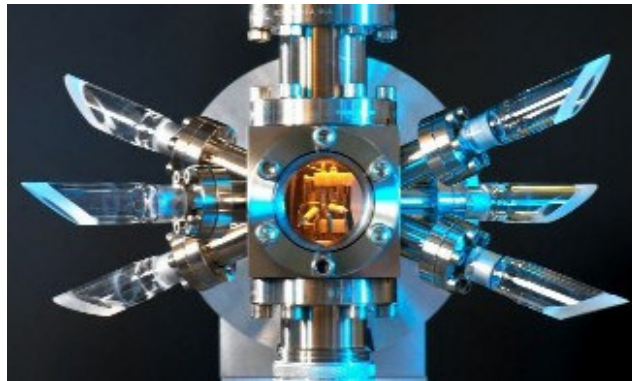


# Opportunities for space-based experiments using optical clock and comb technology



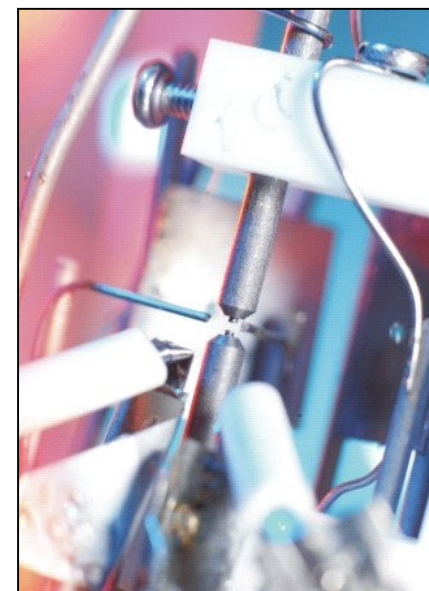
**Patrick Gill**

**National Physical Laboratory, UK**

*Quantum to Cosmos, Virginia, 9<sup>th</sup> July 2008*

# Outline

- Background to ESA studies
- Technology: recent developments & state-of-the-art performance
  - Local oscillators
  - Trapped ion standards
  - Neutral atom standards
  - Femtosecond combs
  - Optical clock comparison
- Opportunities for space missions
- Development plan for optical clocks at suitable technology readiness to move to space qualification



$^{88}\text{Sr}^+$  ion trap (NPL)

# ESA study 2006-07: optical frequency synthesizer for space-borne optical frequency metrology

Patrick Gill, Hugh Klein and Helen Margolis  
National Physical Laboratory



Ronald Holzwarth, Marc Fischer and Theodor Hänsch  
Menlo Systems GmbH



Stephan Schiller  
Heinrich-Heine Universität Düsseldorf



Volker Klein  
Kayser-Threde GmbH (KT)



ESTEC Contract No. 19595/06/NL/PM  
ESA Technical Officer: Eamonn Murphy



# Conclusions & Recommendations:

- Optical frequency combs now mature lab devices
- Ground-based optical clocks specs of  $10^{-17}$  –  $10^{-18}$  available in near future
- Significant advance on microwave frequency best capability
- Opportunities across a range of future space mission sectors



**High precision, high performance clocks,  
Need to work on high reliability for space**

- A substantial ESA-sponsored development programme **to enable optical clock technology to be better prepared for future space missions**
- ESA-steer in the planning of a **future mission based on optical clocks**
- Focus the efforts of leading optical frequency metrology groups and companies **to achieve a space-based optical clock demonstrator within the next decade**

# Development of Optical Atomic Clocks for Space

Patrick Gill, Helen Margolis & Hugh Klein  
National Physical Laboratory

## Remit:

Draw up a viable technology development plan for OACs for space

Timescale: May – September 2008

ESTEC Contract No. 21641/08/NL/PA  
ESA Technical Officer: Eamonn Murphy



# Technology development plan for OACs in space

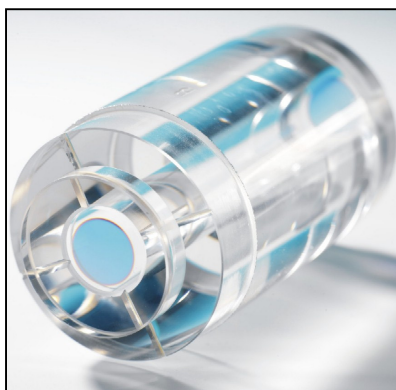
- Pointers to potential future missions and associated user requirements benefiting from OACs
- Aim for a fit between fundamental physics & other subsidiary science mission goals
- Identify necessary parallel development activities to progress OAC sub-unit technologies to TRL 5/6, ideally consistent with next CV timeframe
- Identify a co-ordinated activity plan (with costs) involving the ESA space research community that addresses the following sub-units:
  - Atomic reference (cold atom and single ion options)
  - Optical local oscillator
  - Frequency synthesis
  - Frequency comparison
- Integration of sub-unit development into advanced prototype (by 5 years)
- Identify systems providers and ball-park cost for next stage EM

# Optical Clocks: What and Why?

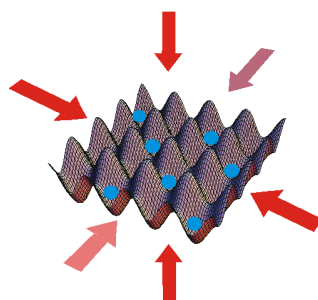
$$\text{instability } \sigma \propto \frac{\Delta f}{f} \frac{1}{(S/N)}$$

- Based on narrow optical transitions in atoms or ions
- Frequencies  $\sim 10^5$  times higher than microwave frequencies
- Q-factor  $\sim 10^{15}$
- Better time resolution
- Better stabilities than microwave clocks

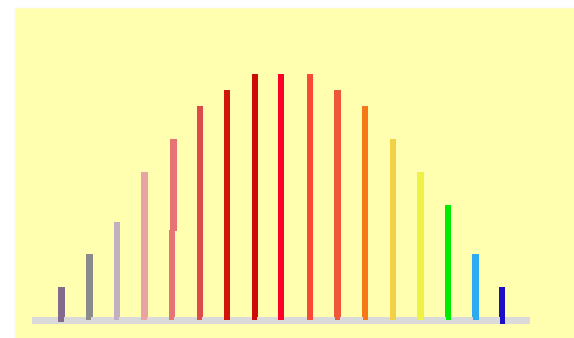
$$\sigma(\tau) \sim \frac{1}{2\pi f \sqrt{NT_{\text{int}} \tau}}$$



Cavity-stabilised  
Oscillator  
(Ultra-stable laser)

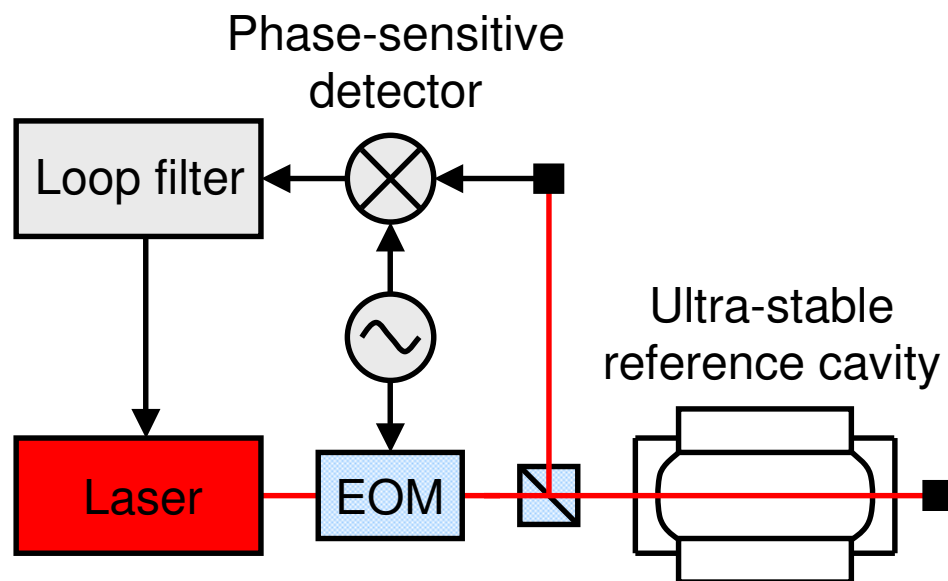


Reference (Narrow optical  
transition in an atom or ion)



Counter  
(Femtosecond comb)

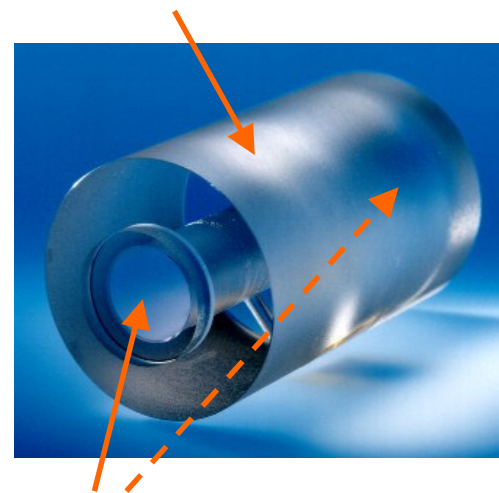
# Optical local oscillators



## Spacer:

Ultra-low-expansion (ULE) glass

Length  $\sim 10$  cm  $\rightarrow$  FSR  $\sim 1.5$  GHz



## Mirrors:

optically contacted to spacer

Refl.  $> 99.998\%$ , finesse  $\sim 200,000$

Cavity must be:

- Operated at a temperature where coefficient of thermal expansion  $\alpha_{\text{CTE}}$  is close to zero;
- Isolated from sources of vibration.

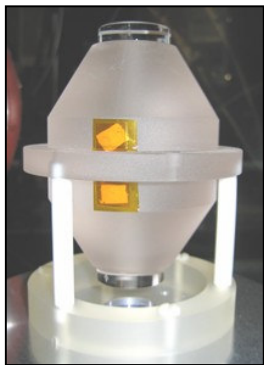


# State-of-the-art LO performance

**Benchmark:** ULE-cavity-stabilized dye laser at NIST  
linewidth  $\sim 0.2$  Hz, rel. frequency instability  $3 \times 10^{-16}$  at 1 s

**Other systems:** Nd:YAG laser  $\sim 0.4$  Hz (NPL, JILA, ...)  
Diode lasers  $\sim 0.4 - 1$  Hz (PTB, NIST, NPL, ...)  
Ti:sapphire  $\sim 5$  Hz (NPL)

