho) = (4Ze^2/d_R) \sum_{j=1}^N a_j b_j^2 \exp(-b_j^2 \rho^2)$$

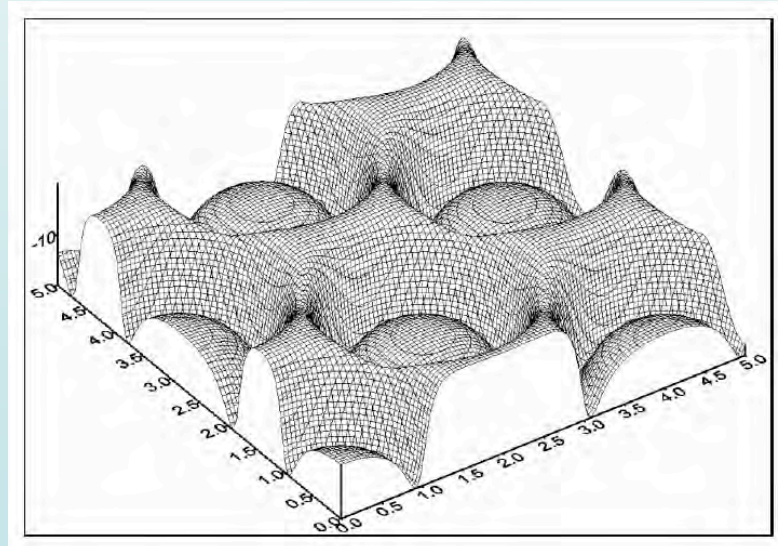
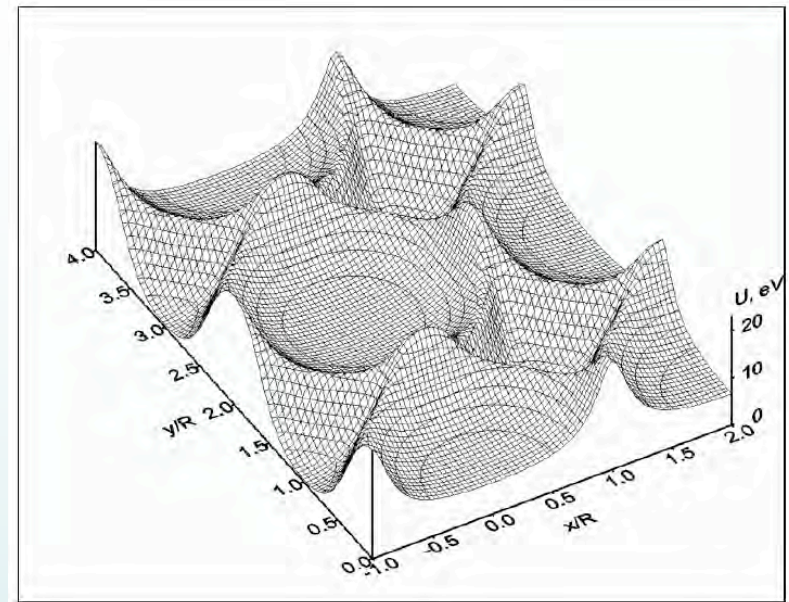
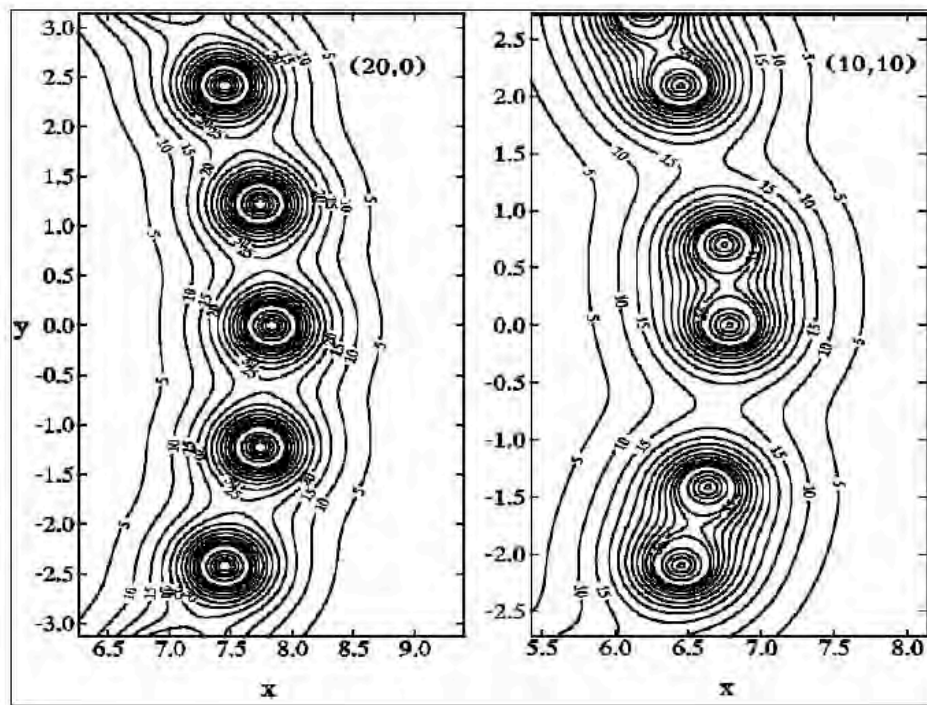
$$U(\mathbf{r}) = \sum_i V_R(|\mathbf{r} - \mathbf{r}_i|) \quad \text{continuum potential as sum of row potentials}$$



$$U(r) = (16\pi dZe^2/3\sqrt{3}l^2) \sum_{j=1}^N a_j b_j^2 \exp\{-b_j^2[r^2 + (d/2)^2]\} I_0(b_j^2 rd)$$

r – distance from the tube
 $I_0(x)$ – mod. Bessel function

Potentials: Doyle-Turner approximation

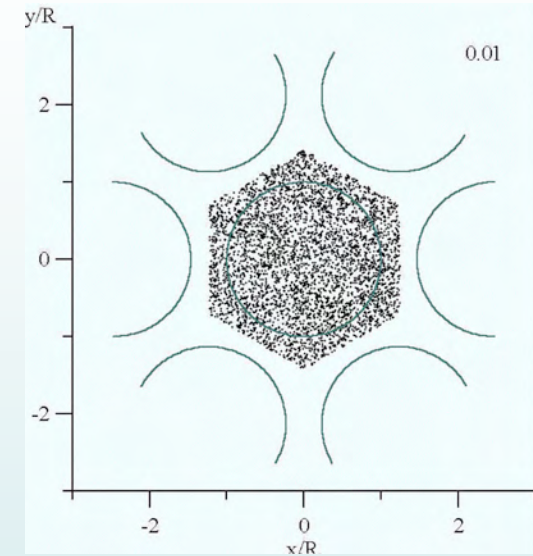
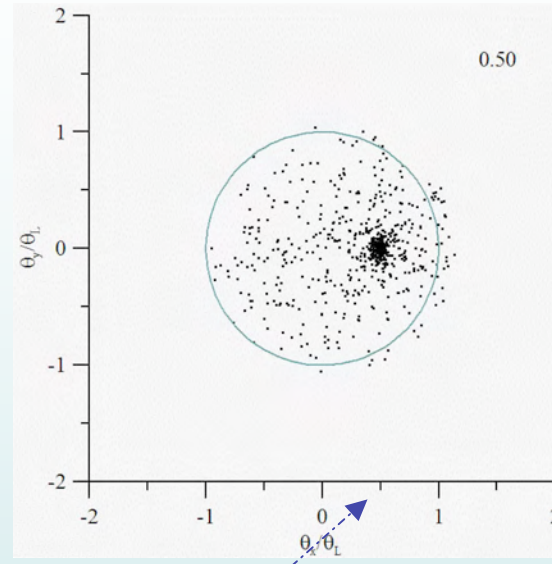
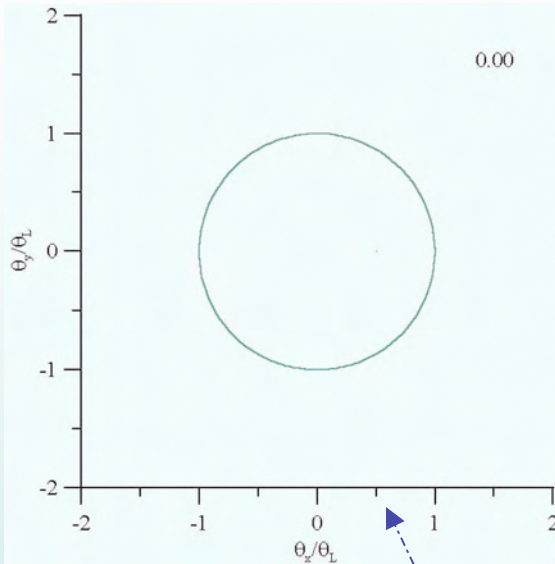


Phys. Lett. A250 (1998) 360
NIM B143 (1998) 584

Simulations for particles channeling (straight)

Angular distributions

Spatial



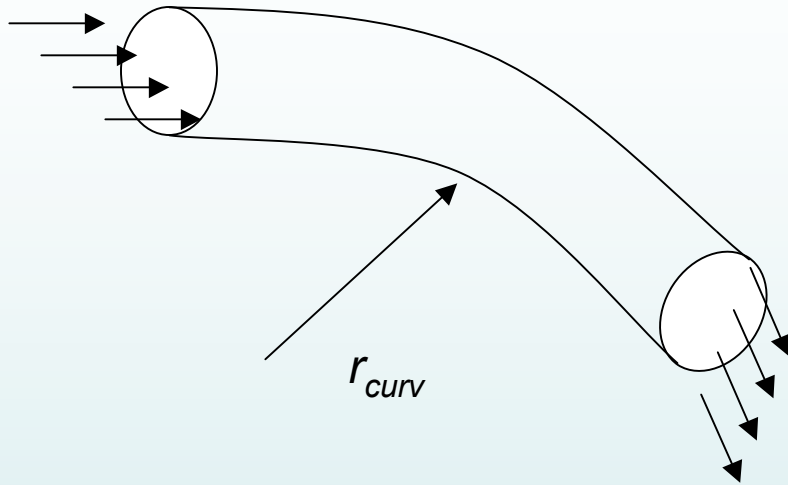
*Scattering within
coherence length:
 $0-L_c$*

*Dechanneling with
propagation length:
 $L_c-20L_c-10^3L_c$*

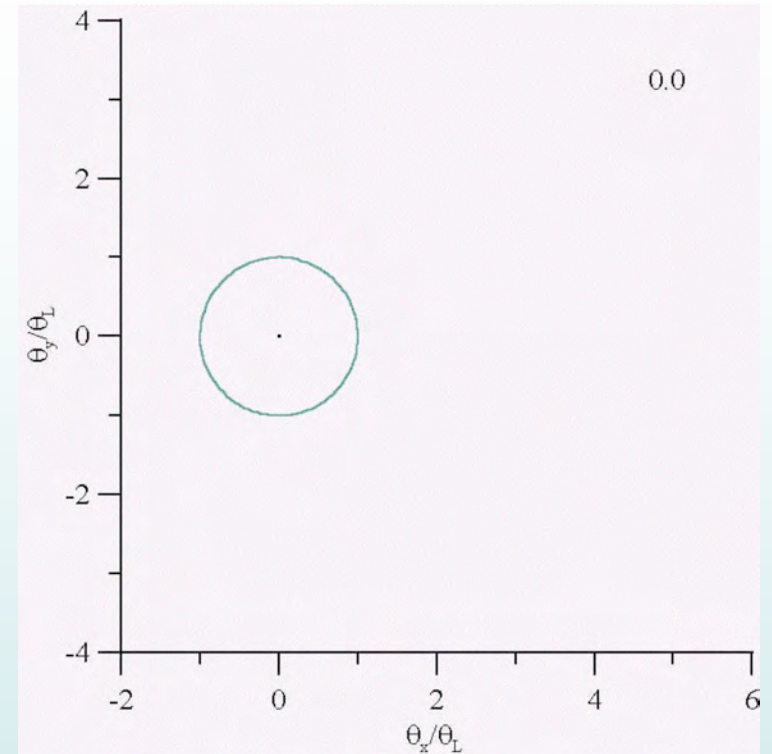
*Flux redistribution:
Channeling & dechanneling*

Angle of incidence – 0.5 critical angle of channeling

Simulations for channeling (bending)



Evolution of angular distribution



μ -capillary \rightarrow n -capillary:

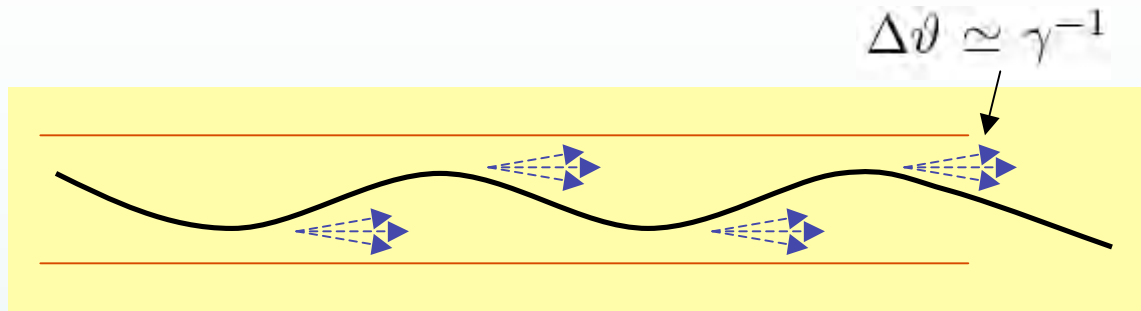
Strong bending effect (high efficiency!) on smaller scale

*Channeling:
Electrons and Positrons*

Channeling Radiation...