## Recent developments: Vibration-insensitive cavities



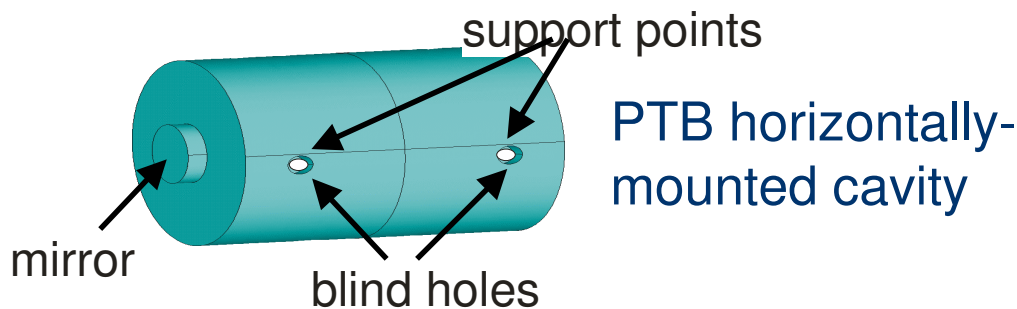
JILA vertical cavity

*Ludlow et al.*  
*Opt. Lett. 32, 641 (2007)*

NPL cut-out cavity



*Webster et al. PRA 75, 011801 (R) (2007)*

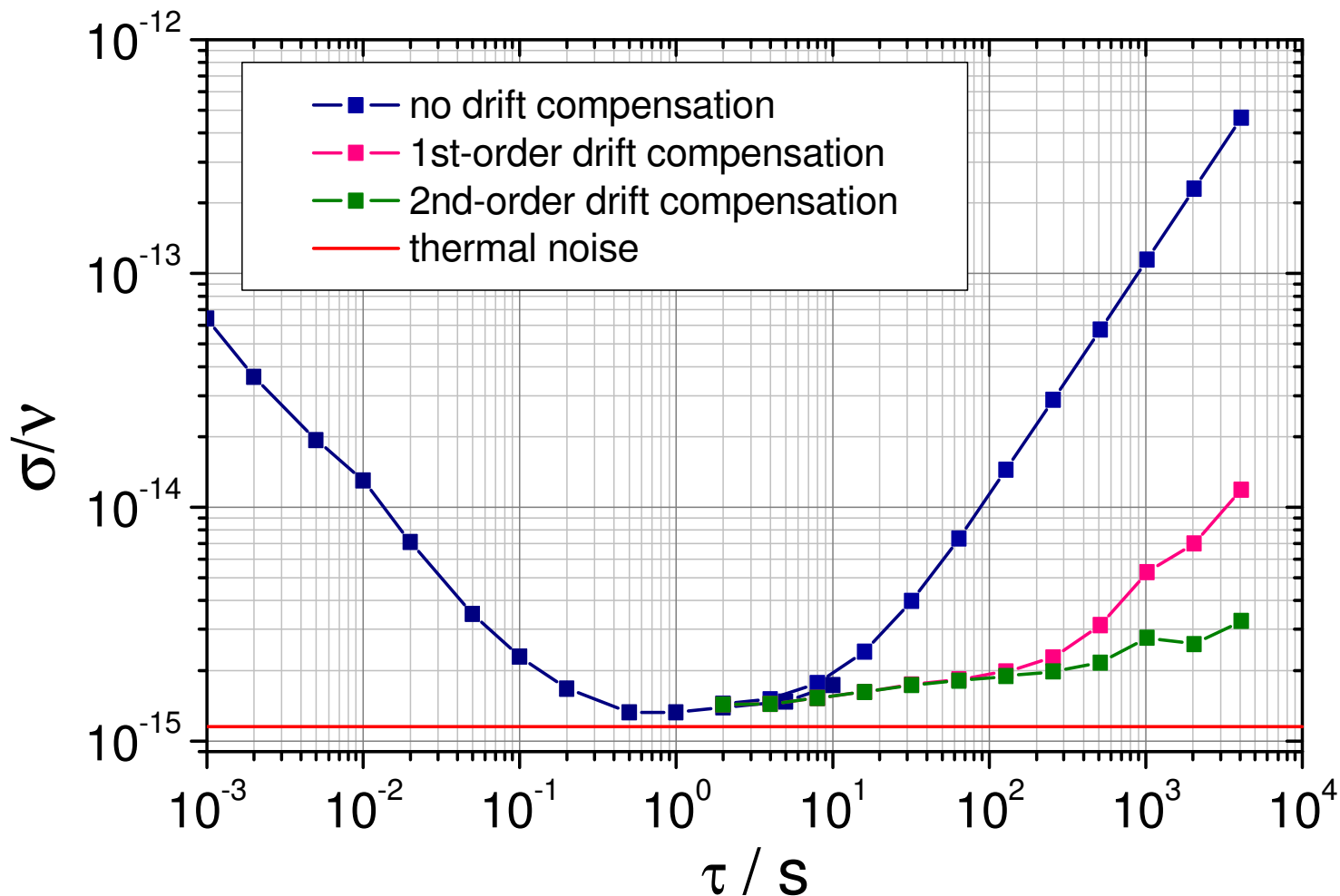


PTB horizontally-mounted cavity

Sensitivity to vertical vibrations  
up to 1000 times lower than  
standard cylindrical cavities

*Nazarova et al., Appl. Phys. B 83, 531 (2006)*

# Thermal noise limit

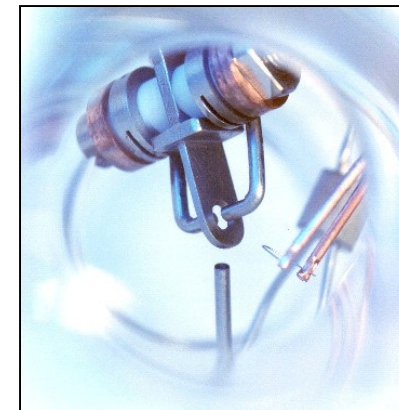


Experiment: Webster *et al.*, PRA 77, 033847 (2008)

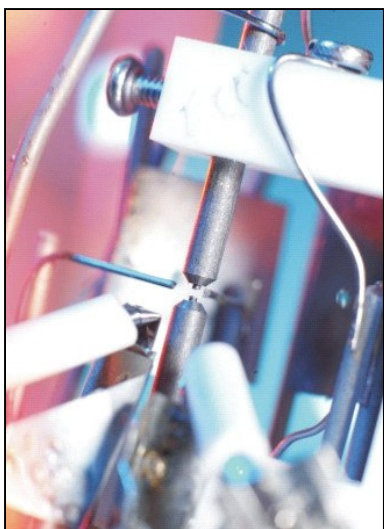
Theory: Numata *et al.*, PRL 93, 250602 (2004)

# Trapped ion optical clocks

- Laser-cooled single trapped ion
- High- $Q$  optical clock transitions ( $10^{15}$  or higher)
- Long interrogation times possible
- Electron shelving scheme → high detection efficiency



$^{171}\text{Yb}^+$  trap (PTB)



$^{88}\text{Sr}^+$  trap (NPL)

Low perturbation environment:

- No 1<sup>st</sup>-order Doppler shift (& minimum 2<sup>nd</sup>-order shift)
- Field perturbations minimised at trap centre
- Background collision rate low

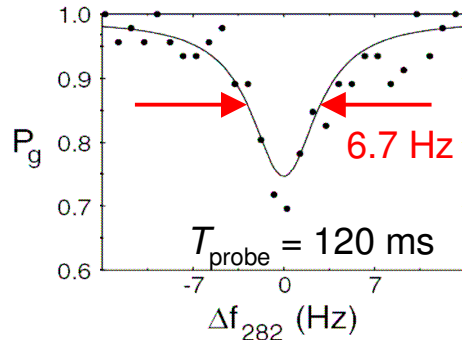


$\text{Ca}^+$  trap (Innsbruck)

# Ion clocks: candidate systems

Ion	Clock transition	$\lambda$ / nm	Natural linewidth / Hz	Best experimental linewidth / Hz	Frequency measurement uncertainty / Hz	Laboratory
$^{199}\text{Hg}^+$	$^2\text{S}_{1/2} - ^2\text{D}_{5/2}$	282	1.8	6.7	0.7	NIST
$^{171}\text{Yb}^+$	$^2\text{S}_{1/2} - ^2\text{D}_{3/2}$	436	3.1	10	2.2	PTB, NPL
$^{88}\text{Sr}^+$	$^2\text{S}_{1/2} - ^2\text{D}_{5/2}$	674	0.4	5	1.7	NPL, NRC
$^{40}\text{Ca}^+$	$^2\text{S}_{1/2} - ^2\text{D}_{5/2}$	729	0.14	15	0.9	Innsbruck, CRL, Marseilles
$^{115}\text{In}^+$	$^1\text{S}_0 - ^3\text{P}_0$	237	0.8	170	230	MPQ / Erlangen
$^{27}\text{Al}^+$	$^1\text{S}_0 - ^3\text{P}_0$	266	$8 \times 10^{-3}$	8.4	0.7	NIST
$^{171}\text{Yb}^+$	$^2\text{S}_{1/2} - ^2\text{F}_{7/2}$	467	$\sim 10^{-9}$	40	11	NPL, PTB

# Ion clocks: observed Q-factors & absolute frequency measurements



## **$^{199}\text{Hg}^+$ standard:**

observed  $Q \approx 1.6 \times 10^{14}$  *Rafac et al., PRL 85, 2462 (2000)*

$f = 1\,064\,721\,609\,899\,145.30(69)$  Hz

(rel uncertainty  $6.5 \times 10^{-16}$ )

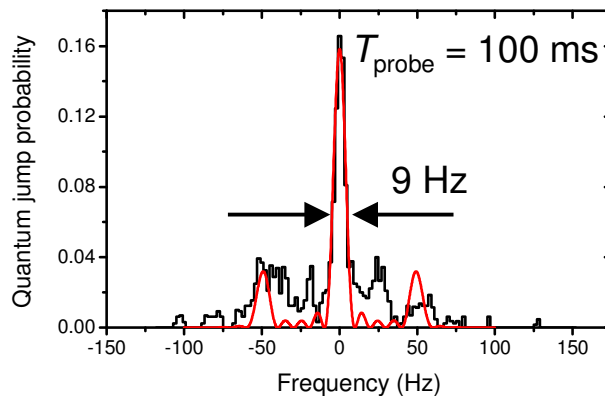
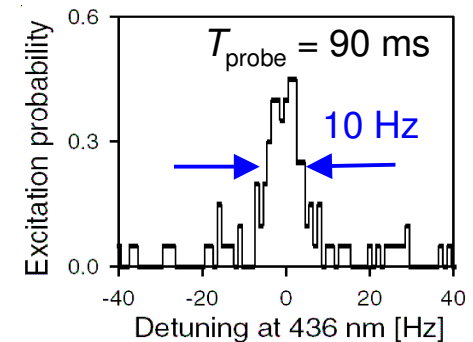
*Stalnaker et al., Appl. Phys. B 89, 167 (2007)*

## **$^{171}\text{Yb}^+$ quadrupole standard:**

observed  $Q \approx 7 \times 10^{13}$  *Peik et al., PRL 93, 170801 (2004)*

$f = 688\,358\,979\,309\,307.6$  (2.2) Hz

(rel uncertainty  $3.2 \times 10^{-15}$ ) *Tamm et al., IEEE TIM. 56, 601 (2007)*



## **$^{88}\text{Sr}^+$ standard:**

observed  $Q \approx 5 \times 10^{13}$  *Barwood et al, IEEE TIM. 56, 226 (2007)*

$f = 444\,779\,044\,095\,484.2$  (1.7) Hz

(rel uncertainty  $3.8 \times 10^{-15}$ )

*Margolis et al., Science 306, 1355 (2004)*

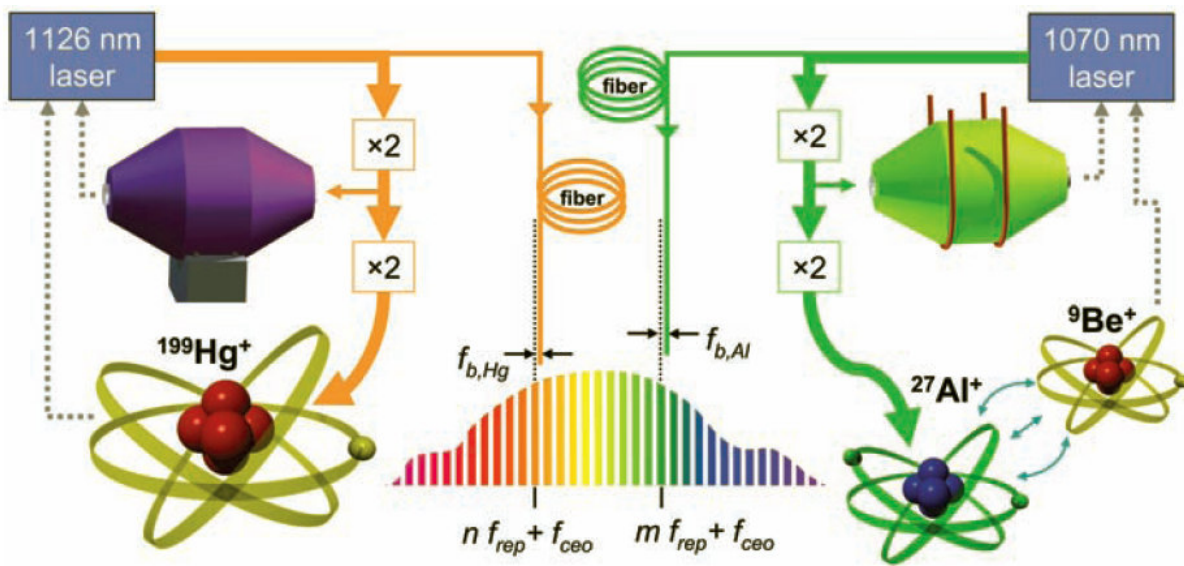
# Ion clocks: frequency ratio measurements

Optical frequency **ratios** can be measured much more accurately.

$$\frac{f_{\text{Al}^+}}{f_{\text{Hg}^+}} = 1.052\,871\,833\,148\,990\,438\,(55)$$

Relative uncertainty  $5.2 \times 10^{-17}$

- $4.3 \times 10^{-17}$  statistics
- $1.9 \times 10^{-17}$  Hg<sup>+</sup> systematics
- $2.3 \times 10^{-17}$  Al<sup>+</sup> systematics

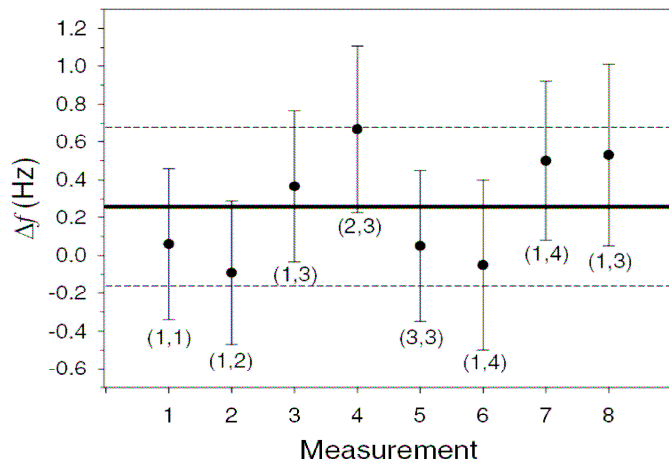
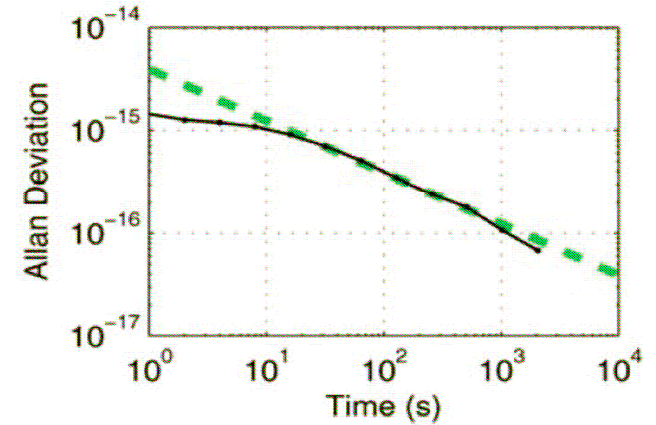


Rosenband *et al.*,  
Science 319, 1808 (2008)

# Ion clocks: stability and reproducibility

Comparison of  $^{199}\text{Hg}^+$  and  $^{27}\text{Al}^+$  standards:  
 instability  $4 \times 10^{-15} \tau^{-1/2}$  for  $20 \text{ s} \leq \tau \leq 2\,000 \text{ s}$

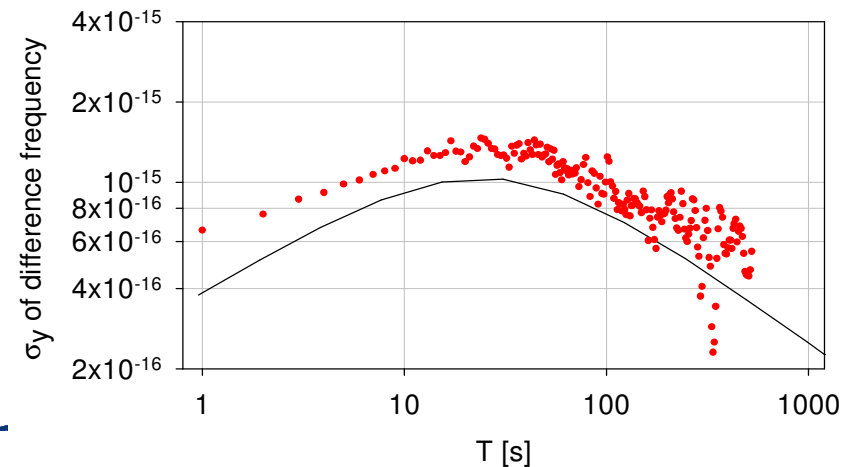
Rosenband *et al.*, Science 319, 1808 (2008)



Peik *et al.*, J. Phys. B: At.Mol.Opt. Phys 39,145 (2006)

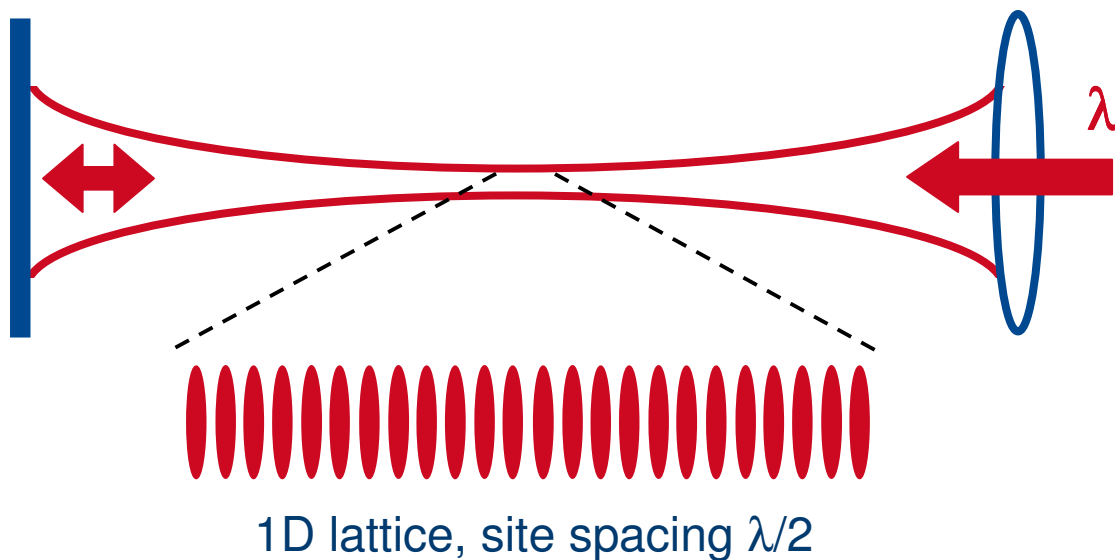
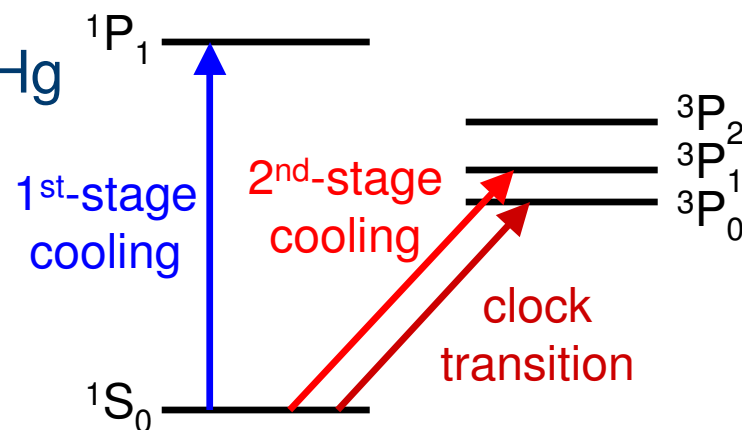
Comparison of two  $^{171}\text{Yb}^+$  standards:  
 fractional frequency difference  $3.8(6.1) \times 10^{-16}$

Schneider *et al.*, Phys. Rev. Lett. 94, 230801 (2005)



# Neutral atom lattice clocks

- $^1S_0 - ^3P_0$  clock transitions in eg Sr, Yb, Hg (mHz natural linewidth)
- Atoms confined in an optical lattice
- AC Stark shift eliminated by operating at “magic” wavelength
- $N$  atoms, stability  $\propto N^{1/2}$
- Ultimate goal: 3D lattice with 1 atom per site





# Lattice clocks: absolute frequency measurements

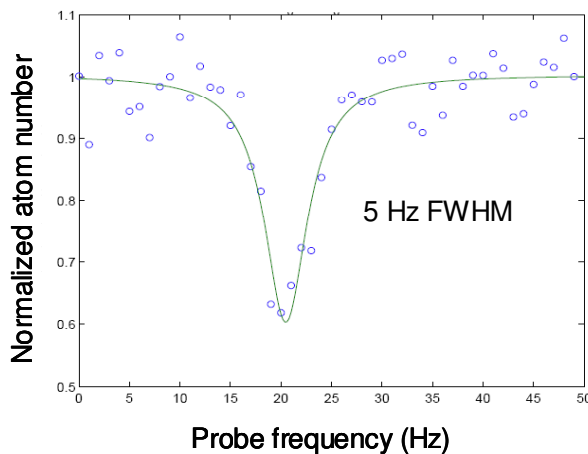
$^{87}\text{Sr}$  standard:

- Highest observed optical Q-factor ( $2 \times 10^{14}$ )
- Independent measurements from 3 groups now agree at the  $10^{-15}$  level
- Secondary representation of the second

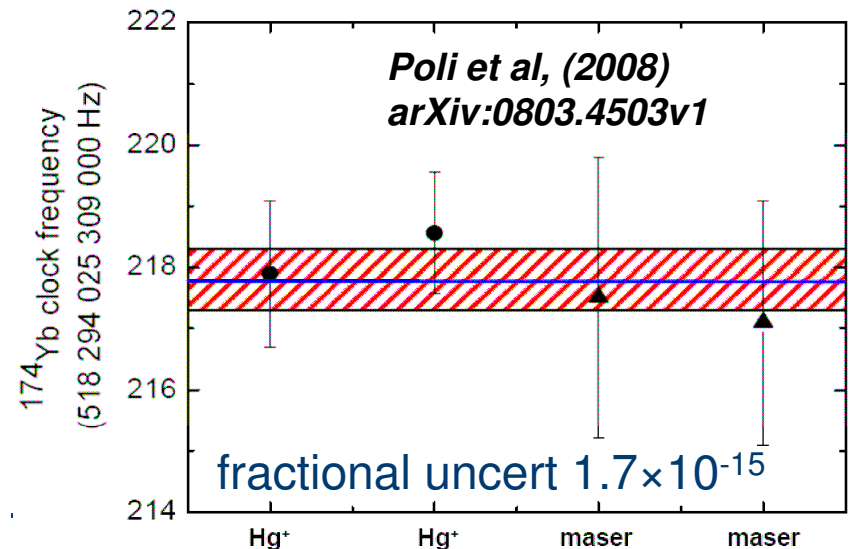
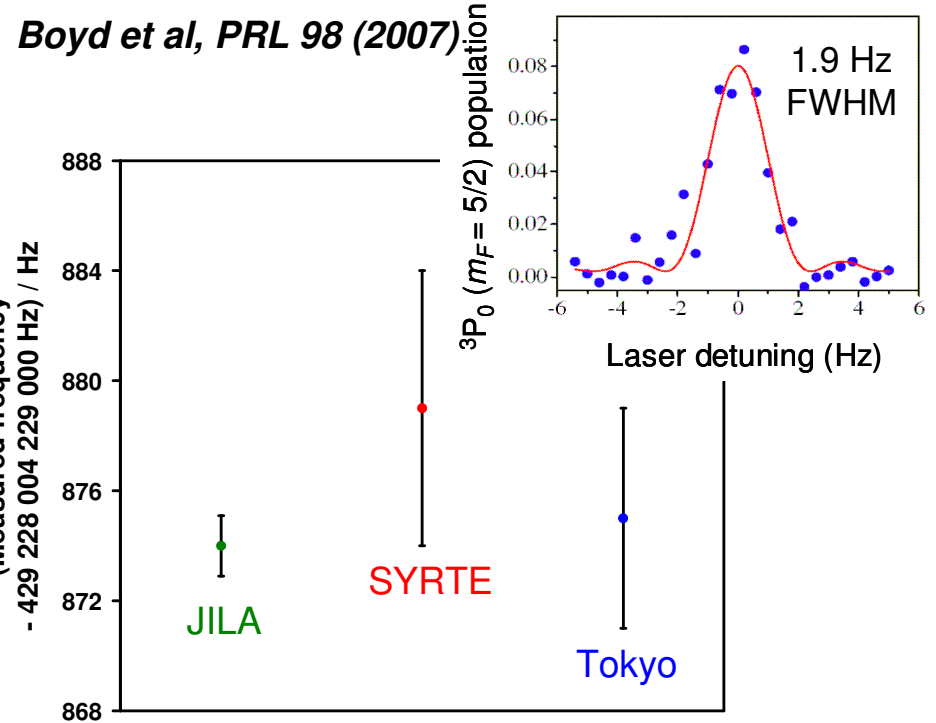
$^{174}\text{Yb}$  standard:

- observed  $Q \sim 1 \times 10^{14}$

*Barber et al, Proc. SPIE 6673, (2007)*



Both Qs limited by spectroscopic probe times

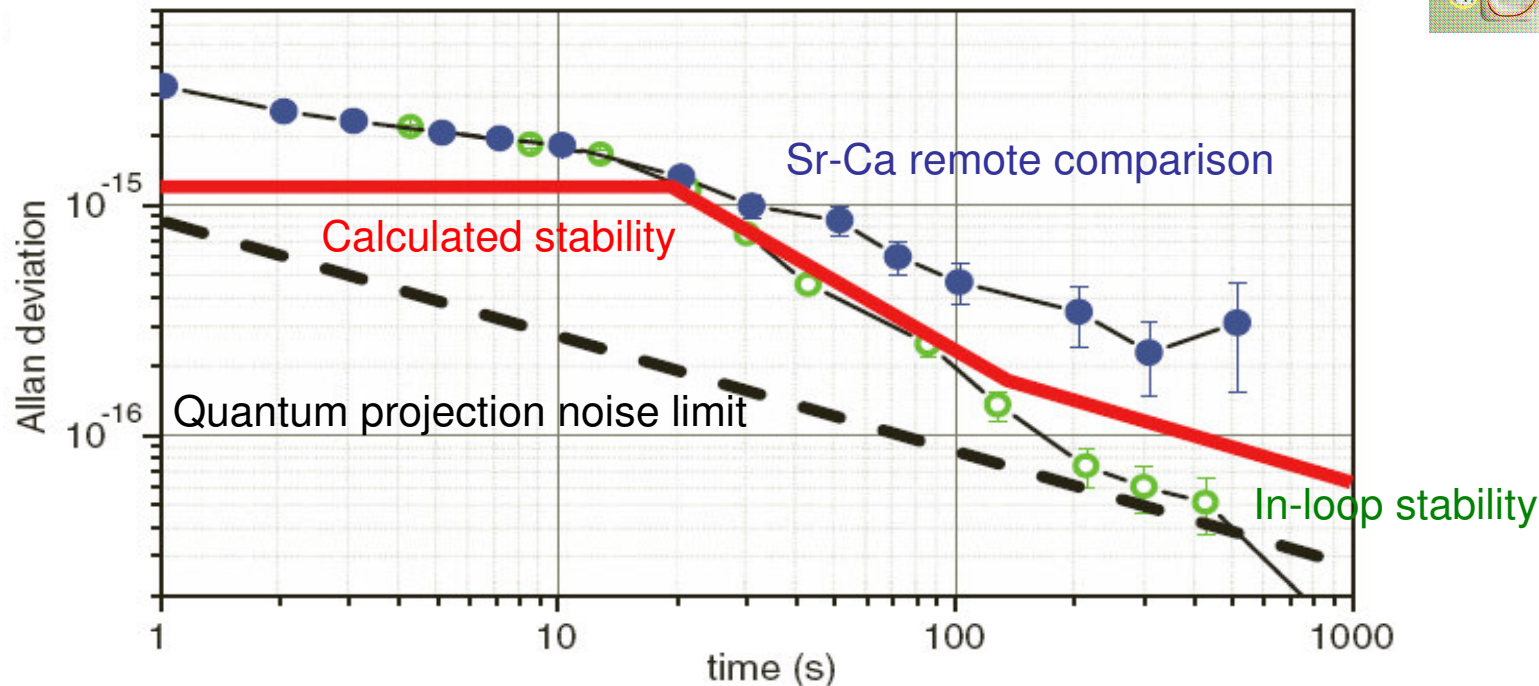
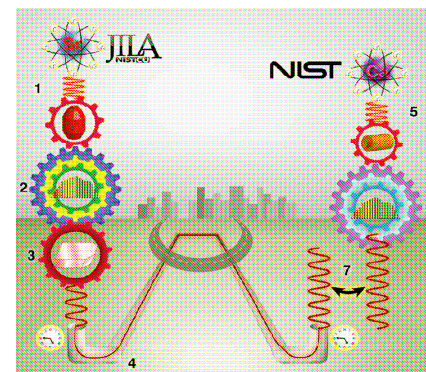


# Lattice clocks: systematic uncertainty & stability

$^{87}\text{Sr}$  standard:

Fractional frequency uncertainty of  $10^{-16}$  demonstrated by remote optical comparison with a Ca standard.

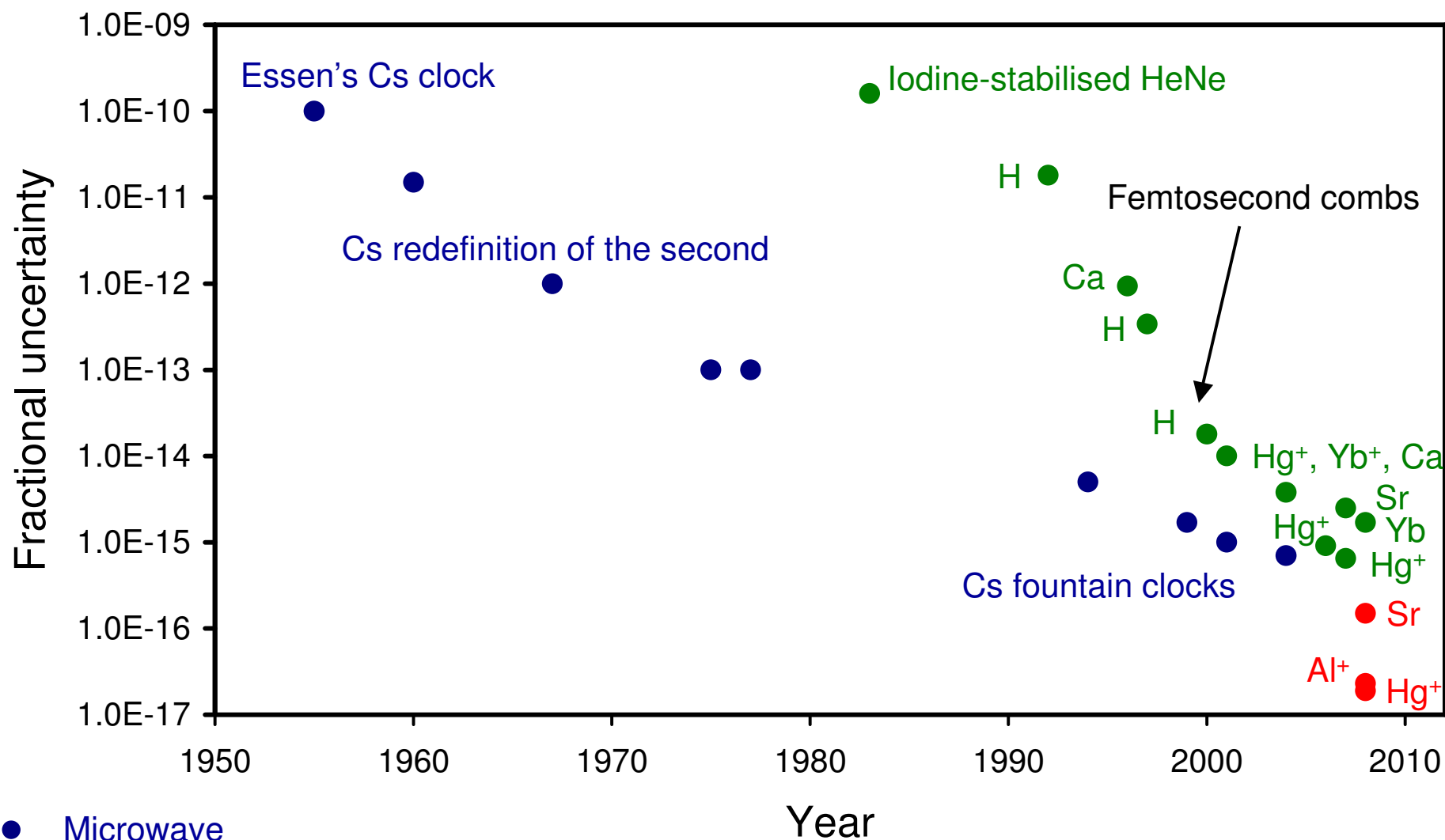
*Ludlow et al., Science 319, 1805 (2008)*



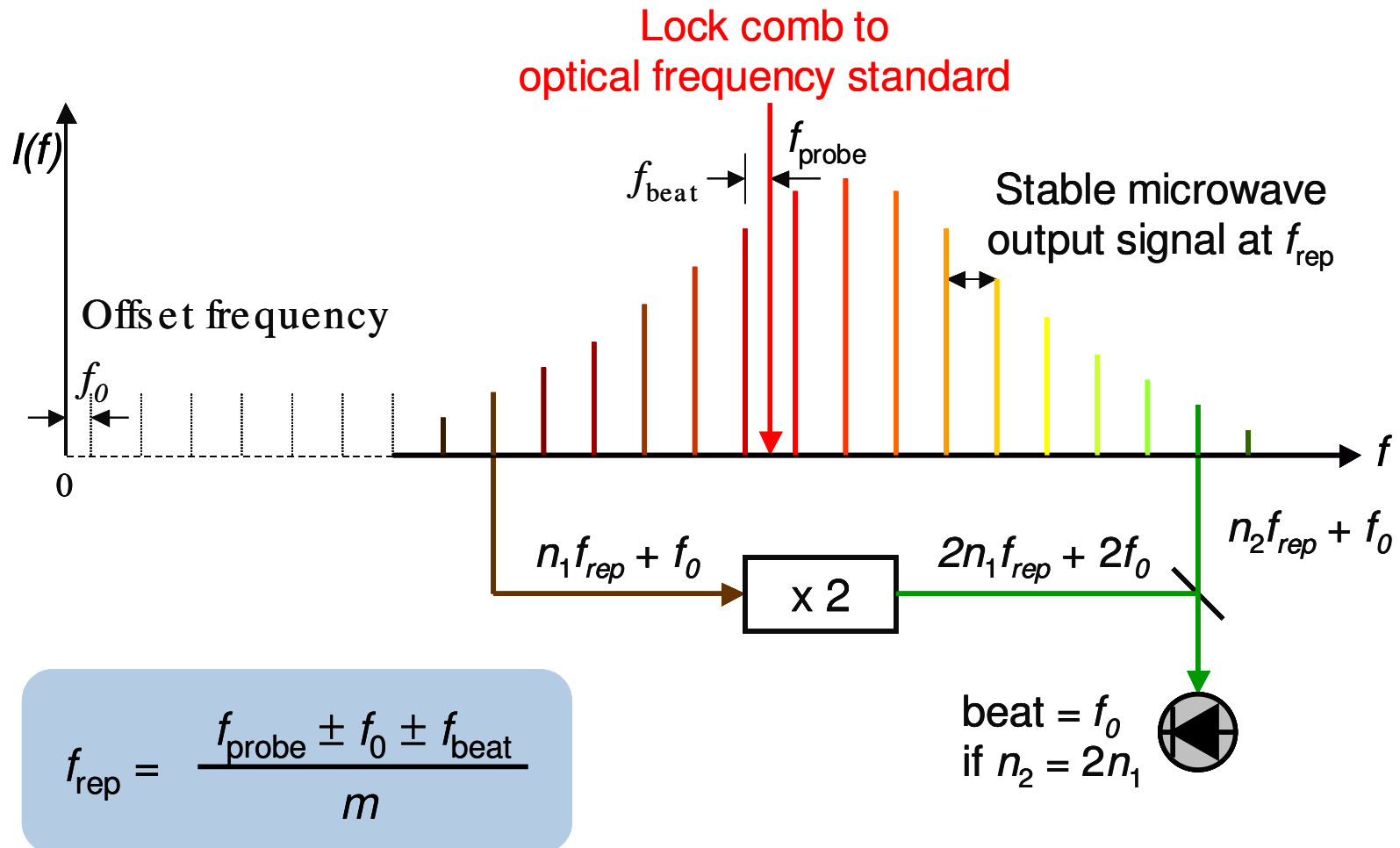
Similar stability demonstrated for  $^{174}\text{Yb}$  (v.  $\text{Hg}^+$ )