@ Channeling Radiation:

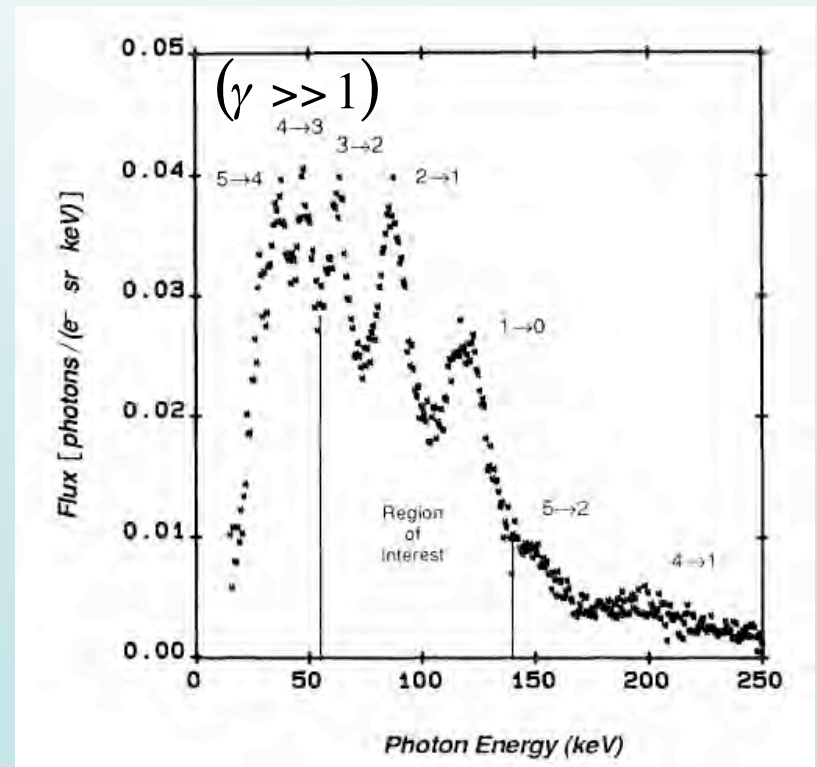
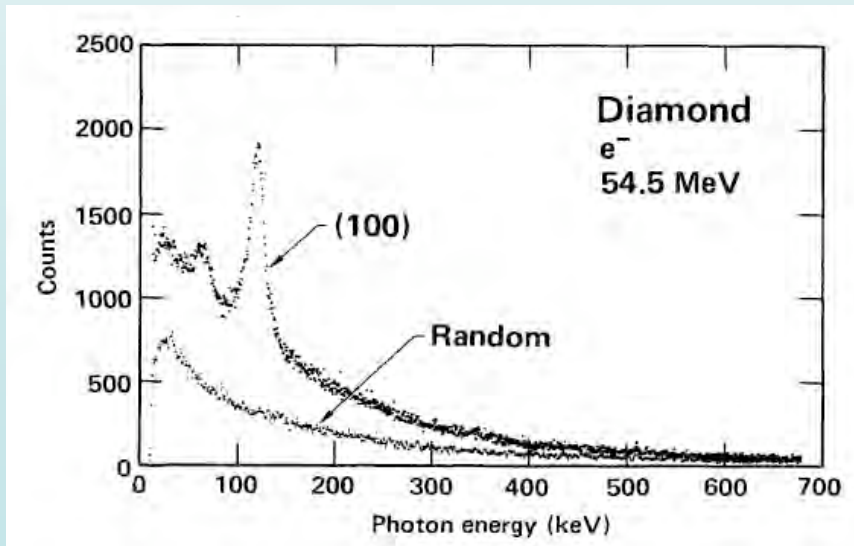
$$\omega = \omega(\theta) = \frac{\omega_{fi}}{1 - \beta_{\parallel} \cos \theta}$$



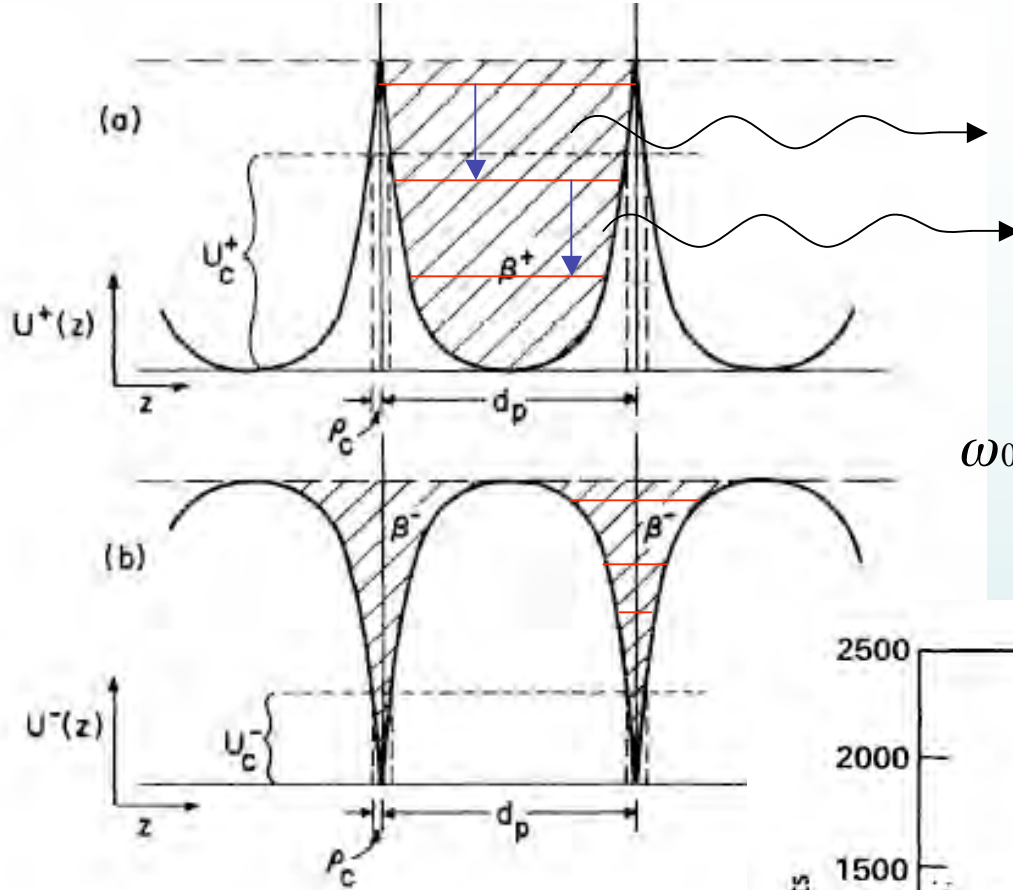
ω_{fi} - optical frequency \longrightarrow Doppler effect $\longrightarrow \omega\gamma^{3/2} \approx \omega\gamma^2$

Powerful radiation source of X-rays and γ -rays:

- polarized
- tunable
- narrow forwarded

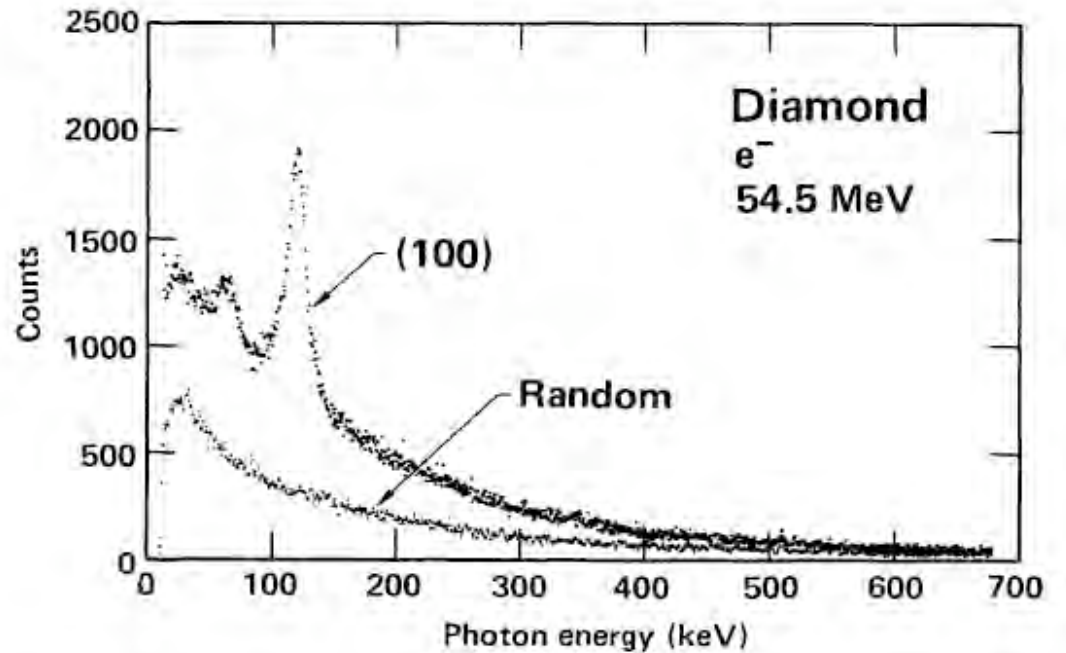


Channeling Radiation...strong Doppler effect



$$\omega_0 \propto 10 \text{ eV}$$

$$\omega_0 \rightarrow 2\gamma^2 \text{ max forward} \rightarrow 200 \text{ keV}$$



Bremsstrahlung & Coherent Bremsstrahlung vs Channeling Radiation

Bremsstrahlung (Deutsch, Sommerfeld) – brake radiation

@ amorphous - electron:

- Radiation as sum of independent impacts with atoms
- Effective radius of interaction – a_{TF}
- Coherent radiation length $l_{coh} \gg a_{TF}$
- Deviations in trajectory more than effective radiation angles:

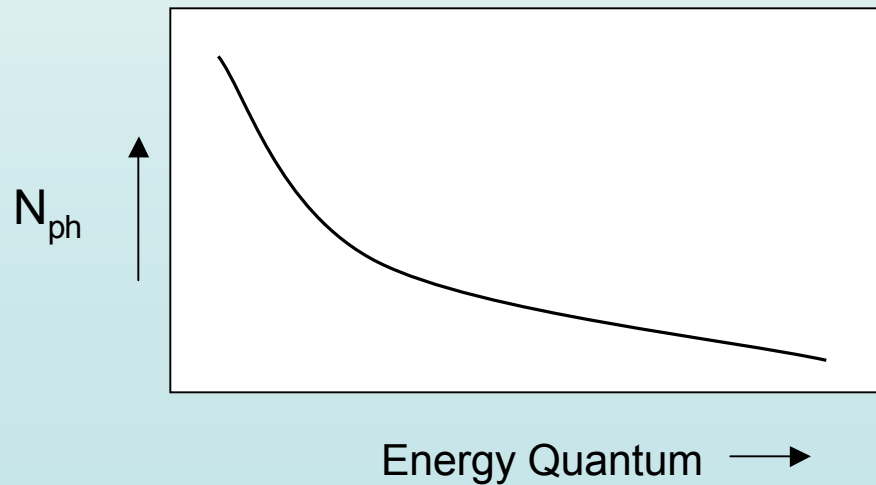
$$\Delta\theta \propto a_{TF} / p$$

$$\Delta\vartheta \simeq \gamma^{-1}$$

$$\left(\frac{d^2 I}{d\omega \Omega} \right)_{BR} \simeq (\pi L_R)^{-1} \gamma^2 \frac{1 + \gamma^4 \theta^4}{(1 + \gamma^2 \theta^2)^4}$$

→

$$\left(\frac{dI}{d\omega} \right)_{BR} \simeq \frac{4}{3} L_R^{-1}$$



Bremsstrahlung & *Coherent Bremsstrahlung* vs Channeling Radiation

@ interference of consequent radiation events:

phase of radiation wave $\longrightarrow (\omega t - \mathbf{k}\mathbf{r}(t))$

Radiation field as interference of radiated waves:

$$l_{coh} \approx \frac{v}{\omega - \mathbf{k}\mathbf{r}} = \frac{\lambda\beta}{1 - \beta \cos\theta} \longrightarrow l_{coh} \propto \gamma^2 \lambda$$

Coherent radiation length can be rather large even for short wavelength

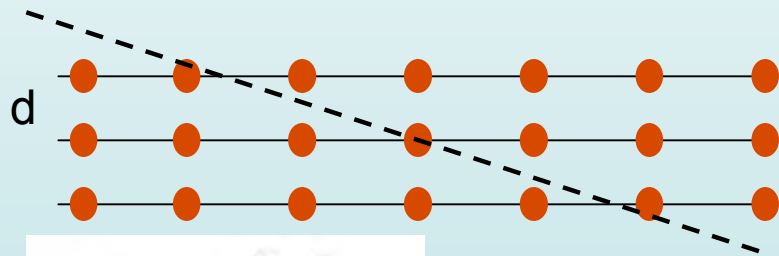
@ crystal:

$$l_1 = n l_{coh}$$

$$l = d / \sin \alpha$$

$$l_1 = \frac{n\lambda\beta}{1 - \beta \cos \theta}$$

$$\omega_0 \equiv \beta / l_1$$



$$\omega = \frac{n\omega_0}{1 - \beta \cos \theta}$$

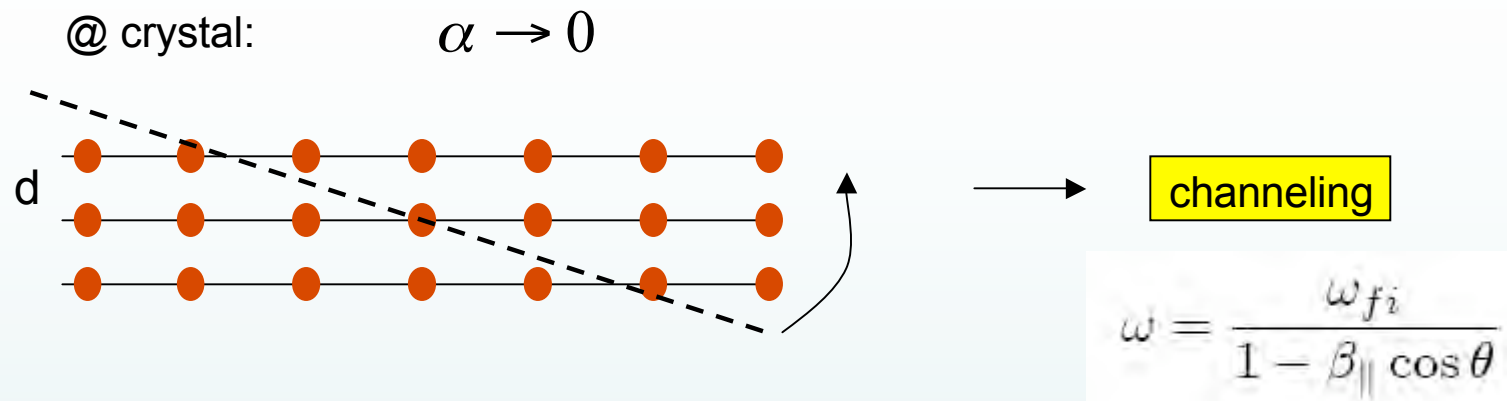
$$\left(\frac{d^2 I}{d\omega \Omega} \right)_{CBR} \propto \delta(\omega(1 - \beta \cos \theta) - n\omega_0)$$

N_{ph}



Energy Quantum \longrightarrow

Bremsstrahlung & Coherent Bremsstrahlung vs Channeling Radiation



$$\left(\frac{dI}{d\omega}\right)_{CR} \propto \omega \left[1 - 2 \left(\frac{\omega}{\omega_m}\right) + 2 \left(\frac{\omega}{\omega_m}\right)^2 \right], \quad \omega \leq \omega_m \simeq 2\gamma^2 \omega_{fi}$$

$\frac{ChR}{B} \propto \gamma^{1/2} Z^{-2/3}$ at definite conditions channeling radiation can be significantly powerful than bremsstrahlung

B:	CB:	ChR:
$\propto NZ^2$	NZe	$N \leftrightarrow l_{coh} \propto \gamma^2 / \omega \quad N_{eff}$
	$\propto (NZ)^2$	$\propto (N_{eff} Z)^2$