*Poli et al., arXiv:0803.4503v1 (2008)*

# Improvements in optical frequency standards



# Femtosecond combs: optical clock operation

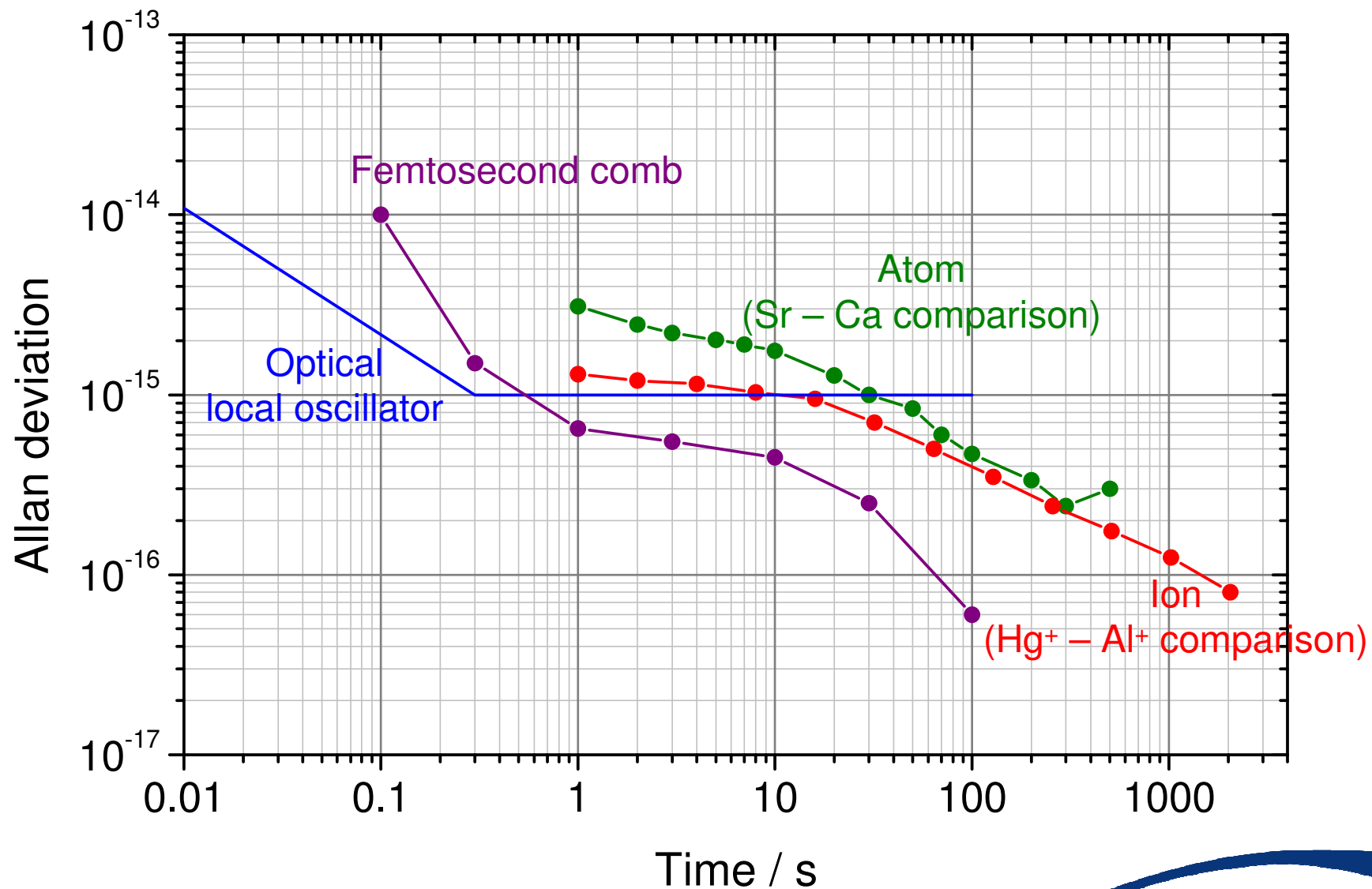


→ millions of modes across visible/IR with known frequency

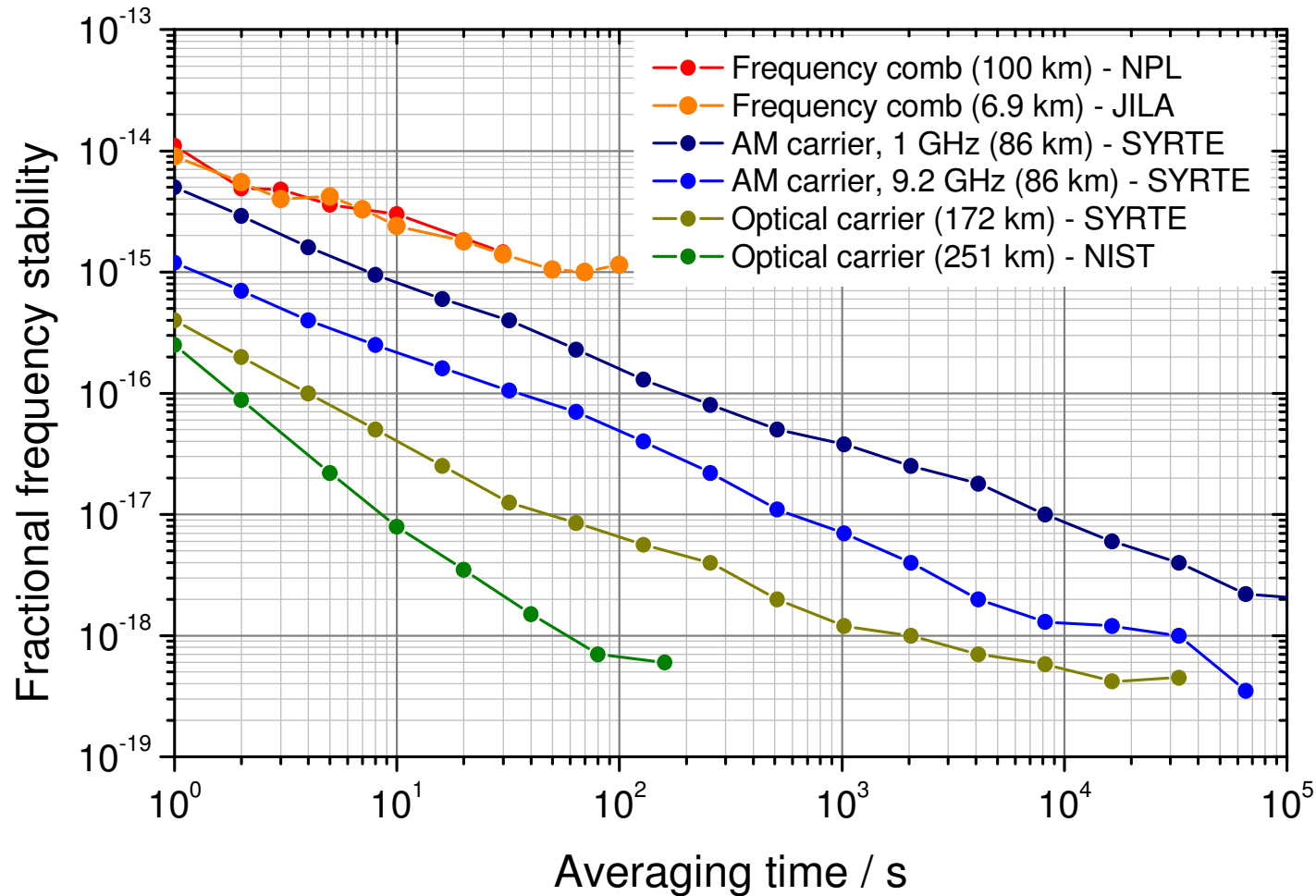
- Uncertainty between combs locked to the same optical ref:  $\sim 1.4 \times 10^{-19}$  (Ma et al, Science 2004)

— • Comb hardware: fs laser (eg TiS, Fibre laser ....) + microstructure fibre

# Overall system performance



# Optical clock comparison by fibre: state of the art



Compare frequency transfer by fibre with satellite MWL between high performance remote clocks to validate MWL for transportable ground clocks

# Opportunities for OAC space missions in fundamental physics

Development of quantum theory of gravity implies violations of standard General Relativity principles such as the Einstein Equivalence Principle:

GR effects small, but space environment offers variable gravity, large distances, high velocities and low accelerations and freedom from Earth seismic noise. Optical clocks most sensitive to gravitational effect through effect on frequency

## Tests of Local Position Invariance (LPI)

- Absolute gravitational redshift (GRS) measurements due to  $\Delta U/c^2$  orbit change in Earth potential
- Absolute GRS measurements of solar potential
- Null GRS tests between dissimilar clocks in changing potential

$$\frac{\nu_1 - \nu_2}{\nu} = \frac{U(r_1) - U(r_2)}{c^2}$$

$$\frac{\nu_A}{\nu_B} = \text{const.}$$

## Tests of Local Lorentz Invariance (LLI)

- Test of time dilation between ground & space clock (Ives-Stilwell)
- Cavity / OAC freq comparison in orbiting arrangement (Kennedy-Thorndike)

Measurement of space-time curvature  
(Shapiro time delay)

# EGE (Einstein Gravity Explorer)

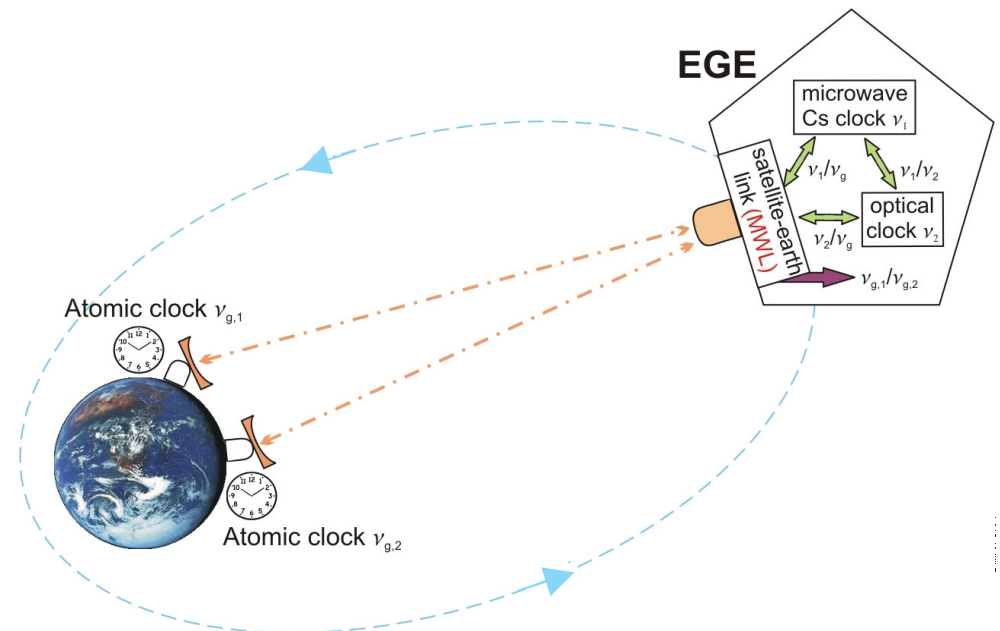
Class M Cosmic  
Vision proposal:  
Schiller, Tino, Gill,  
Salomon *et al.* (2007)

## Scientific goals:

- Tests of fundamental physics (gravitation)  
(Gravitational redshift, variation of fundamental constants,  
Lorentz invariance + + + +)
- Spin-off to other fields  
(Determination of earth's geopotential, comparison of distant terrestrial  
clocks at the  $10^{-18}$  level, technology demonstration)

## Payload:

- Two atomic clocks  
(one optical, one microwave)
- Optical frequency comb
- Microwave link to earth