SPARC & SPARX & SPARXINO

SPARC

R&D program towards high brightness e⁻ beam & SASE-FEL experiment
(150 MeV e⁻ : $\lambda \sim 500$ nm)

SPARX Phase I - SPARXINO

R&D towards an X-ray FEL-SASE source (1.25 GeV : $\lambda < 10$ nm)

Self
S
P
A
R
X

Source

Pulsed

Amplified

Radiation

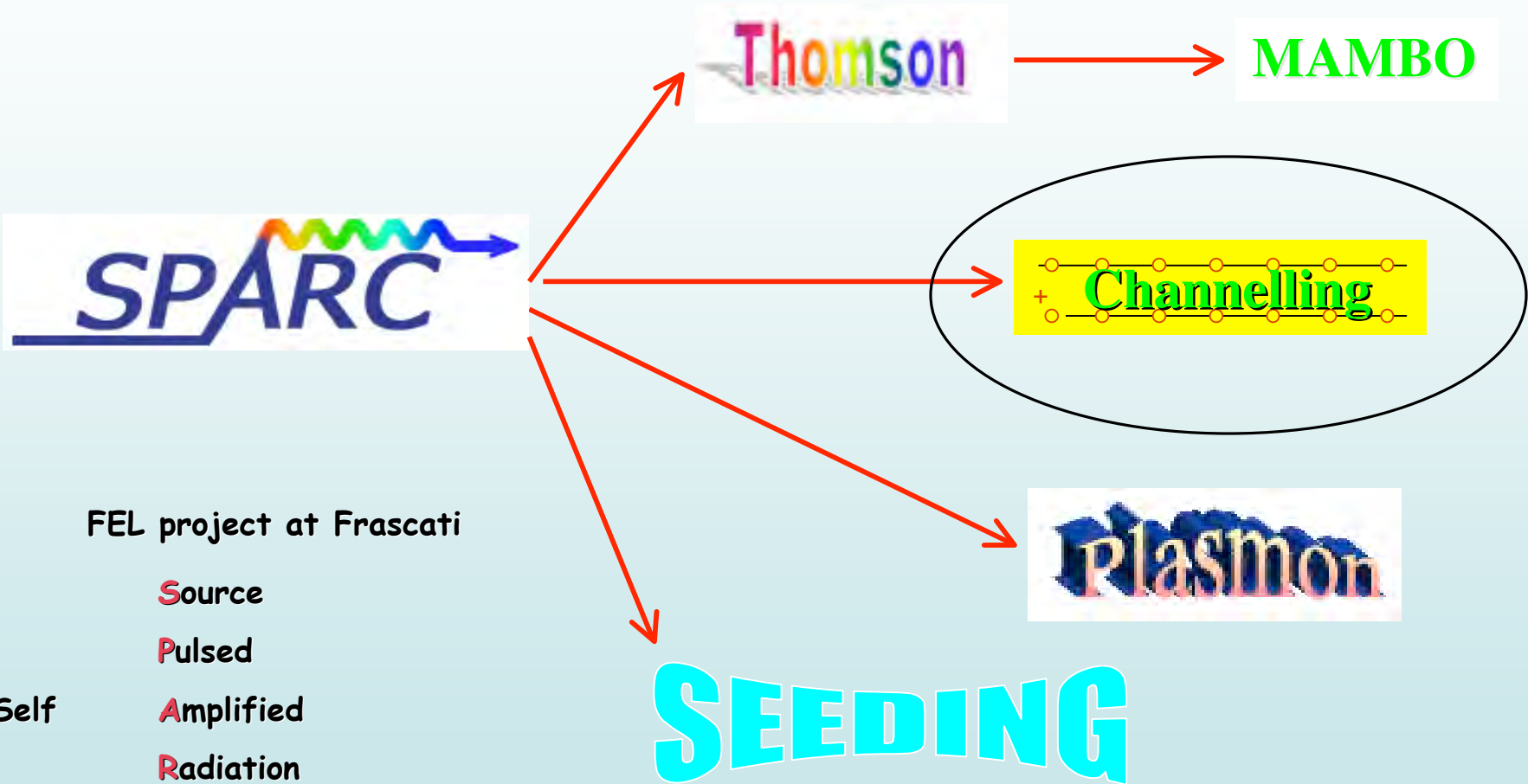
X

SPARX

(2.5 GeV e⁻ : $\lambda = 13.5 - 1.5$ nm)

Self-Amplified Pulsed X Radiation Source

Channeling Radiation & Coherent Bremsstrahlung



FEL project at Frascati

Source

Pulsed

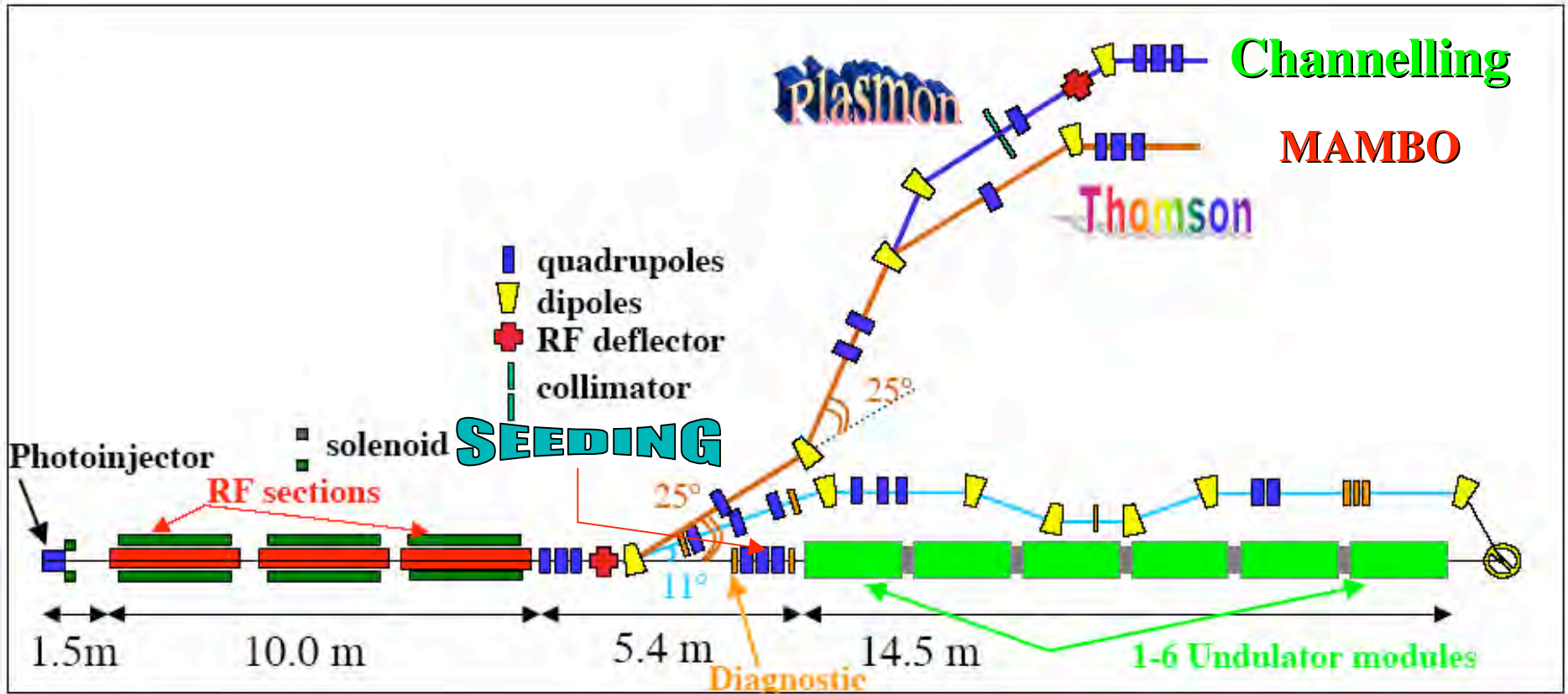
Self Amplified

Radiation

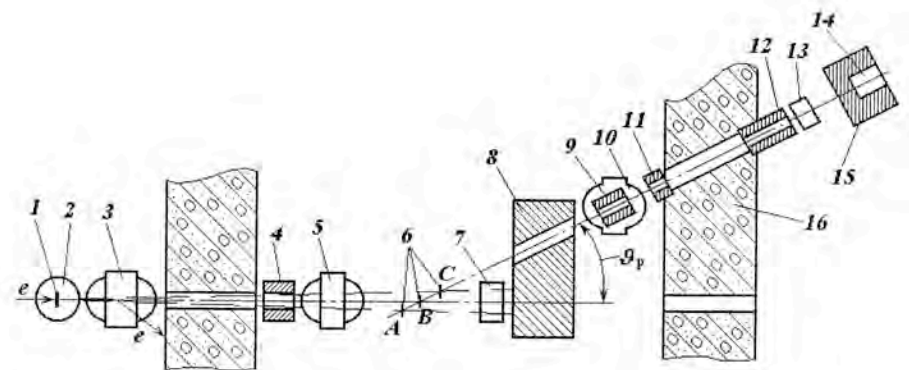
Coherent

Self-Amplified Pulsed Coherent Radiation Source

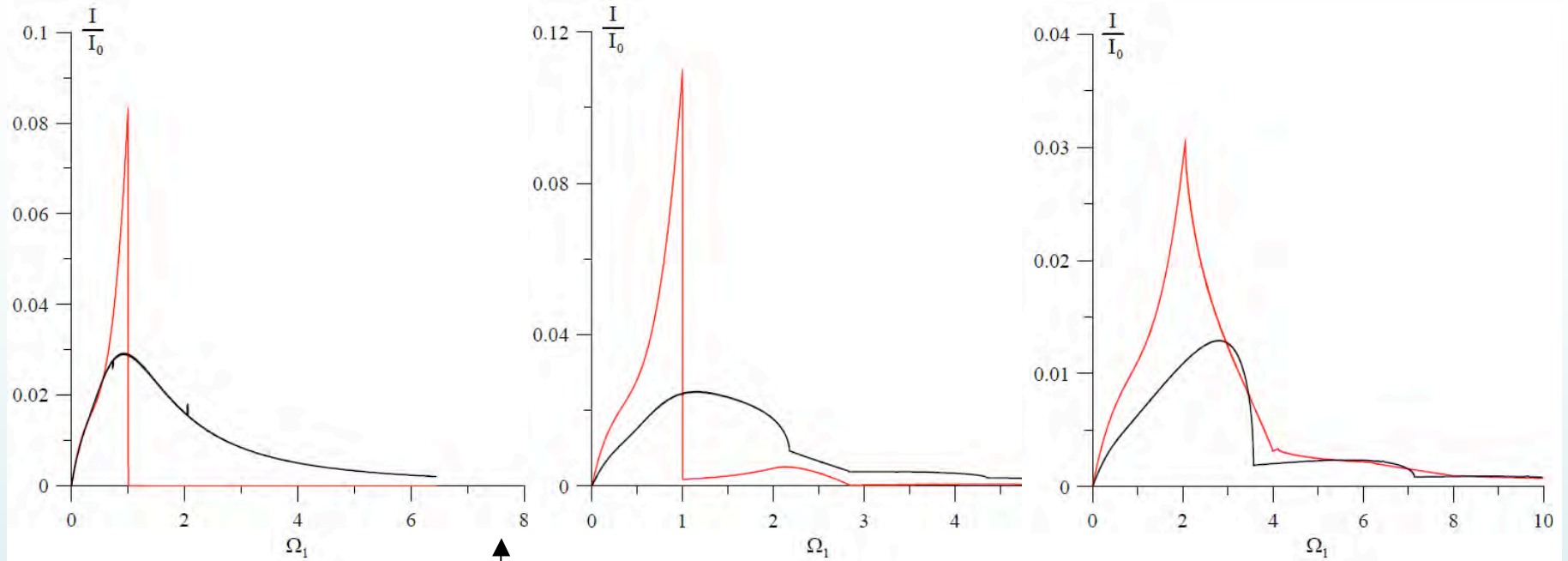
Experimental scheme



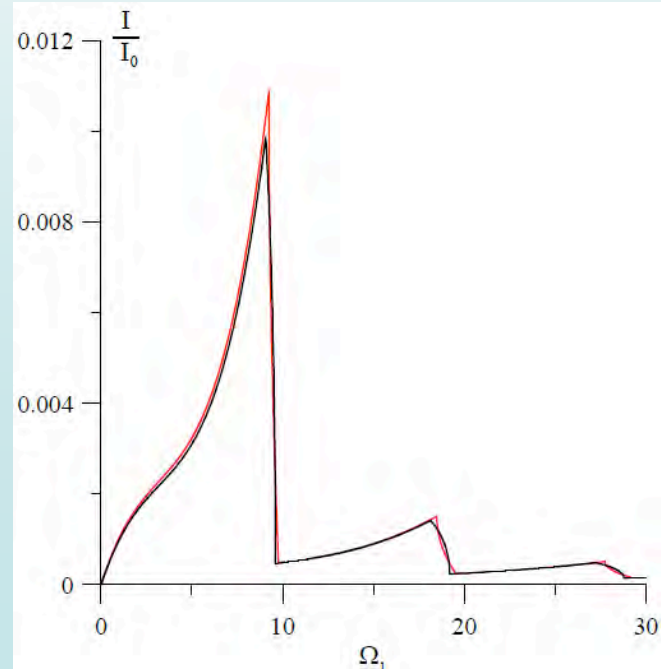
“Channeling” line layout
by Kharkov group



Calculation of ChR spectra



Channeling Radiation
VS
Coherent Bremsstrahlung



Channeling Radiation vs Thomson Scattering

$$\omega_{lab}^{ChR} \approx \frac{2\gamma^2}{1 + \theta^2\gamma^2} \omega_0^{ChR} \quad \text{- radiation frequency -} \quad \omega_{lab}^{TS} \begin{cases} \vartheta = 0 \\ \vartheta = \pi/2 \\ \vartheta = \pi \end{cases} \simeq \begin{cases} 1 \\ 2 \\ 4 \end{cases} \frac{\gamma^2}{1 + \vartheta^2\gamma^2} \omega_0^{TS}$$

$\propto \gamma^{3/2}$ $\propto \gamma^2$

$$\left(\frac{dN_{ph}}{dt}\right)_{ChR} \propto \gamma^{1/2} \quad \text{- number of photons per unit of time -} \quad \left(\frac{dN_{ph}}{dt}\right)_{TS} \propto Const$$

$$P \propto \gamma^2 \quad \text{- radiation power -} \quad P \propto \gamma^2$$

@ comparison factor: $f \simeq \frac{\mathbf{A}_{Ch}^2 L_{Ch}}{\mathbf{A}_{TS}^2 L_{TS}} \rightarrow L_{Ch}(z) \simeq \int_0^z N_{ch}(z) dz$
 Laser beam size & mutual orientation

@ strength parameters – crystal & field:

$\mathbf{A}_{Ch}^2, \text{ eV}/\text{\AA}^3$	Si <110>	C <100>	W <111>
	~ 520	~ 580	~ 10000

$\mathbf{A}_{TS}^2 \sim 700 \text{ eV}/\text{\AA}^3$ for the 10 TW laser with a beam diameter of 0.1 mm

Channeling Radiation vs Thomson Scattering

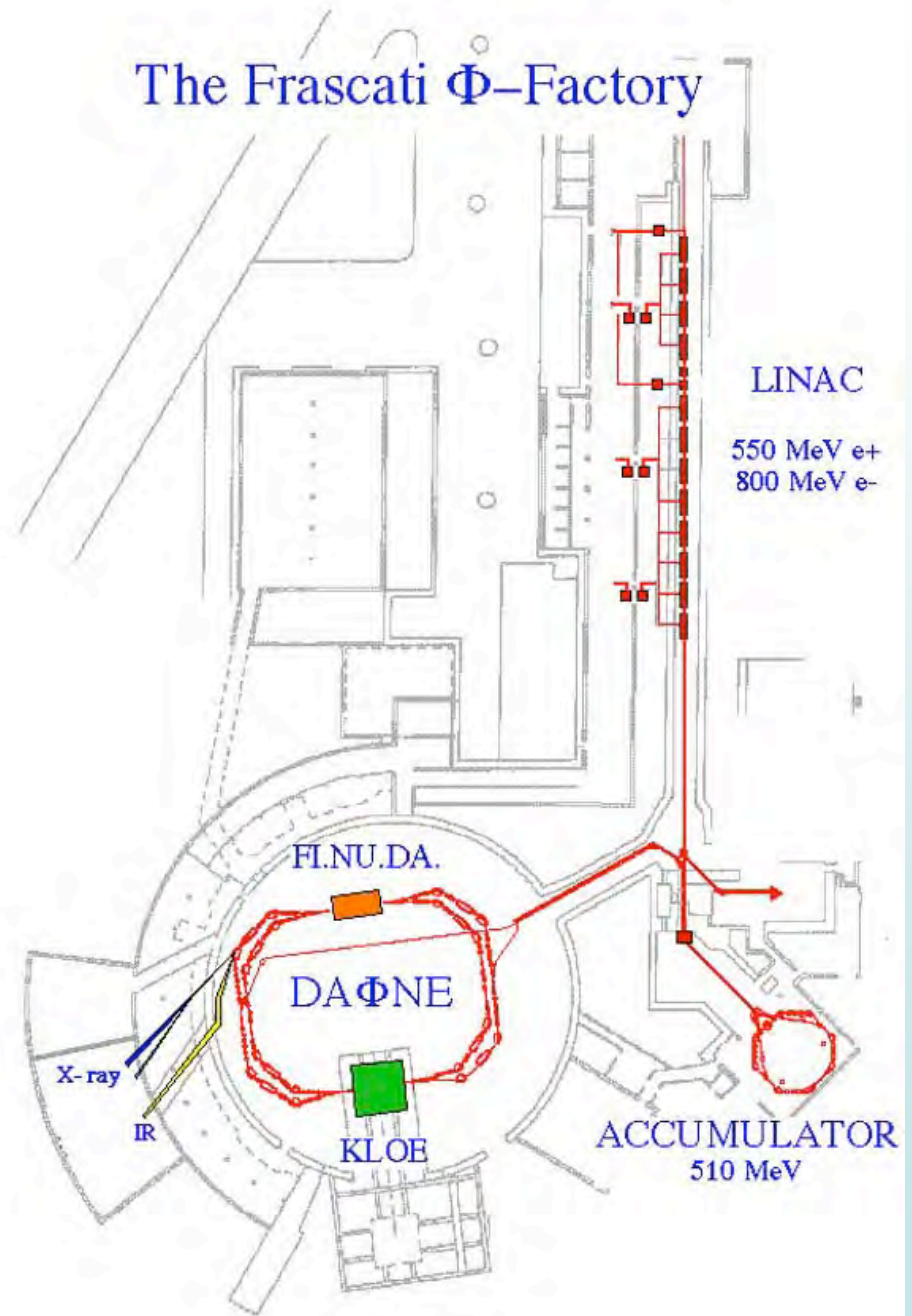
For X-ray frequencies: **100 MeV** electrons **channeled** in 105 μm Si (110) emit $\sim 10^{-3}$ ph/e⁻
corresponding to a Photon Flux $\sim 10^8$ ph/sec

ChR – effective source of photons in very wide frequency range:

- in x-ray range – higher than B, CB, and TS
- however, TS provides a higher degree of monochromatization and TS is not undergone incoherent background, which always takes place at ChR

SPARX-ino proposal

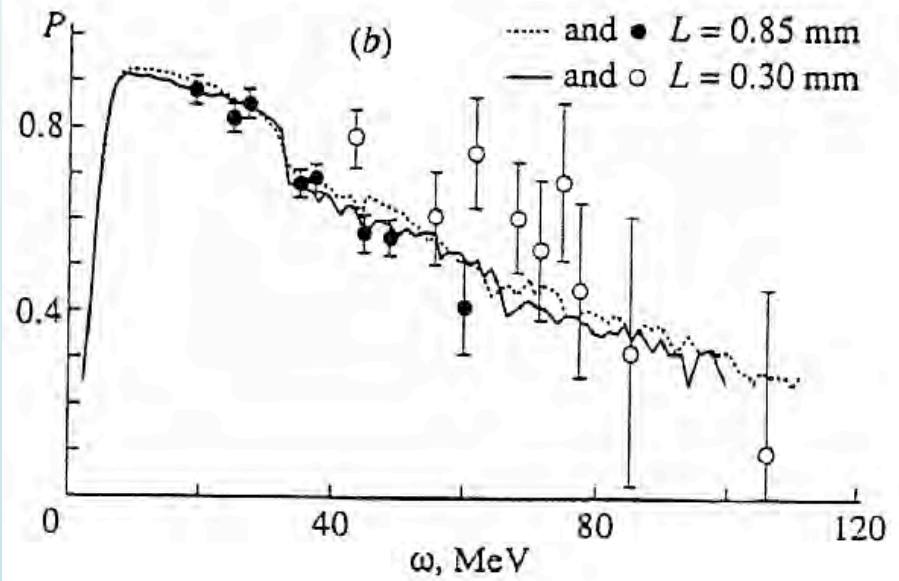
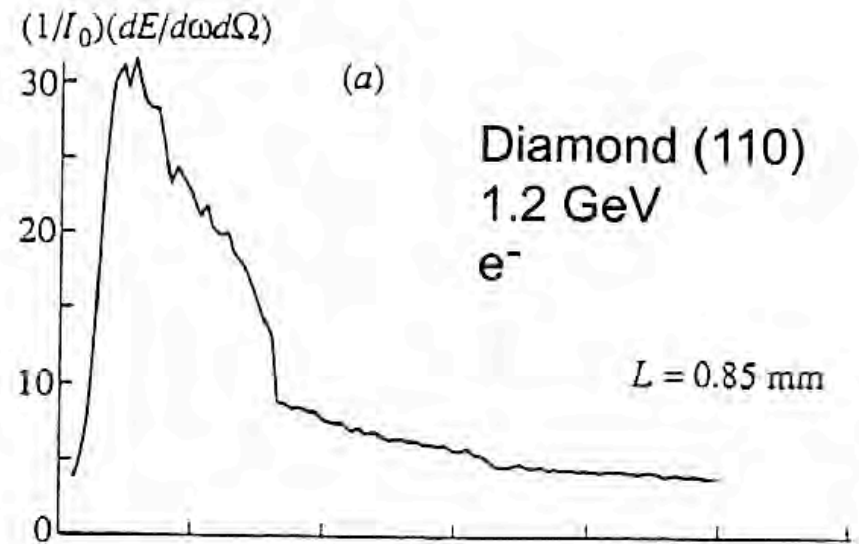
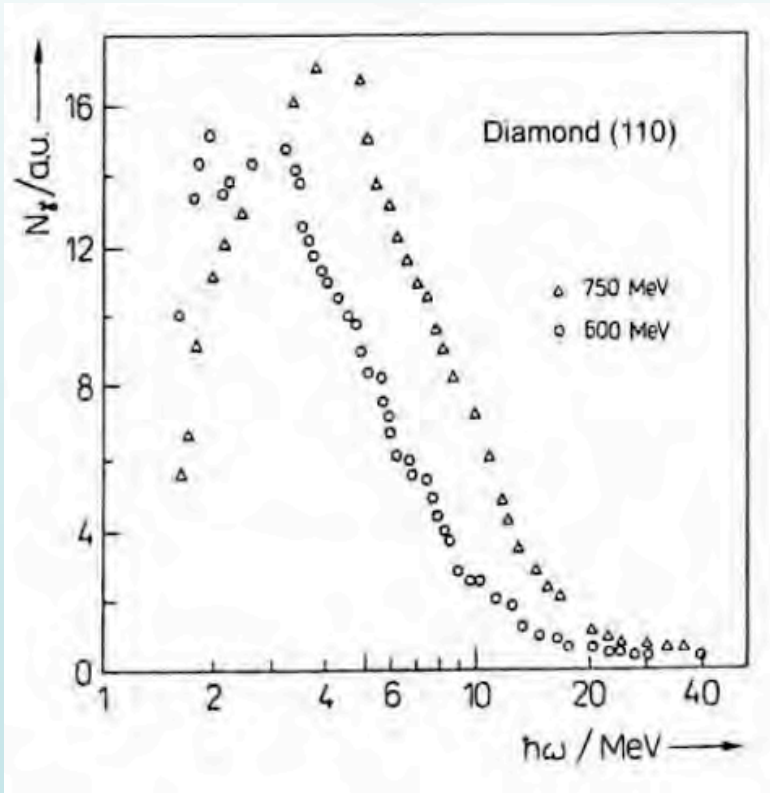
- Upgrade the DAFNE Linac to drive a 5-10 nm SASE-FEL
- Beam energy : 1.2 - 1.5 GeV
- Upgrade the injector to a RF photo-injector (SPARC-like)
- Proposal in preparation



Spectra for e^+/e^- channeling

Channeling Radiation

0.5 – 1.2 GeV



Comparison: Channeling Radiation vs Bremsstrahlung

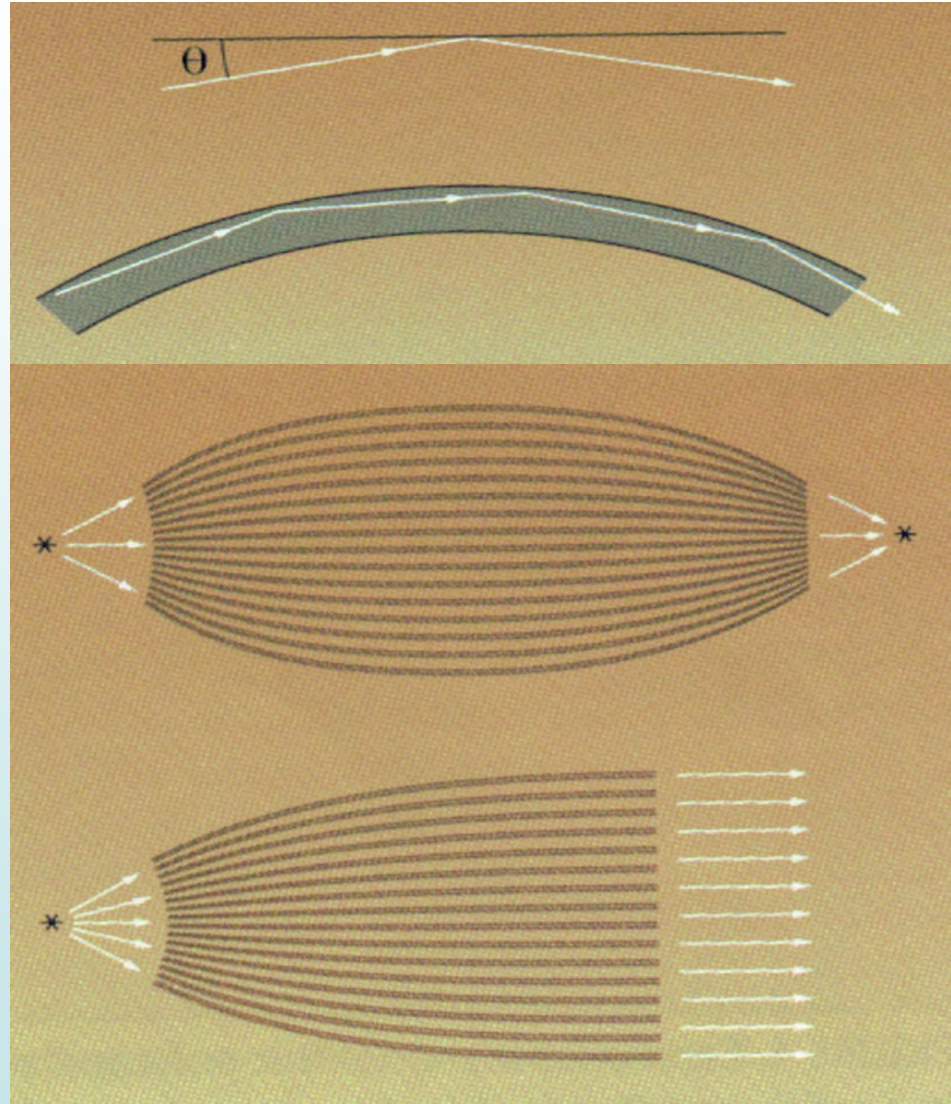
		Diamond (110)					Si (110)				
U_0	eV	23.46					21.28				
d	Å	1.2611					1.9201				
I_{BH}	cm ⁻¹	0.11					0.14				
		E	θ_L	ω_1	I_0	I_0/I_{BH}	E	θ_L	ω_1	I_0	I_0/I_{BH}
		MeV	mrad	MeV	cm ⁻¹		MeV	mrad	MeV	cm ⁻¹	
		150	0.559	0.302	34.89	317	150	0.533	0.189	19.80	141
		450	0.323	1.567	60.43	549	450	0.308	0.980	34.29	245
		750	0.250	3.372	78.02	709	750	0.238	2.109	44.27	316
		1000	0.217	5.192	90.09	819	1000	0.206	3.248	51.11	365
		1200	0.198	6.825	98.69	900	1200	0.188	4.269	55.99	400



*Channeling:
X-Rays and Neutrons*

X-ray and neutron capillary optics

@ Basic idea of **polycapillary optics** is very close to the phenomenon of charged **particle channeling**



X-ray & Neutron Channeling: samples of capillary optics



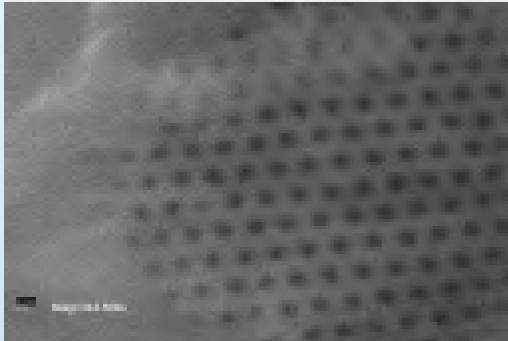
1st generation:
[m]



2^d generation:
[cm]

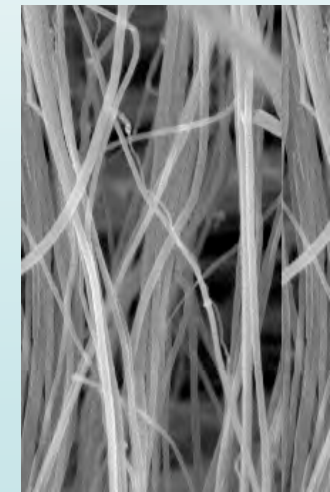


3^d & 4th generations:
[mm]



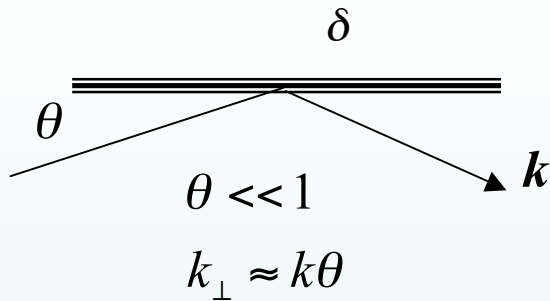
5th generation:
[μm – nm]

<http://www.unisantis.com>
<http://www.iroptic.com>



?n-capillaries?