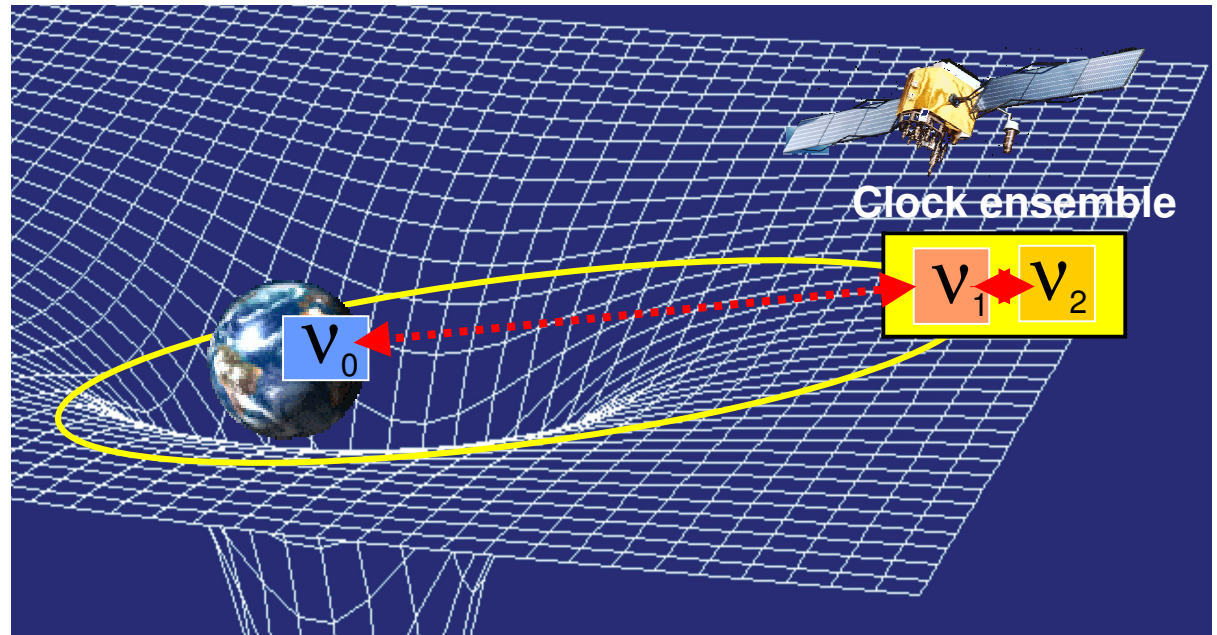




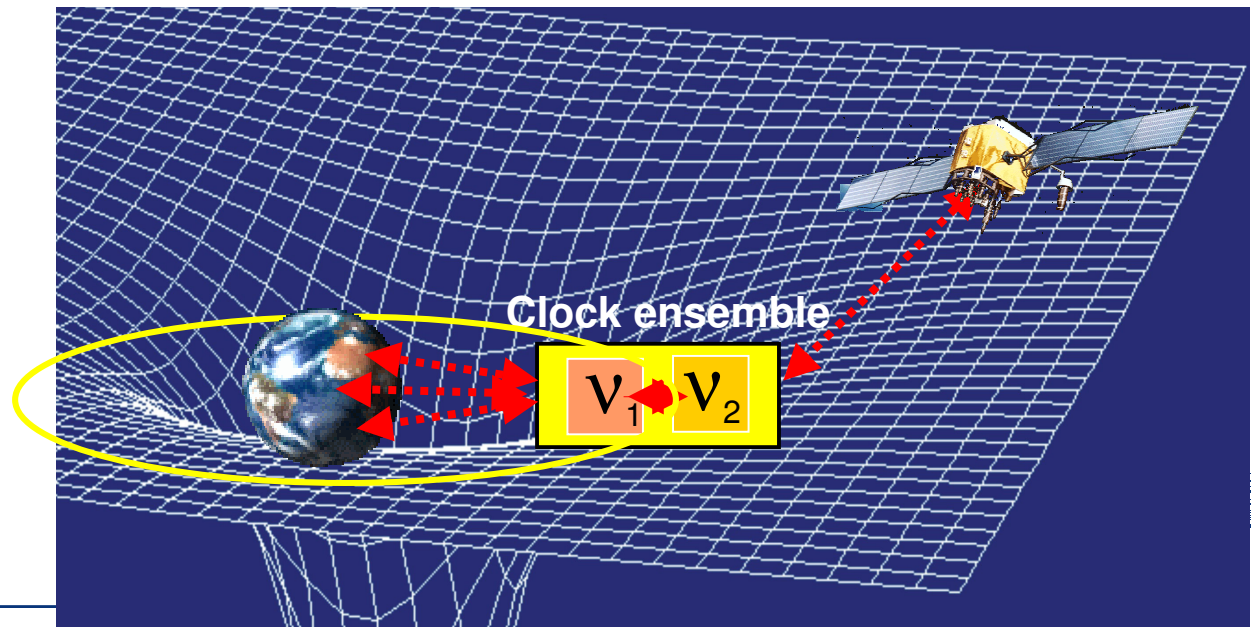
# Possible EGE Mission Scenario

Schiller 2007

- Orbital phase I  
(~ 1 year duration, highly elliptic orbit)
  - Test of Local Position Invariance and of grav. redshift



- Orbital phase II  
(geostationary, several years duration)
  - Master clock for earth and space users
  - Geophysics



# SAGAS (Search for Anomalous Gravitation using Atomic Sensors)

Class L Cosmic Vision proposal:  
Wolf *et al.* (2007)

Scientific goals:

- Tests of fundamental physics (gravitation) in deep space (universality of gravitational redshift, local position invariance, parameterised post-Newtonian gravity, Pioneer anomaly, low frequency gravitational waves, variation of fundamental constants)
- Exploring the outer solar system (Kuiper belt mass distribution and total mass, planetary gravitational constant for Jupiter)

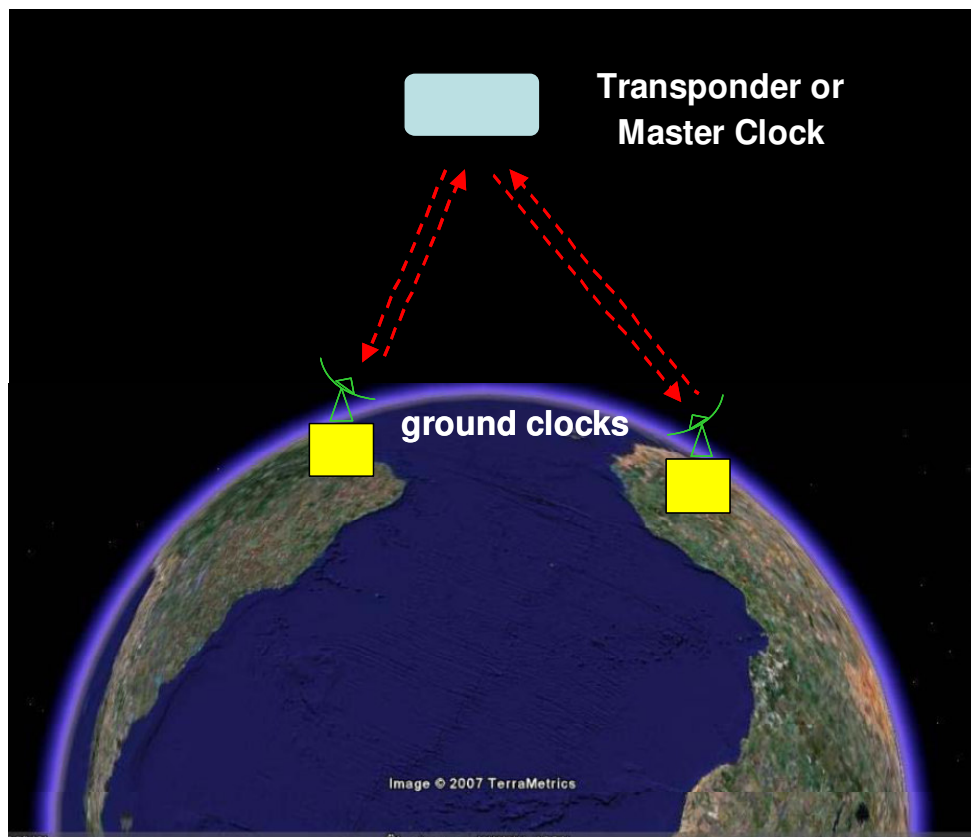
Payload:

- Trapped ion optical frequency standard
- Cold atom accelerometer
- Laser link for ranging, communication & frequency comparison

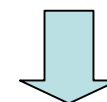


# OAC benefits for Geoscience

Direct measurement of the earth's geopotential with high resolution by using the gravitational redshift.



Comparison of ground clocks  
with  $10^{-18}$  accuracy



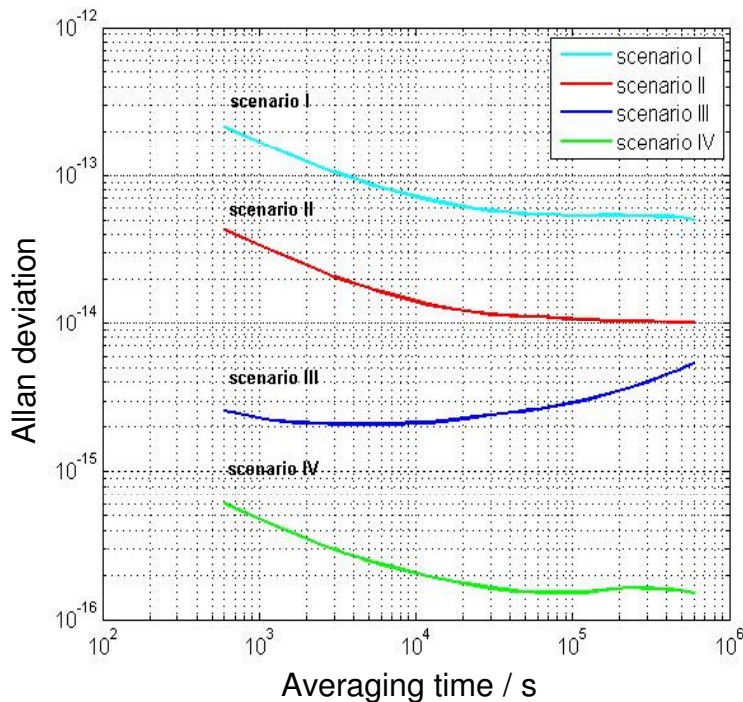
Measurement of potential  
differences with equivalent  
height resolution of 1 cm

Use of airborne clocks  
referenced to master should  
allow improved spatial resolution  
& faster data acquisition

# Navigation: optical clocks for future GNSS

Benefits of using optical clocks in both satellite & ground segments:

- Improved timing / location resolution
- Improved integrity / autonomy of satellite segment
- Better correction for atmospheric and multi-path effects
- Improved time transfer



Scenario	Satellite time	System time	Theoretical error over 2 hours / ns
I	Rubidium clock	Optical clock	0.59
II	Passive maser	Optical clock	0.11
III	Optical clock	Active maser	0.14
IV	Optical clock	Optical clock	0.002

Simulations by Institute of Communications & Navigation (DLR)

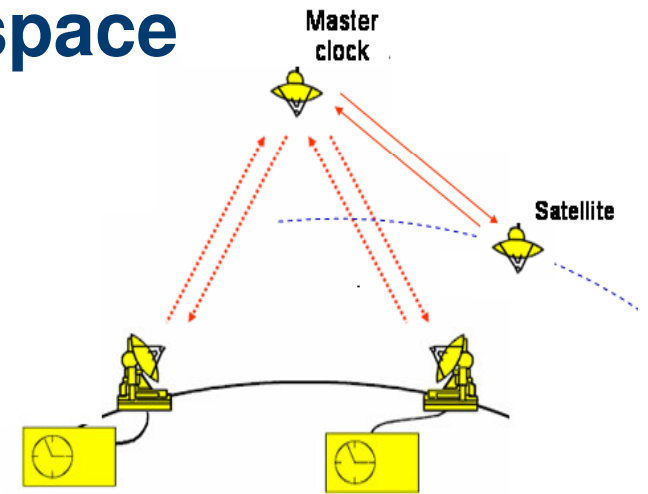
ESA study contract 19837/06/F/VS





# Optical “master” clock (OMC) in space

- Requirement for high accuracy ( $10^{-18}$  level) intercomparison of remote ground-based optical clocks
- ACES MWL target to approach  $10^{-17}$  @ several days takes time
- Common-view comparison via optical master clock
- Geostationary orbit for ease of orbit determination and reduction of tracking requirements
- Altitude determination of master clock to 40 cm required for  $10^{-18}$  accuracy (laser ranging sufficient)
- Also available as a clock reference for satellites in lower orbits



## OAC mission blueprint:

Primary goal

→ Fundamental physics (Tests of GR eg EGE)