Quantum base

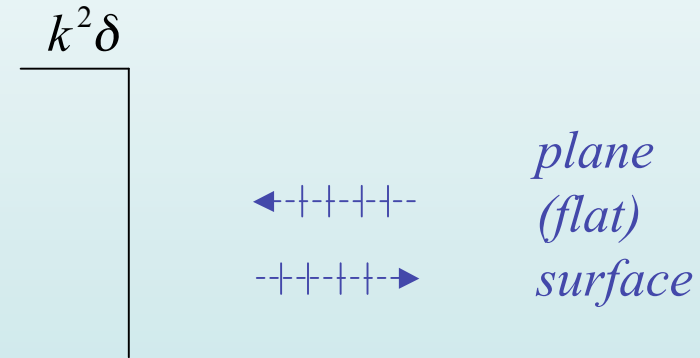


1st order: $\Delta\varepsilon(\vec{r}) = 0$ - no roughness

Wave equation:

$$\left(-\nabla^2 + \underbrace{k^2 \delta(\vec{r}_{\perp})}_{V_{eff}} - k_{\perp}^2 \right) E(\vec{r}_{\perp}) = 0$$

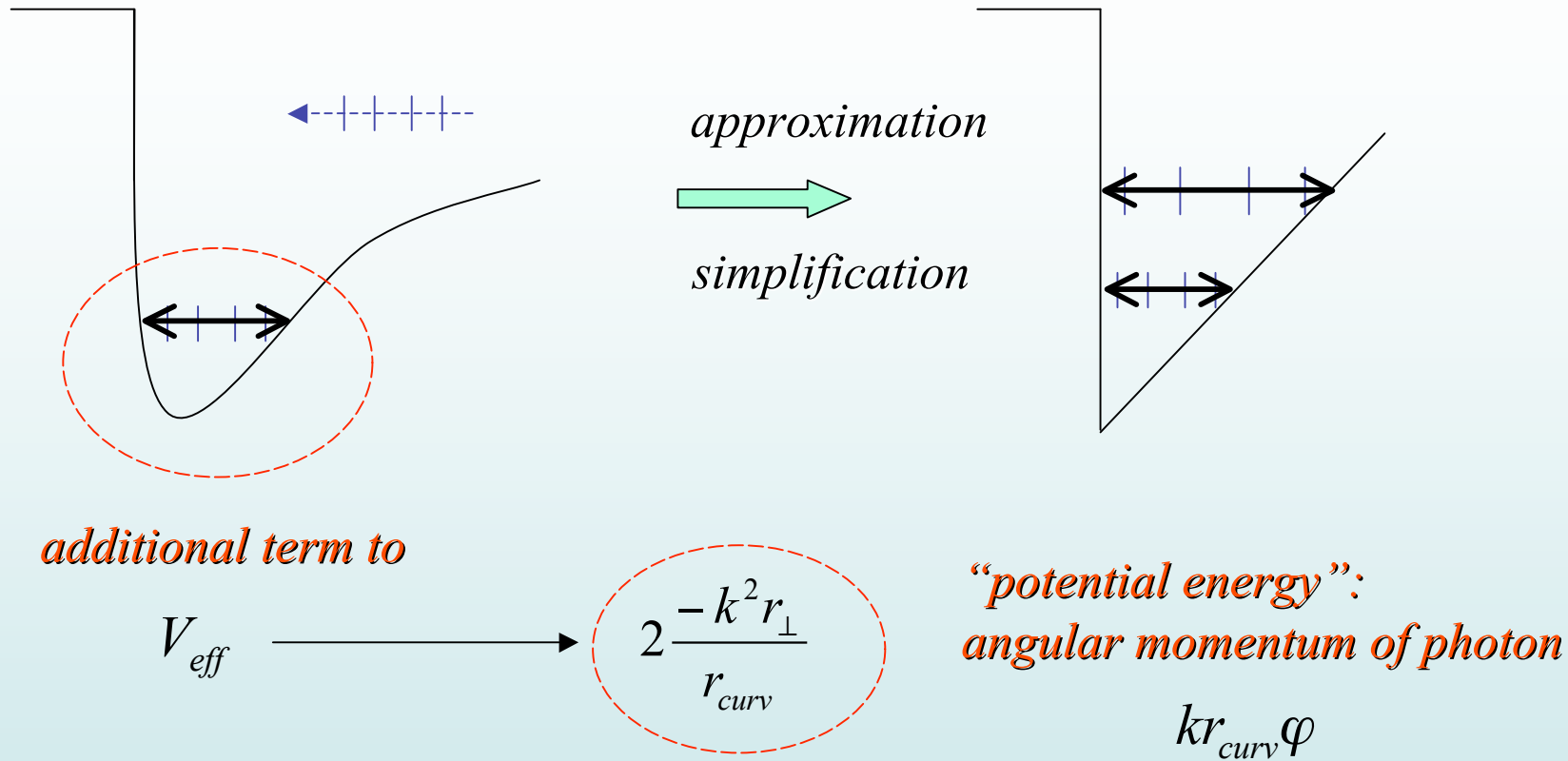
$$k^2 (\delta(\vec{r}_{\perp}) - \theta^2) = \begin{cases} -k^2 \theta^2, & r_{\perp} < r_1 \\ k^2 (\delta_0 - \theta^2) & r_{\perp} \geq r_1 \end{cases}$$



Total external reflection

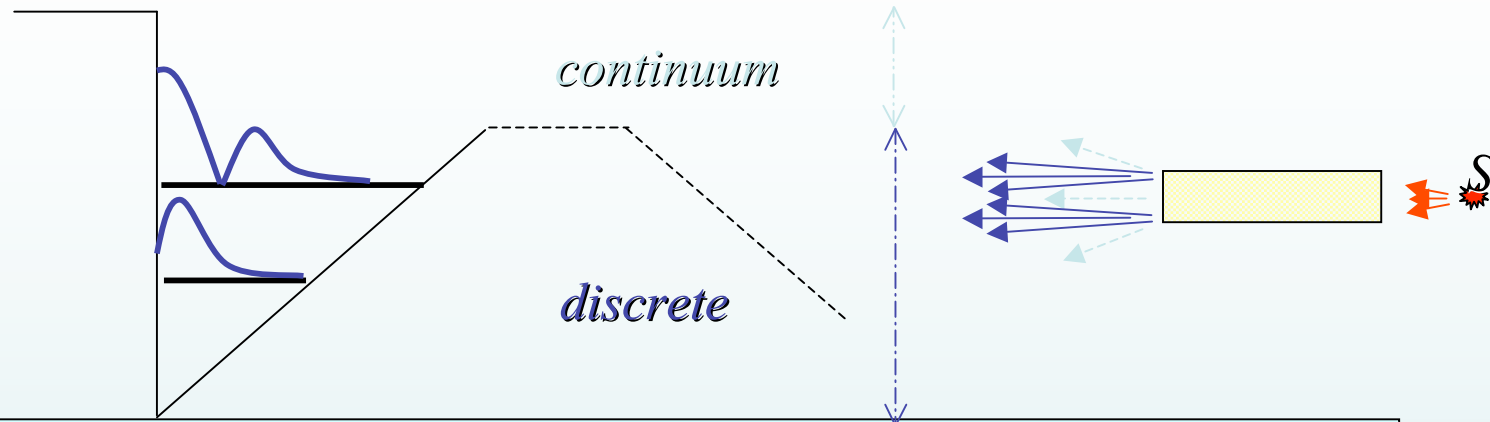
$$V_{eff} \equiv 0 \Rightarrow \theta_c \equiv \theta \approx \sqrt{\delta_0}$$

Quantum base (2) - curvature

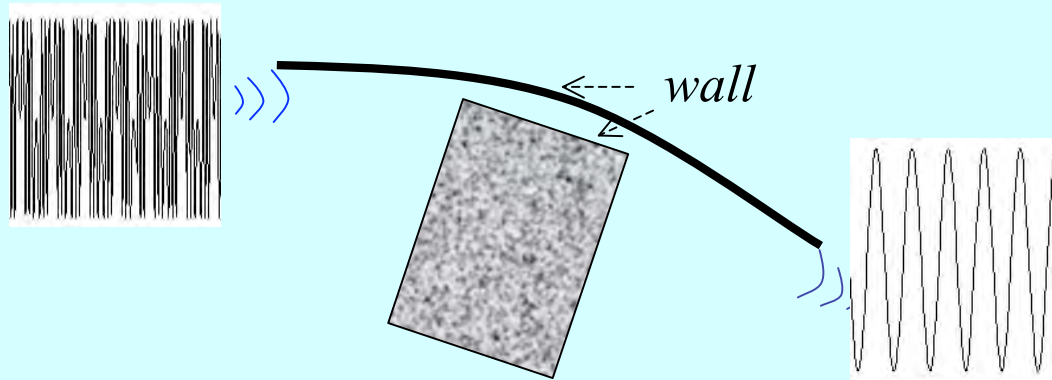


$$V_{eff} = k^2 \left(\delta(r_{\perp}) - \theta^2 - 2 \frac{r_{\perp}}{r_{curv}} \right)$$

Surface channeling - "whispering X gallery"



*** Whispering:**



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Divergence behavior due to surface channeling in capillary optics

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C. Gramaccioni and A. Pifferi

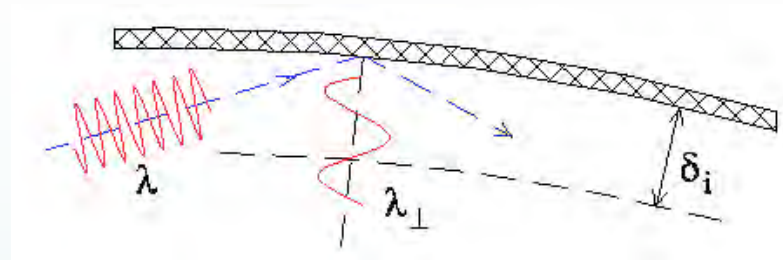
CNR—Istituto di Strutturistica Chimica, P.O. Box 10, I-00016 Montelibretti Sc., Italy

Modes of channeling along curved surfaces

$$\vec{k} = (k_{\perp}, k_{\parallel})$$

$$k_{\perp} \simeq k\theta \quad (\theta < \theta_c)$$

$$\lambda_{\perp} = \lambda/\theta \gg \lambda$$



Effective guide channel



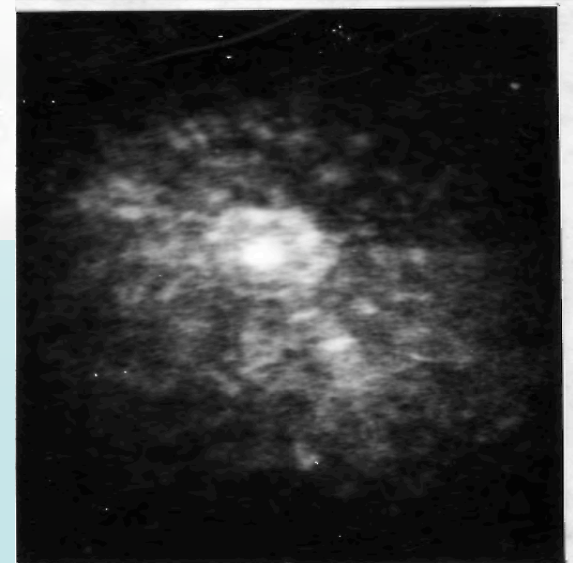
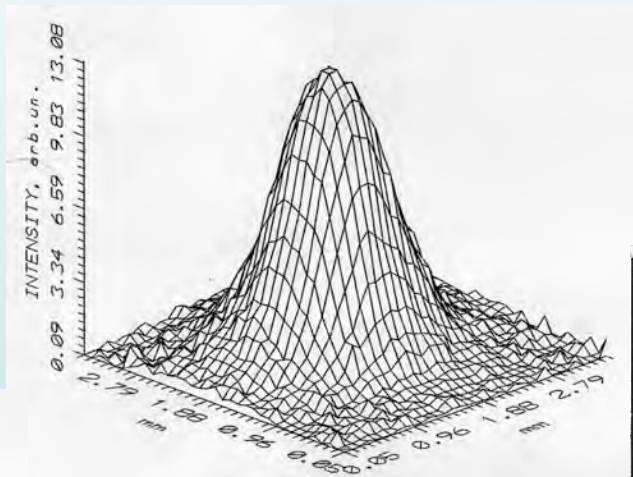
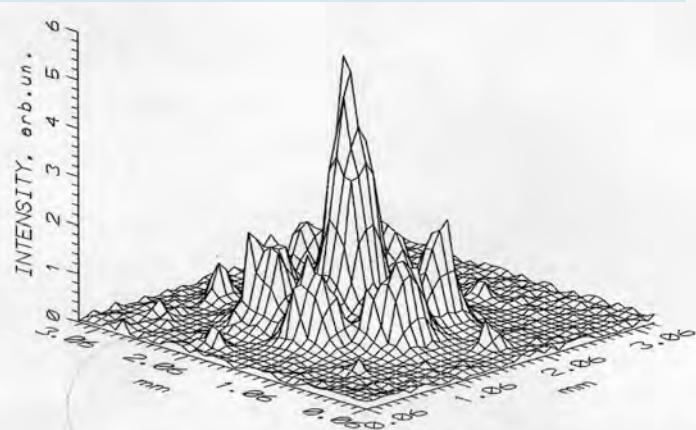
$$\delta_i(\theta) \simeq \lambda_{\perp}(\theta)$$