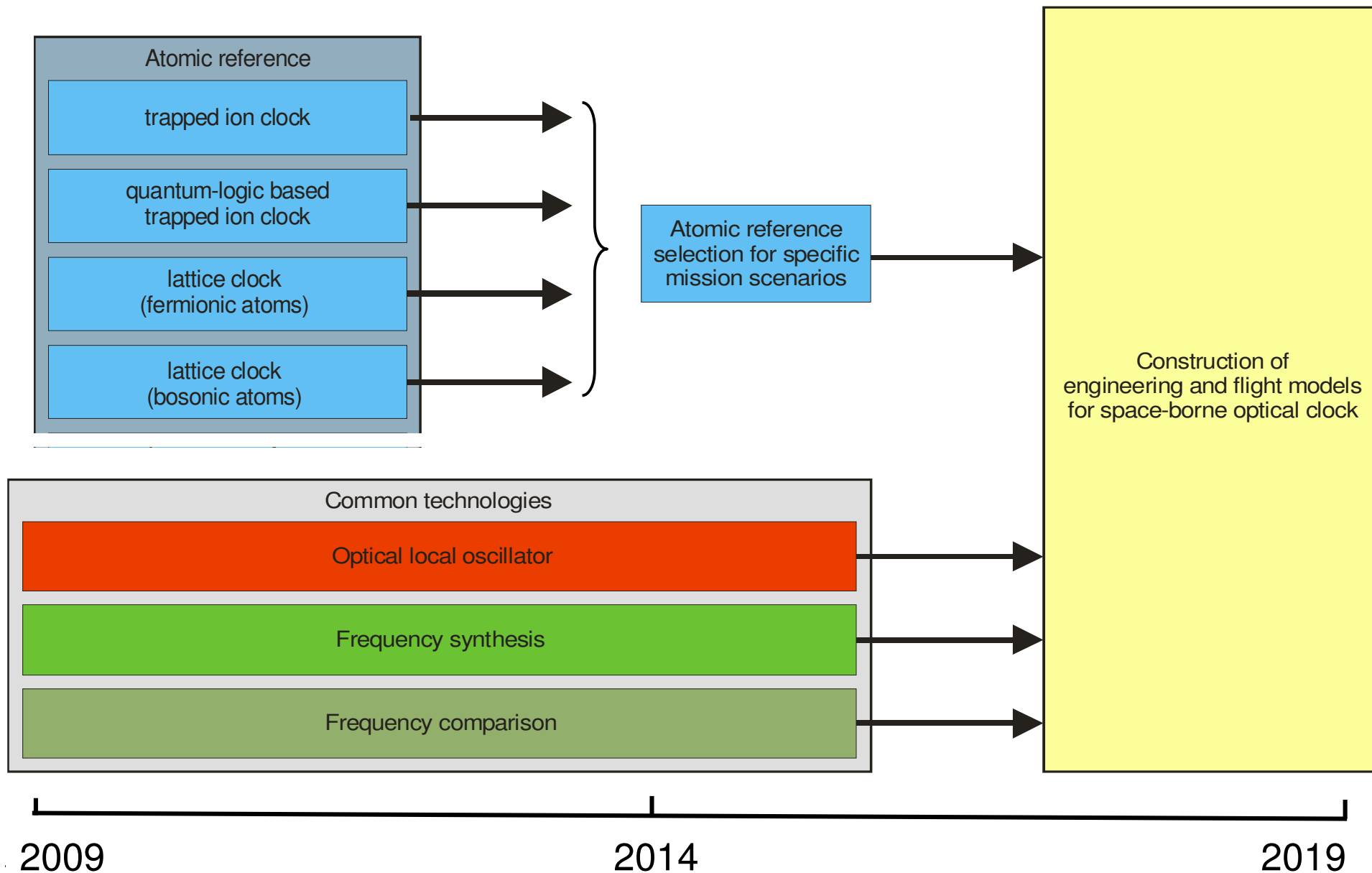
2<sup>nd</sup>ary goals

→ Geoscience (high spatial resn of geopotential)

→ GNSS (input to future GNSS architectures)

→ Optical master clock (high acc remote clock comparison)

# Optical clock parallel-path technology development to reach TRL 5/6 by next CV call + 3 years



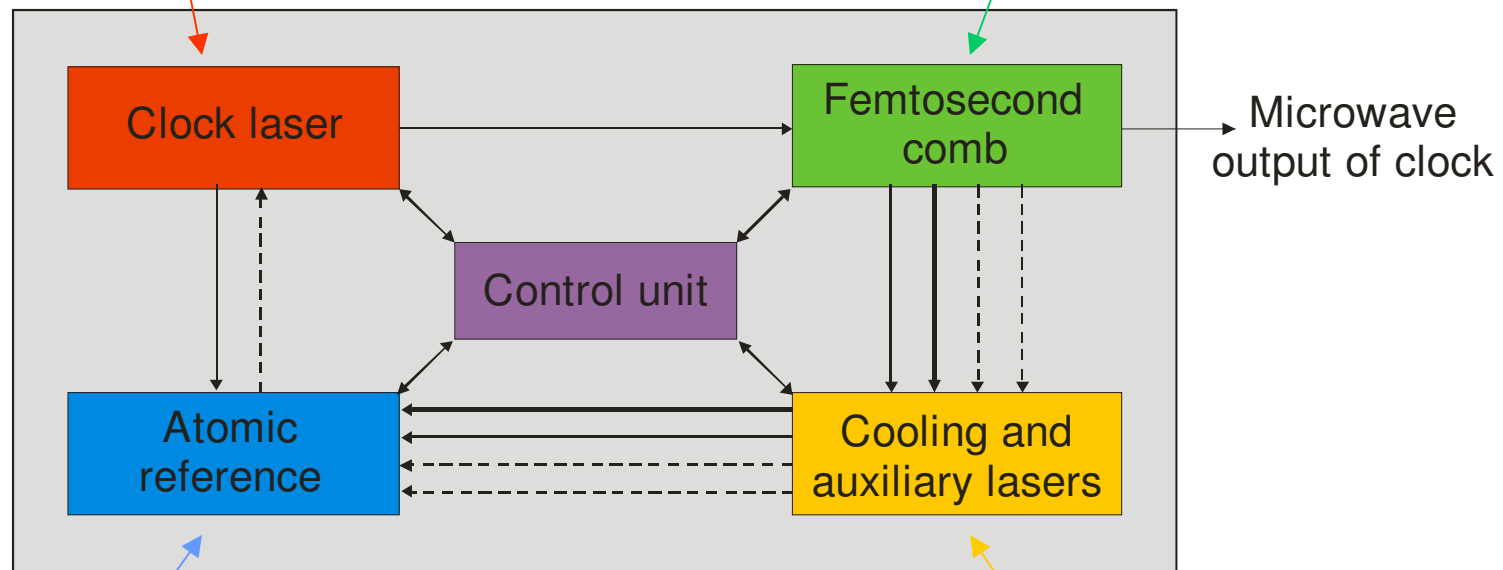
## Benefits of a parallel track development

- Choice of particular clock may be mission dependent
- Better readiness for future Cosmic Vision calls
- Reduced time and improved efficiency to reach EM /FM
- Continuous improvement, benefiting technology development needed for missions
- Common technical sub-packages capable of wide application
- Spin-off to high profile ground-based science  
(eg time variation of fine structure constant;  $m_e/m_p$ )

# Optical clock sub-unit technology requirements

Vibration-insensitive ULE cavity with reduced thermal noise & operating at zero expansivity temperature

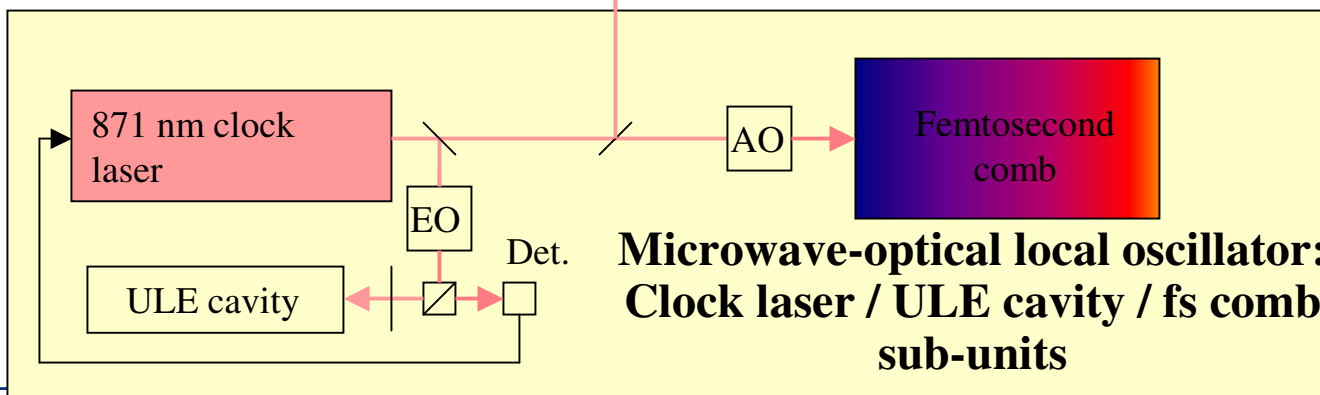
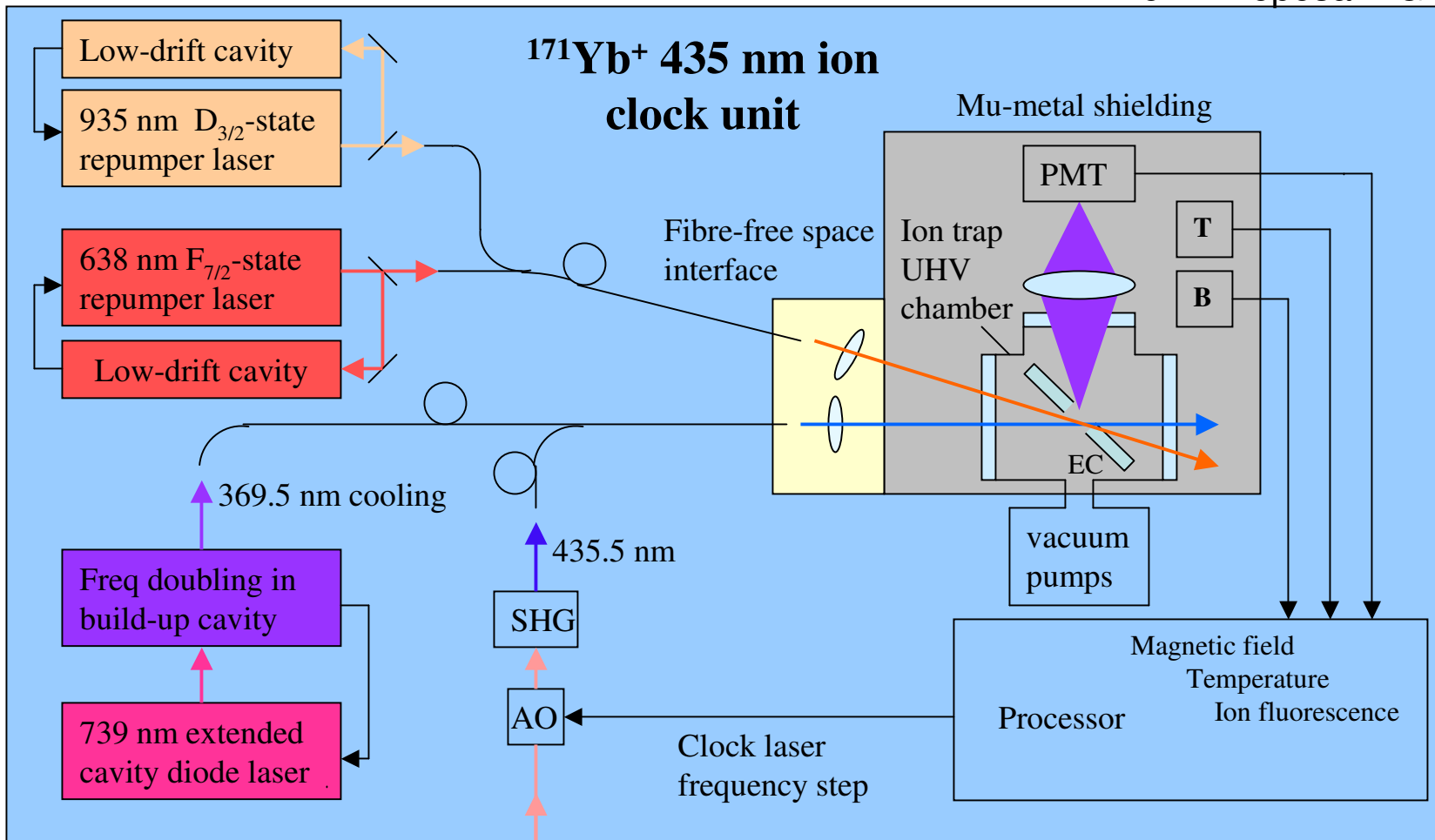
Automated fibre laser fs comb with optical pumping redundancy & radiation hard



Good magnetic field control + shielding;  
Reduced blackbody sensitivity + shielding