$$(r_{\text{curv}})_i \theta^3 \sim \lambda$$

$$(r_{\text{curv}})_i = 1 \text{ cm} \div 1 \text{ m}$$


$$\theta \simeq 10^{-3} \text{ rad}$$

$$\lambda \simeq 0.1 \div 10 \text{ \AA}$$



J.Synchrotron. Rad. 1995
Phys. Lett. A 1995

Down to bulk photon and neutron channeling

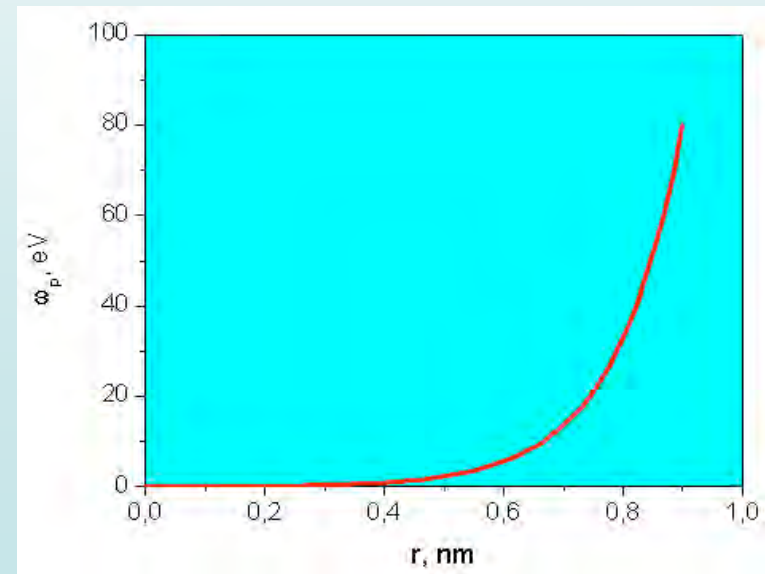
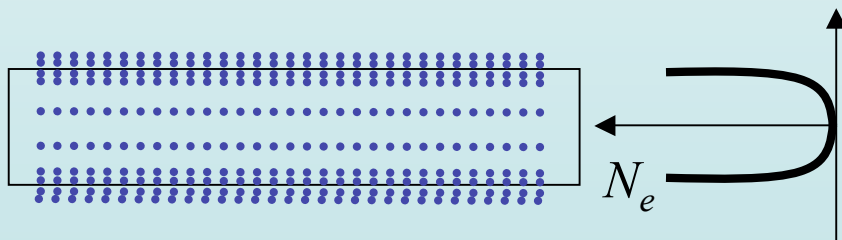
λ

 μm

$\theta \ll 1 \quad (\theta_c \sim 10^{-3})$: grazing incidence optics
 $\lambda \rightarrow \lambda_{\perp} \gg \lambda$: from nm to μm
 $d_0 \sim 1 \mu m \div 10 \mu m : \lambda_{\perp} \ll d_0$: **surface channeling**

λ

 nm

$\theta_d = \lambda/d_0 \sim \theta_c$: diffraction angle approaches Fresnel angle
 $\lambda_{\perp}/d_0 \sim 1$: **bulk channeling**



X-Ray channeling in nanotubes

JETP Letters, Vol. 81, No. 1, 2005, pp. 34–38. Translated from *Fiz'ma v Zhurnal Éksperimental'noi i Teoreticheskoi Fiziki*, Vol. 81, No. 1, 2005, pp. 37–42
Original Russian Text Copyright © 2005 by Okotrub, Dabagov, Kudashov, Gusel'nikov, Kinloch, Windle, Chuvilin, Bulusheva

Orientalional Effect of the Texture of a Carbon-Nanotube Film on the Intensity of CK_{α} Radiation

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² Laboratori Nazionali di Frascati, INFN, I-00044 Frascati (RM), Italy

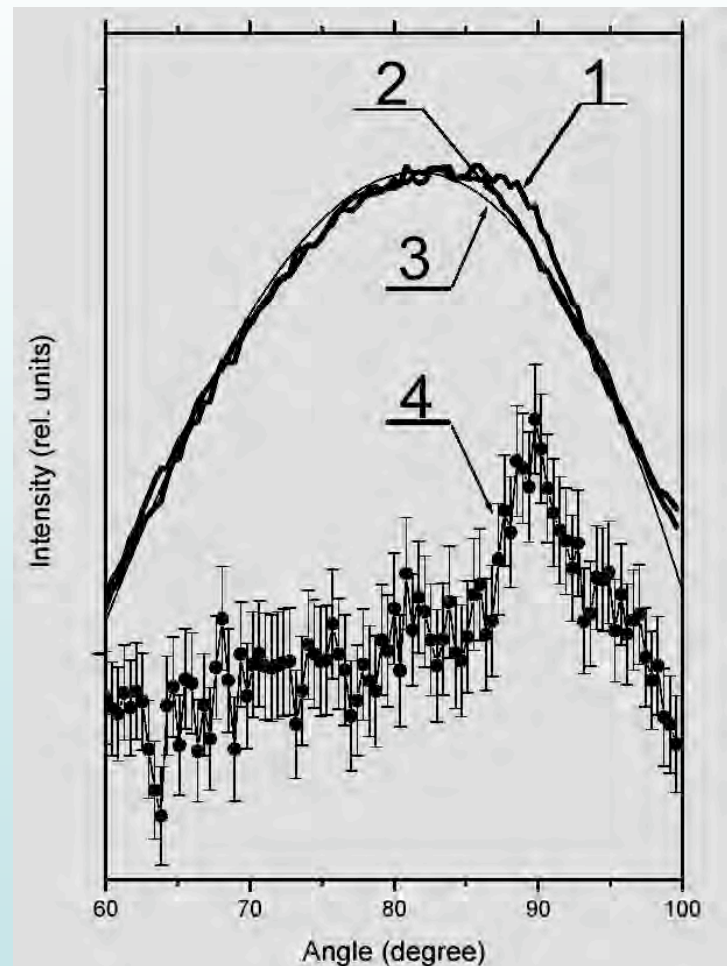
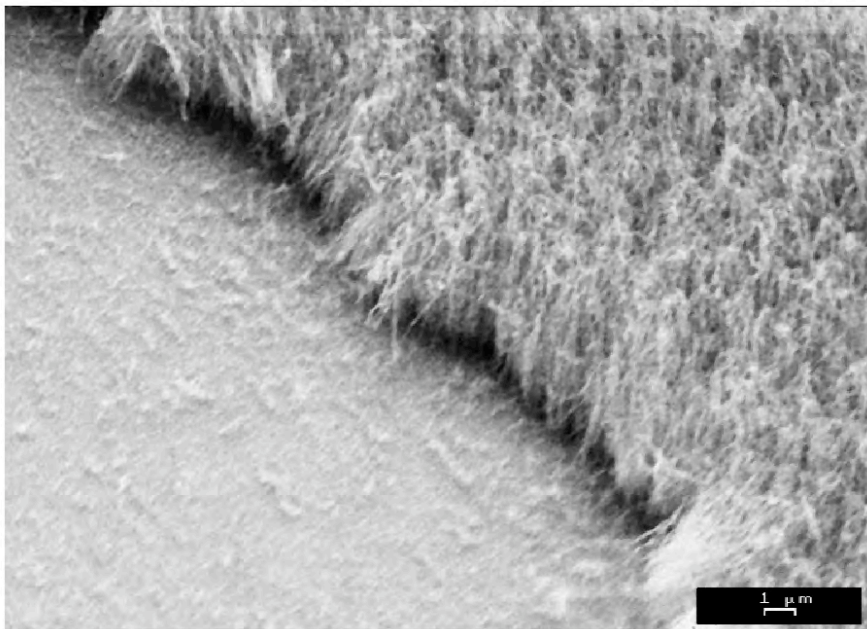
³ Lebedev Physical Institute, Russian Academy of Sciences, Leninskii pr. 53, Moscow, 117924 Russia

⁴ Department of Materials Science and Metallurgy, Cambridge, United Kingdom

⁵ Boreskov Institute of Catalysis, Siberian Division, Russian Academy of Sciences,
pr. akademika Lavrent'eva 5, Novosibirsk, 630090 Russia

Received September 16, 2004; in final form, December 6, 2004

The angular dependence of the intensity of CK_{α} radiation measured from a film of oriented carbon nanotubes shows an increase in the yield of x-ray fluorescence along the growth direction of nanotubes. The angular distribution of the intensity of scattered x rays is close in magnitude to the angular distribution of the directivity of nanotubes in the film, which is determined by analyzing an electron-microscope image. To explain the propagation of radiation along the nanotubes, two mechanisms are proposed on the basis of reflection from inner walls of a tube (channeling) and an anomalous dispersion of CK_{α} photons in the carbon medium. © 2005 Ple-



Channeling 2004 - Channeling 2006

@ “Channeling 2004”

Workshop on Charged and Neutral Particles

Channeling Phenomena

(Frascati 2-6 November 2004)

<http://www.lnf.infn.it/conference/channeling>

- Radiation of relativistic charged particles in periodic structures
- Coherent scattering of electrons and positrons in crystals
- Channeling radiation of electrons and positrons in crystals
- Channeling of X-rays and neutrons in capillary systems (micro- and nano-channeling)
- Novel types of sources for electromagnetic radiation (FEL, powerful X-ray sources)
- Applications of channeling phenomena (novel radiation sources, X-ray waveguides, capillary/polycapillary optics)

@ “Channeling 2006”

International Conference on Charged and Neutral Particles

Channeling Phenomena

(LNF INFN, June 2006)

...with extended subjects for topics...

Collaboration & Acknowledgements

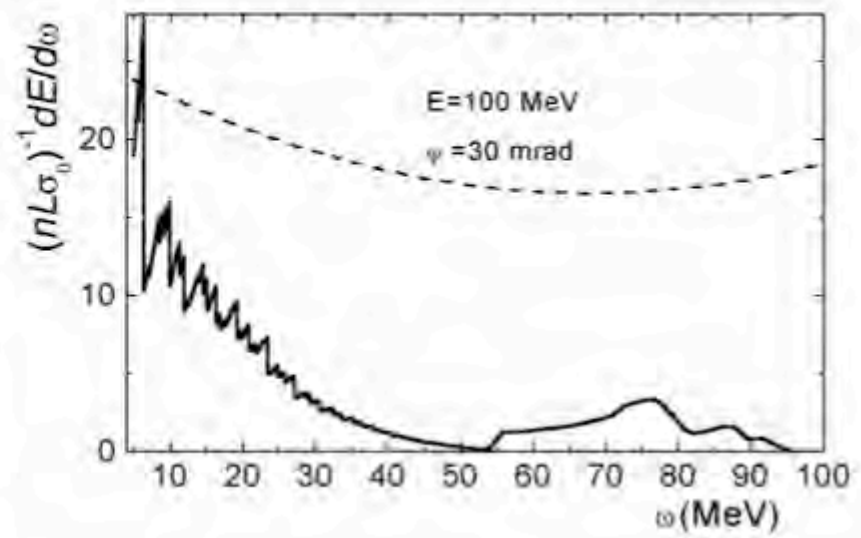
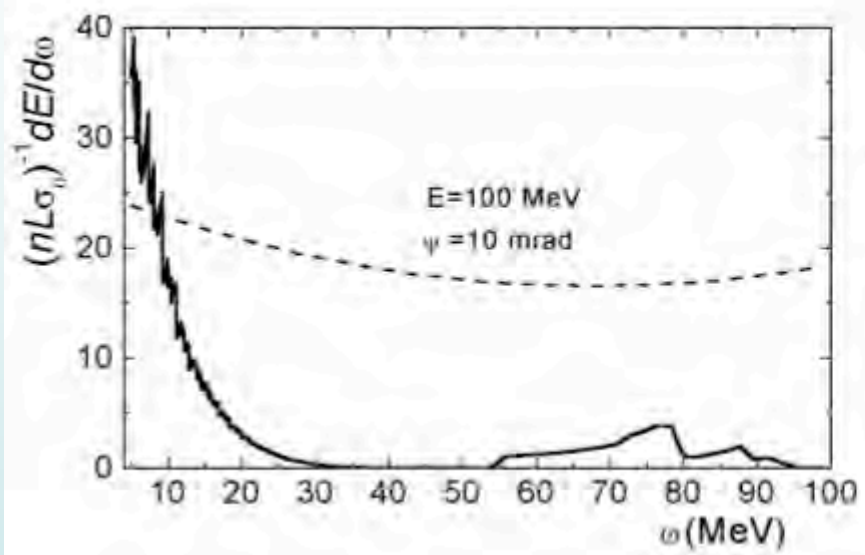
We have started collaboration with groups from:

Italy, Russia, USA, France, Germany, Switzerland,
Ukraine, Belarus, Armenia

...list will be extended...