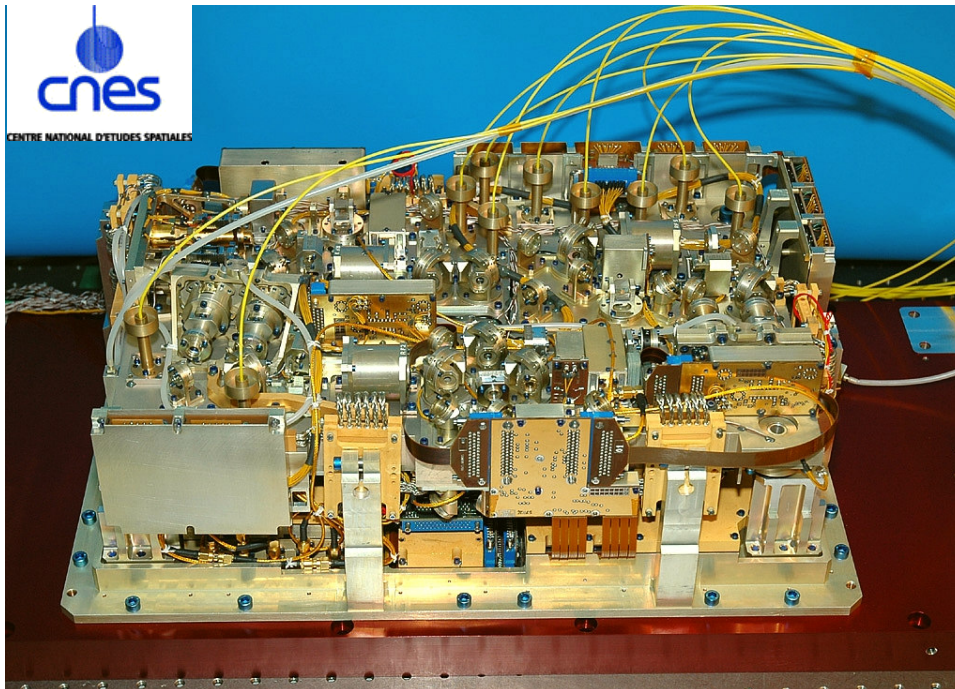
Monolithic DFB or fibre lasers + redundancy and fibre delivery to atom / ion





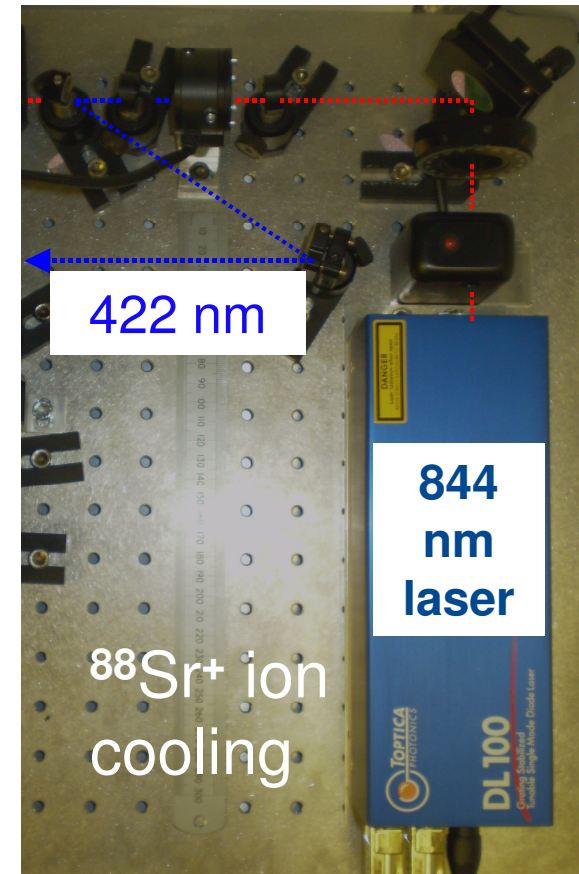
# Laser cooling package

cf ACES development:  
20 kg, 36 W, 30 liters  
Air/vac operation, 10-35 °C



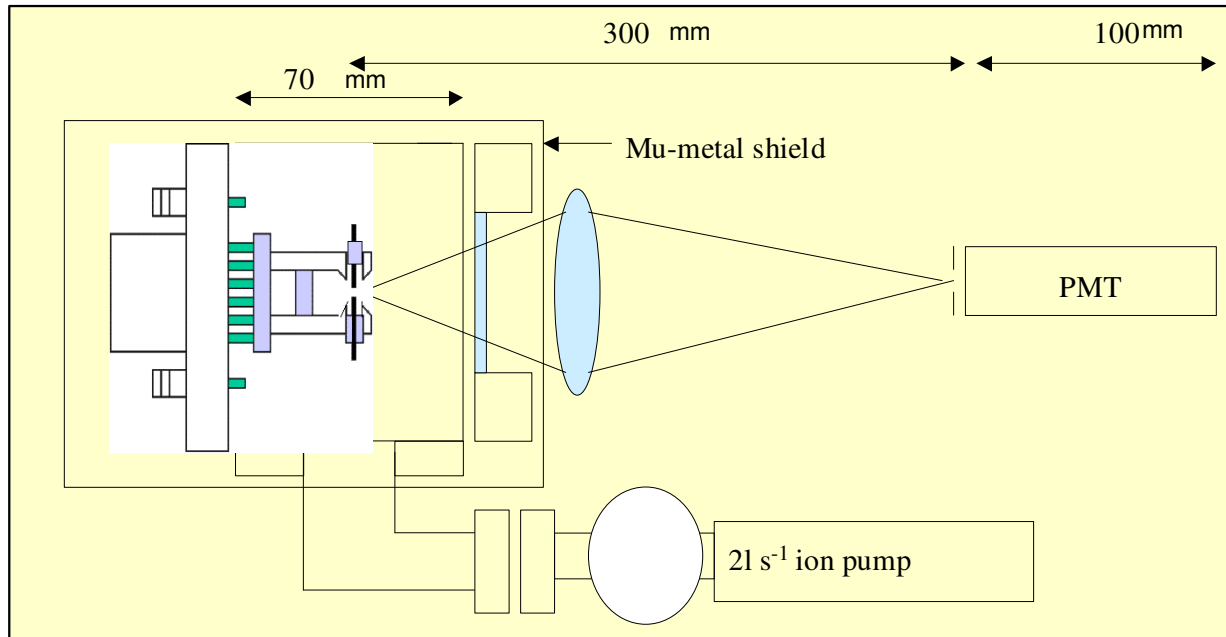
4 ECDL, 4 DL, 6 AOM, 30 PZT  
11 motors, 6 photodiodes  
8 peltier coolers

Potential for reduced package  
for ion clock: eg 1 ECDL +  
single pass doubling + aux  
DFBs + redundancy units



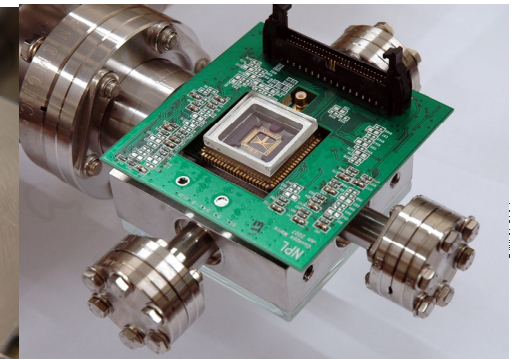
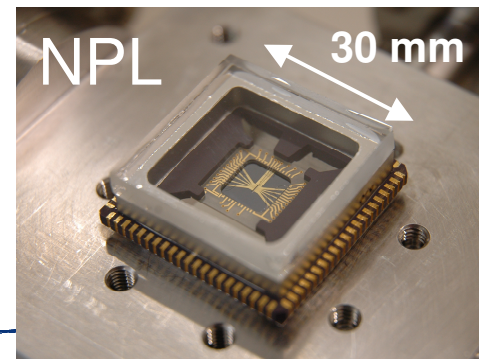
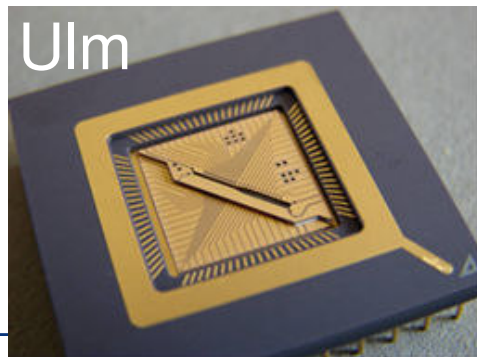
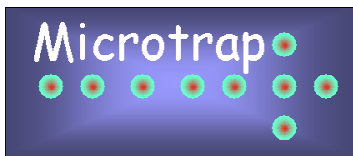
Single pass doubling in PPKTP  
150 mW 844 nm diode →  
0.5 mW of Sr<sup>+</sup> 422 nm cooling light

# Ion clock physics package



$^{88}\text{Sr}^+$  ion trap lab development ~ 10 litre volume

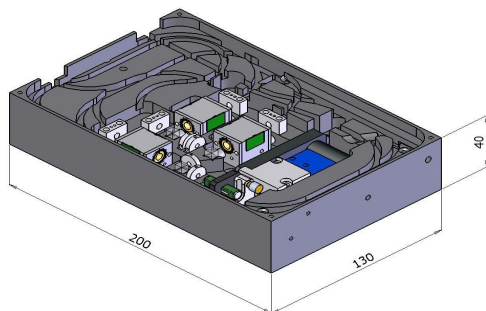
Microtrap development based on gold-coated ceramic wafers (Ulm) or gold-coated single silica-on-silicon wafer (NPL)



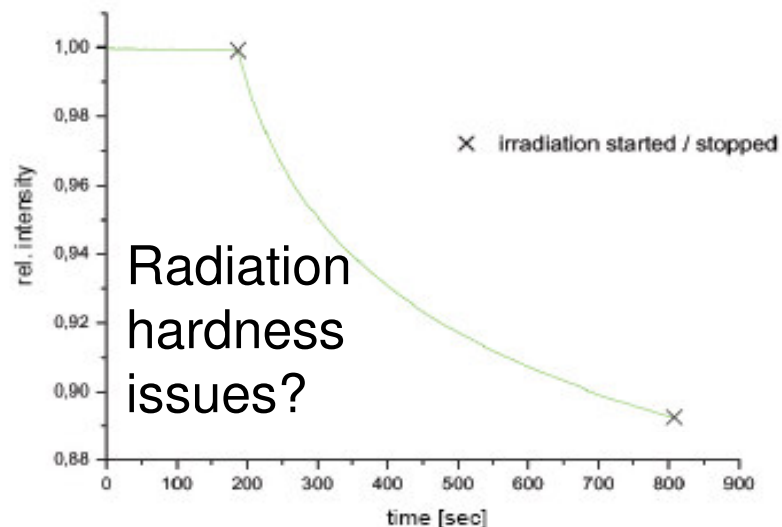
# Femtosecond comb package

Transmissivity of an Er doped fibre (25 mm) irradiated with 2.6 MeV protons of a flux of  $1.9 \cdot 10^{11}$  protons /  $\text{cm}^2 \text{ s}$  (from Predehl 2006).

Commercial fibre-laser based comb



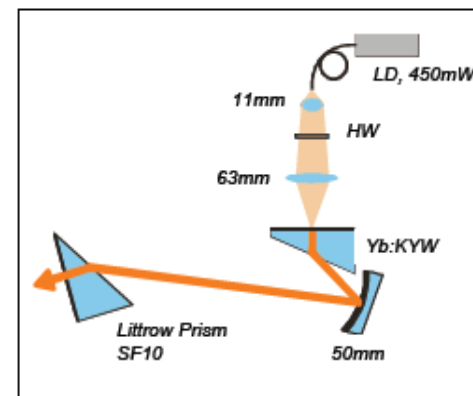
Space version: target vol 1 litre (200x130x40 mm), 5W power



Radiation hardness issues?

Alternative high efficiency fs laser sources

A.A. Lagatsky et al, Opt. Express 12, 3928 (2004)



- Transform-limited 100fs over 1042-1075nm
- Average mode-locked power of 230mW at 294MHz
- **Optical-to-optical conversion efficiency is 53%**



# OAC space clock issues

- Acceleration dependencies
- Influence of cosmic radiation
- Prolonged unattended & maintenance-free operation
- Mass, volume & power
- Operation in vacuum
- Internal spacecraft environment
- External perturbations

Type of optical clock	power (W)	Physics volume (litres)	Physics package mass	Support structure mass	Electronics mass	Total mass
Ion clock	60	50	50 kg	20 kg	30 kg	100 kg

# Conclusion

- Proposal for a technology development programme
  - managed through ESA TEC-MME Directorate
  - involving development activities across the ESA research community in a co-ordinated way
- Input to FPAG road-map construction
- added resource (if successful) for ESA Science / Fundamental Physics strategy for optical clock-based future mission scenarios