Appendix

Additional material

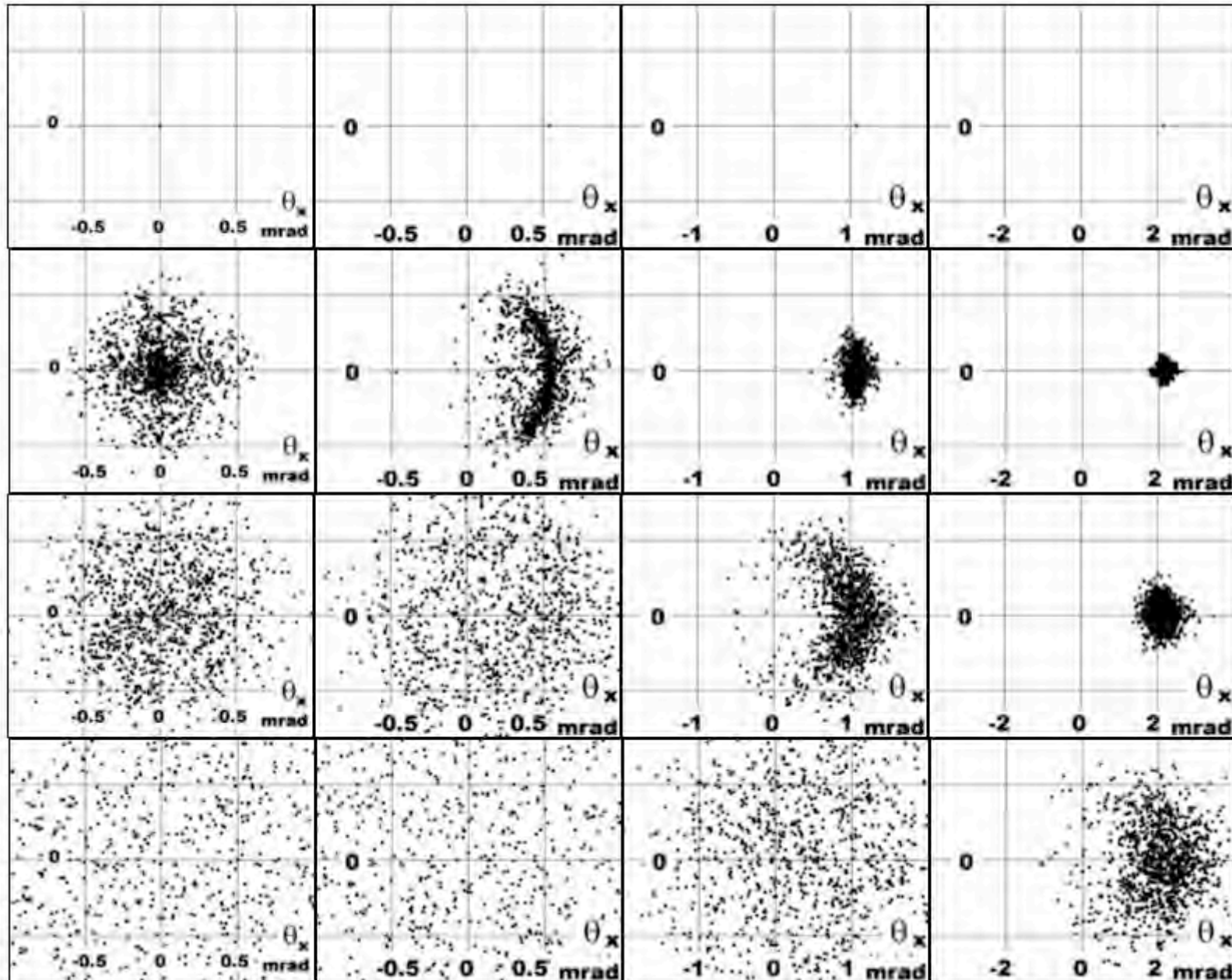


$$\psi_0 = 0 \psi_c = (0.0, 0.0) \text{ mrad}$$

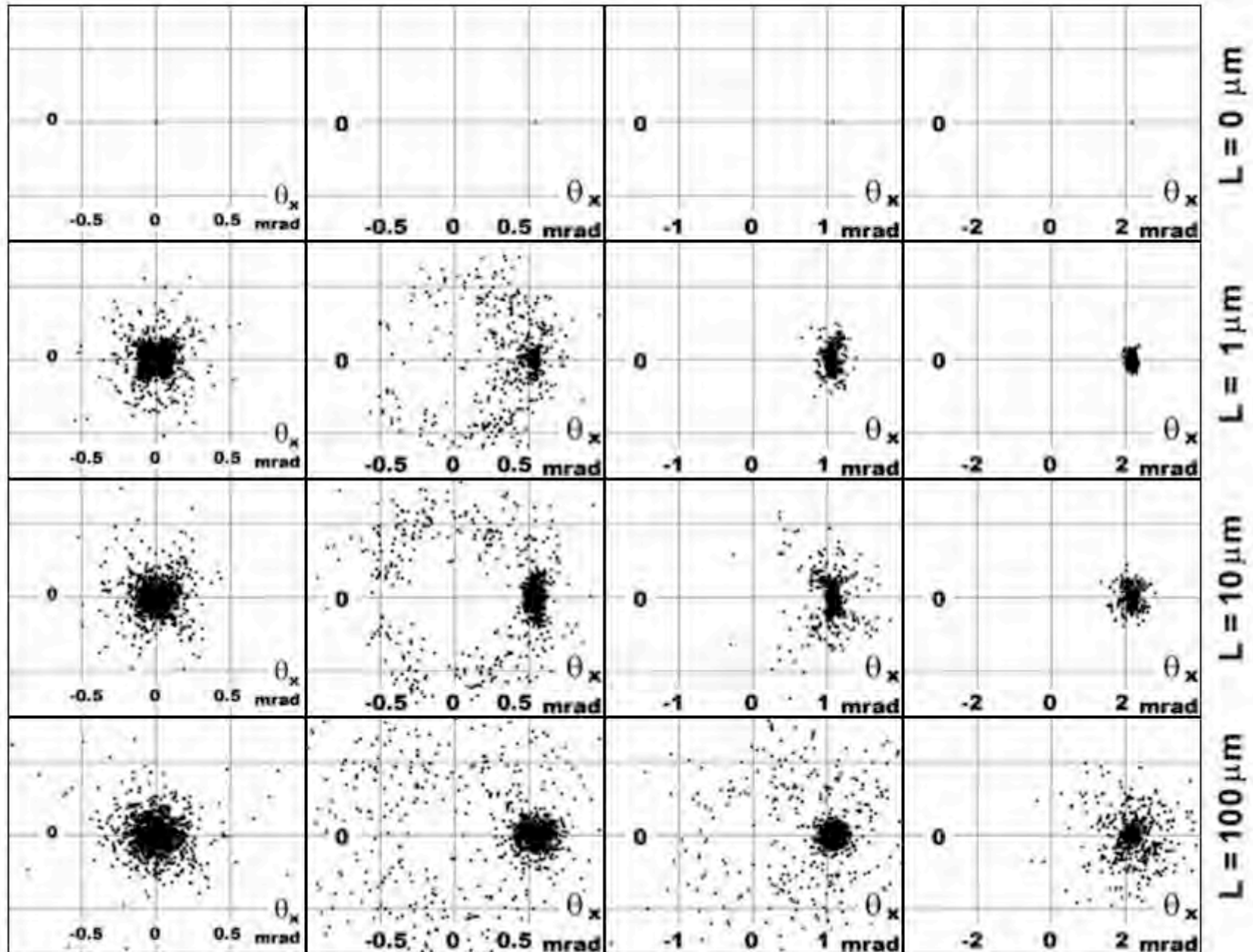
$$\psi_0 = 1 \psi_c = (0.55, 0.0) \text{ mrad}$$

$$\psi_0 = 2 \psi_c = (1.1, 0.0) \text{ mrad}$$

$$\psi_0 = 4 \psi_c = (2.2, 0.0) \text{ mrad}$$



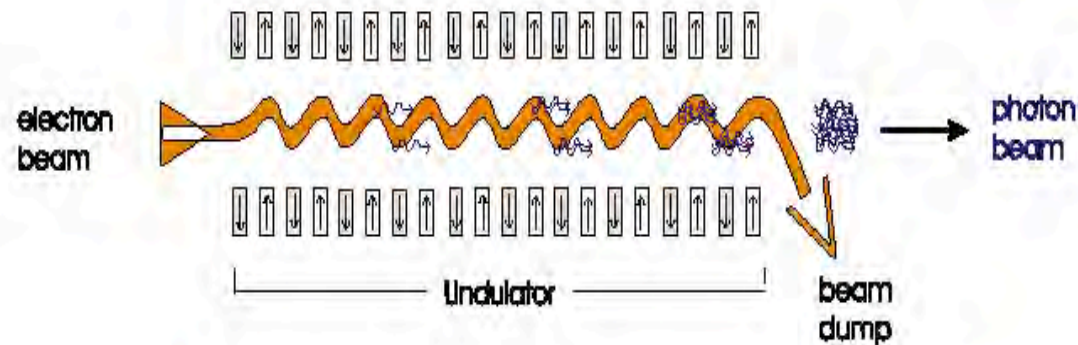
$$\psi_0 = 0\psi_c = (0.0, 0.0) \text{ mrad} \quad \psi_0 = 1\psi_c = (0.55, 0.0) \text{ mrad} \quad \psi_0 = 2\psi_c = (1.1, 0.0) \text{ mrad} \quad \psi_0 = 4\psi_c = (2.2, 0.0) \text{ mrad}$$



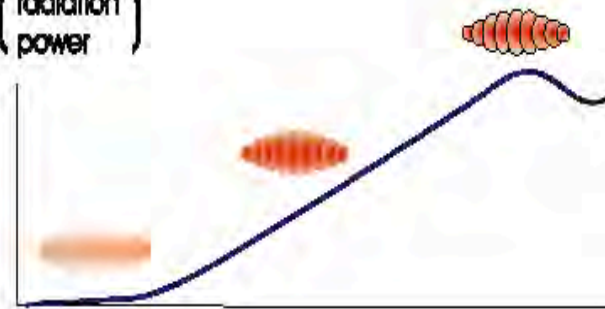
**The Scientific Case in the 10 nm \Rightarrow 1 nm range:
High Peak Brightness ($> 10^{30}$) Ultra-short (< 100 fs) radiation pulses are of
great interest in various areas**

- **molecular physics** (vibrational modes, bond breaking and formation at $\lambda=10$ -1 nm)
- **physics of the clusters** (phase transitions at $\lambda=10$ -1 nm,)
- **surface and interfaces** (real time dynamics and phase transitions, $\lambda=10$ -1 nm)
- **time resolved chemical reactions** (metastable and transition states, magnetic scattering, confined systems, $\lambda=10$ -1 nm)

Free Electron Laser Self-Amplified-Spontaneous-Emission (No Mirrors - Tunability - Harmonics)



log(radiation power)

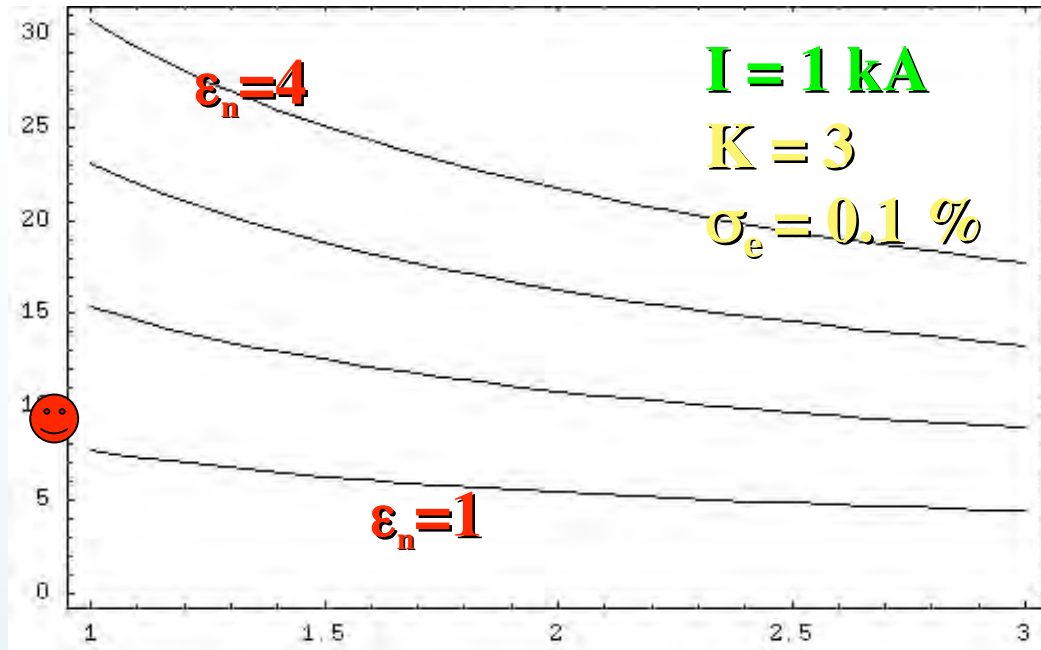


distance

$$\lambda_r = \frac{\lambda_u}{2\gamma^2} (1 + a_u^2 + \gamma^2 \theta^2)$$

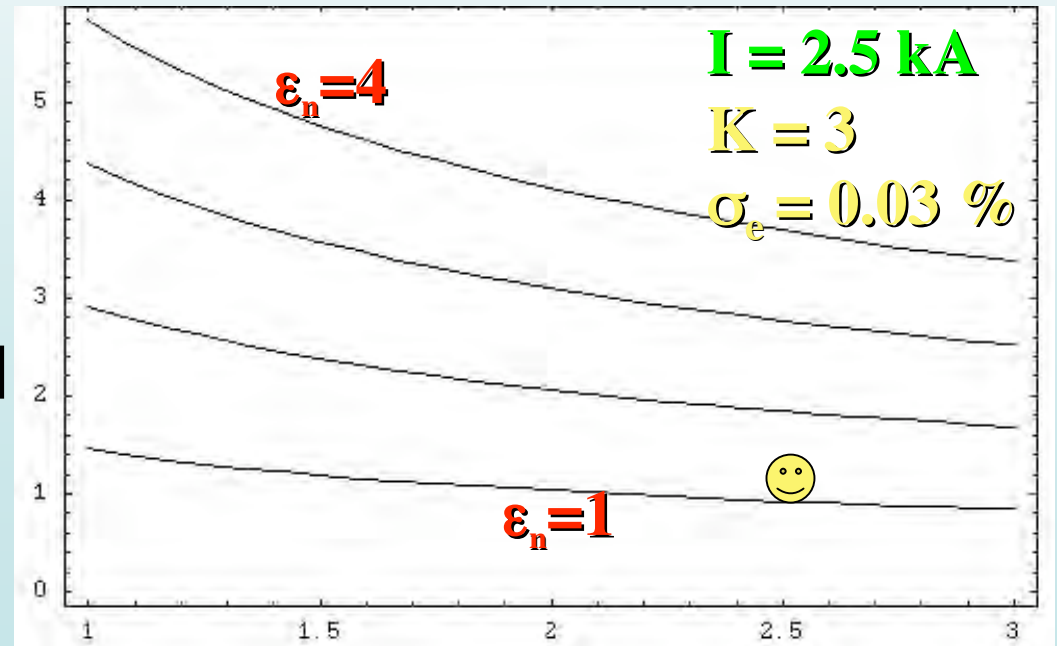
The SPARX-ino opportunity

λ_{cr}
[nm]



Energy [GeV]

λ_{cr}
[nm]



Energy [GeV]

Potential for neutral particles: Moliere approximation

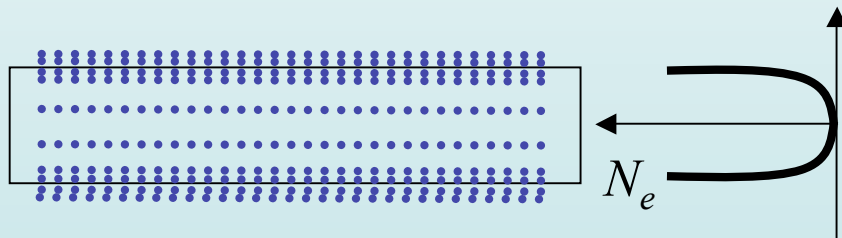
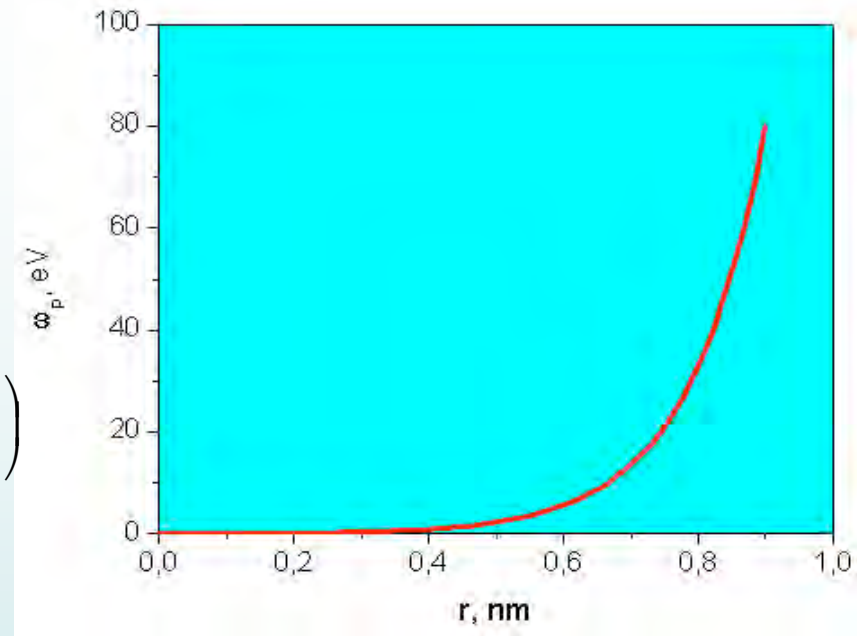
$$N_e(r) = \frac{Z}{4\pi a^2 r} \sum_{i=1}^3 \alpha_i \beta_i^2 \exp\left(-\frac{\beta_i r}{a}\right)$$

$$C: \quad Z = 6$$

$$a \approx 0.05Z^{-1/3} - \text{screening length}$$

$$\bar{N}_e(r) \approx \frac{r_{curv} n_a Z}{\pi a^2} \sum_i \alpha_i \beta_i^2 \int_0^\pi d\theta K_0\left(\frac{\beta_i \rho}{a}\right)$$

$$\rho = \left(r^2 + r_{curv}^2 - 2rr_{curv} \cos\theta\right)^{1/2}$$



“Continuous filtration”

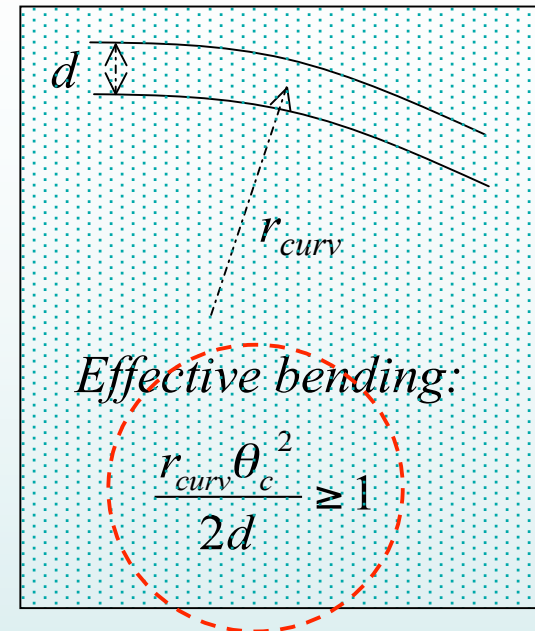
Phys. Lett. A250 (1998) 360
NIM B143 (1998) 584

Nanocapillary: Bending efficiency

$$n = \sqrt{1 - \theta_c^2} \approx \sqrt{1 - \frac{\omega_p^2}{\omega^2}}$$

$$\omega_p = \sqrt{\frac{4\pi N_e e^2}{m}} - \text{plasma frequency}$$

ω - photon frequency



μ -capillary: 10^0 - 30^0 through 10-20cm

*n -capillary: the reduce of the dimensions by several orders
with much higher efficiency*

Thomson

$$E_x \cong 2\gamma^2 E_{\text{las}} (1 - \cos\psi)$$

$$N_X \propto \Sigma_T f \frac{N_{e^-} N_{h\nu}}{\sigma_{\text{coll}}^2} = 2 \cdot 10^{9/11}$$

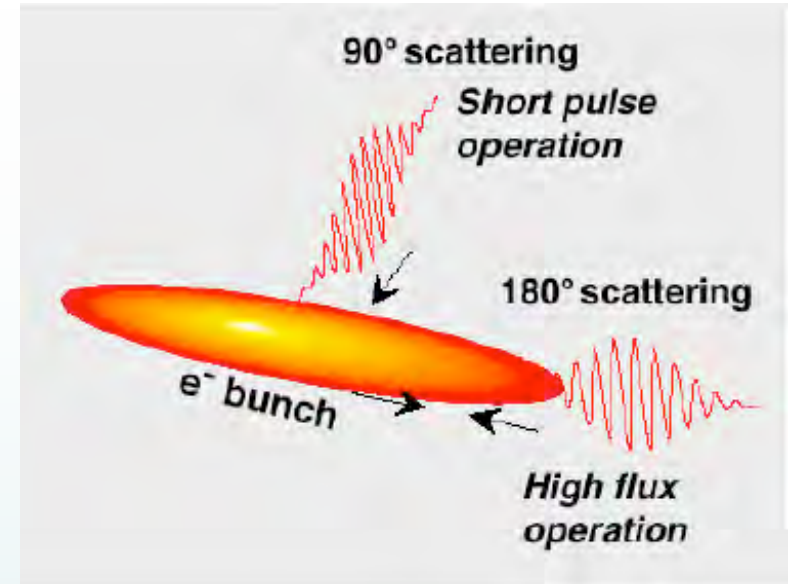
- Produzioni di impulsi X :

10⁹ fotoni/s, durata 3 ps, **monocromatici**

tunabili nel range **20 keV - 1 MeV**.

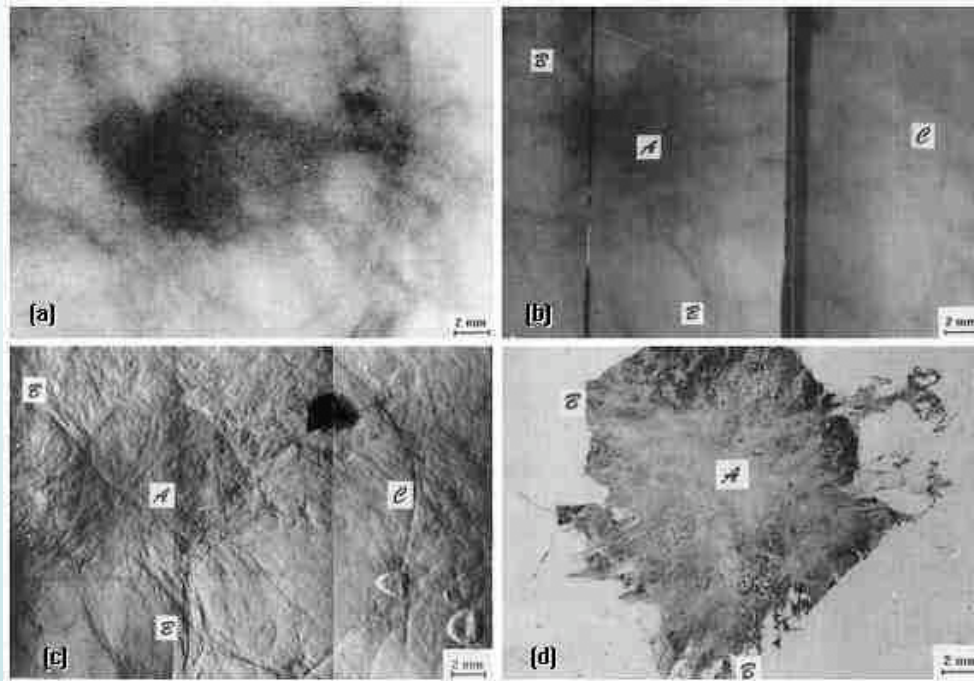
Raggiungimento di **10¹¹ fotoni/s** con spot focali all'interazione di **5 μm**.

- Studi di tecniche di **mammografia** (e **angiografia coronarica**) con X monocromatici.
- Studi di **single molecule protein crystallography**.



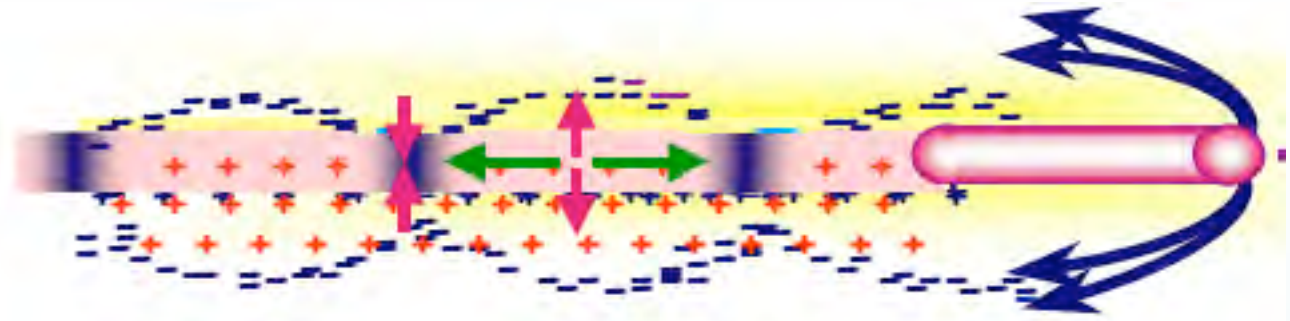
MaMBO Experiment: Mammography Monochromatic Beam Outlook

La realizzazione di una immagine (su superficie 18x24 cm²) in tempi di **2600 s** scende a **2.6 s** con l'upgrade previsto su SPARC che porta il num. di fotoni a $2.5 \cdot 10^{11}$ γ/s



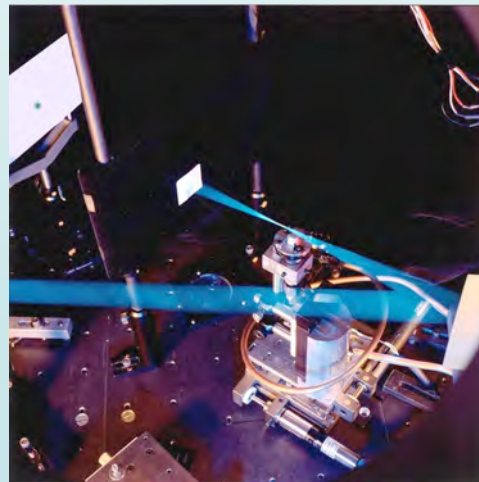
The contrast (sensitivity to tissue density variations) goes from 8% to 0.1%, while the spatial resolution goes from 0,15 -0,3 mm to 0.01-0.015 mm. This means the capability to detect a tumor 30 times smaller in volume, i.e. a 2 year earlier detection of the tumor.

Plasmon



Accelerazione a plasma di pacchetti di elettroni (**25 pC**) da **100 MeV a 130 MeV** con spread energetico $\leq 5\%$, emitt. $\leq 1 \mu\text{m}$, con laser non guidato (5 mm acc. length).
Accelerazione con laser guidato (**5 cm**) fino a 400 MeV, **gradienti $> 5 \text{ GV/m}$** .

$$\varepsilon_n \leq \sqrt{\gamma \frac{\Delta n_p}{n_p} \frac{\lambda_p}{2\pi}}$$

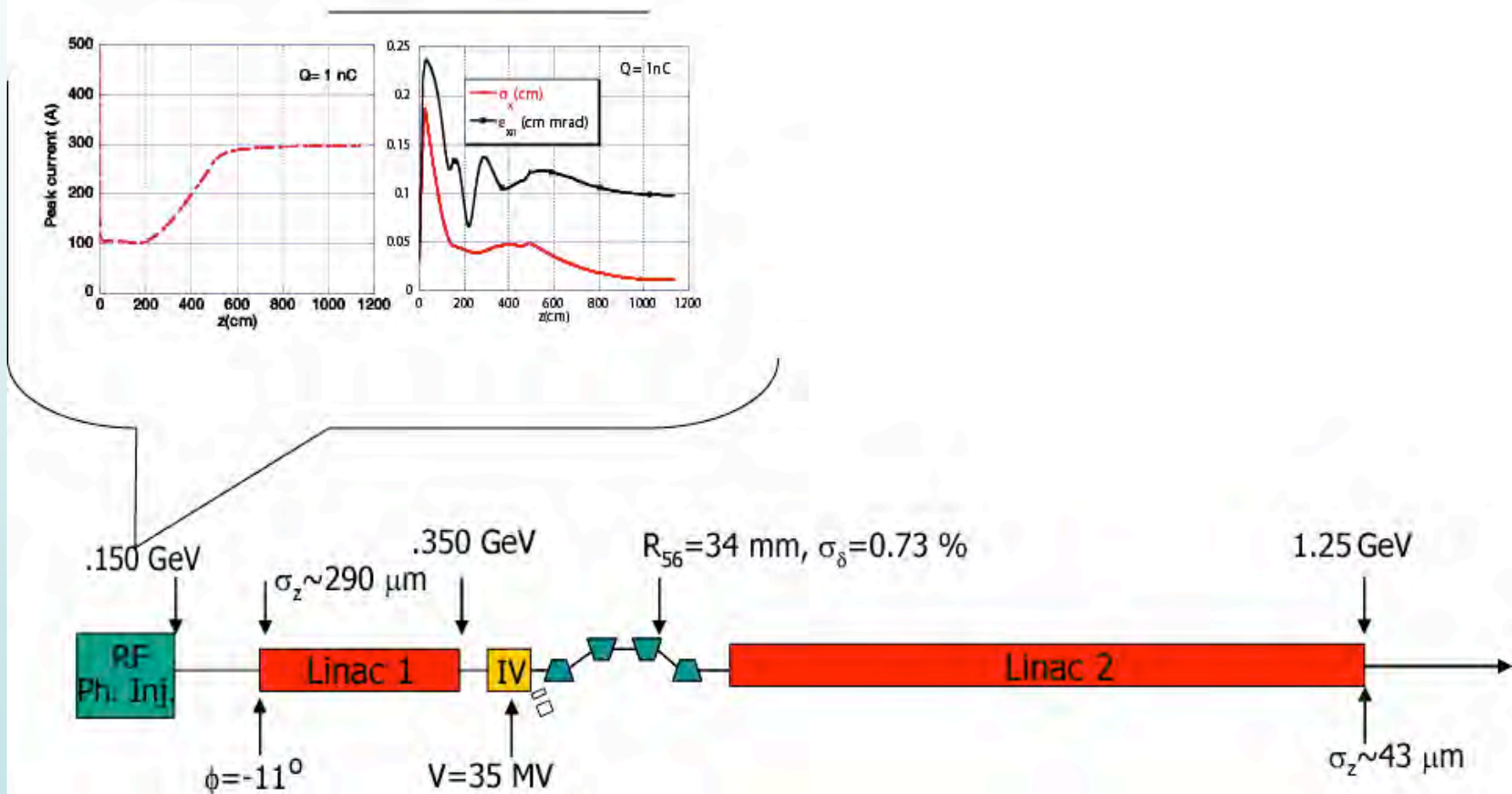


$$\Phi_p \approx 50 \mu\text{m}$$

$$\lambda_p \approx 30 - 100 \mu\text{m}$$

SPARX-ino proposal

SPARC Injector + DAFNE Linac SPARX-ino a 5-10 nm SASE FEL source at LNF



SPARC & SPARX & SPARXINO

- **The SPARC project engineering has been completed**
- **The LINAC is entering, on schedule, the installation phase**
- **First beam delivery in 2006**

- **The SPARX project has been funded**
- **With an up-grade of Dafne Linac the region of a few nm would be achievable.**